# Prolog 

CSC 372, Spring 2015
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## A little background on Prolog

The name comes from "programming in logic".
Developed at the University of Marseilles (France) in 1972.
First implementation was in FORTRAN and led by Alain Colmeraurer.
Originally intended as a tool for working with natural languages.
Achieved great popularity in Europe in the late 1970s.
Was picked by Japan in 1981 as a core technology for their "Fifth Generation Computer Systems" project.

Used in IBM's Watson for NLP (Natural Language Processing).
Prolog is a commercially successful language. Many companies have made a business of supplying Prolog implementations, Prolog consulting, and/or applications in Prolog.

## Prolog resources

There are no Prolog books on Safari.
Here are two Prolog books that I like:
Prolog Programming in Depth, by Covington, Nute, and Vellino Available for free at http://www.covingtoninnovations.com/books/ PPID.pdf. That PDF is scans of pages and is not searchable.

The copy at http://cs.arizona.edu/classes/cs372/springl5/covington/ ppid.pdf has had a searchable text layer added.

Programming in Prolog, 5th edition, by Clocksin and Mellish ("C\&M")
A PDF is available via a UA library link on the Piazza resources page.
(http://link.springer.com.ezproxy2.library.arizona.edu/book/10.1007\%2F978-3-642-55481-0)
A PDF of Dr. Collberg's Prolog slides for 372 is here:
http://cs.arizona.edu/classes/cs372/springl5/CollbergProlog.pdf
There's no Prolog "home page" that I know of.
We'll be using SWI Prolog. More on it soon.

## Facts and queries

## Facts and queries

A Prolog program is a collection of facts, rules, and queries. We'll talk about facts first.

Here is a small collection of Prolog facts:
> \$ cat foods.pl food(apple). food(broccoli). food(carrot). food(lettuce). food(rice).

These facts enumerate some things that are food. We might read them in English like this: "An apple is food", "Broccoli is food", etc.

A fact represents a piece of knowledge that the Prolog programmer deems to be useful. The name food was chosen by the programmer.

We can say that facts.pl holds a Prolog database or knowledgebase.

## Facts and queries, continued

At hand:
\$ cat foods.pl
food(apple).
food(broccoli).
food, apple, and broccoli are examples of atoms, which can be thought of as multi-character literals. Atoms are not strings! Atoms are atoms!

Here are two more atoms:
'bell pepper'
'Whopper'

An atom can be written without single quotes if it starts with a lower-case letter and contains only letters, digits, and underscores.

Note the use of single quotes. (Double quotes mean something else!)

## Sidebar: Accessing the Prolog examples

The Prolog examples from the slides are here: (linked on Piazza resources) /cs/www/classes/cs372/springl5/pl

The a5 write-up suggests making a www symlink in your 372 directory on lectura like this:

```
$ cd ~/372
$ ln -s /cs/www/classes/cs372/springl5 www
```

Given the above you can copy foods.pl into your directory like this:
\$ cd ~/372
\$ cp www/pl/foods.pl .
Because a directory is specified as the destination (dot is the current directory), your copy will be named foods.pl, matching the source name.

Note that "pl" above is is PL, for Prolog.

## Facts and queries, continued

On lectura, we can start SWI Prolog and load a file of facts like this:

$$
\text { \$ swipl -l foods } \quad \text { (.pl suffix is assumed) }
$$

\% /home/whm/372/foods.pl compiled 0.00 sec, 8 clauses
Welcome to SWI-Prolog (Multi-threaded, 64 bits, Version 6.6.6)
?- (-? is the swipl prompt)
Once the knowledgebase is loaded we can perform queries:
?- food(carrot). true.
?- food(pickle).
false.

Prolog responds based on the facts it has been given. We know that pickles are food but Prolog doesn't know that because there's no fact that says so.

A query can consist of one or more goals. The queries above consist of one goal.

## Facts and queries, continued

Here's a fact: food(apple).
Here's a query: food(apple).
Facts and queries have the same syntax. The interpretation depends on the context in which they appear.

If a line is typed at the interactive ?- prompt, it is interpreted as a query.
When a file is loaded with -1 on the command line its contents are interpreted as a collection of facts.

Loading a file of facts is also known as consulting the file.
We'll see later that files can contain "rules", too. Facts and rules are the two types of clauses in Prolog.

Simple rule for now: use all-lowercase filenames with the suffix .pl (PL) for Prolog source files.

## Sidebar: Reconsulting with make

After a .pl file has been consulted (loaded), we can query make. to cause any modified files to be reconsulted (reloaded), after editing the file.
\$ swipl -l foods.pl
Welcome to SWI-Prolog ...
?- food(pickle).
false.
[Edit foods.pl in a different window, and add food(pickle).]
?- make.
\% /home/whm/372/foods compiled 0.00 sec, 2 clauses true.
?- food(pickle).
true.
?- make.
true. (foods.pl hasn't changed since the last make)

## Sidebar: Consulting via query

An alternative to using -l file on the command line is to consult using a query:
\$ swipl
Welcome to SWI-Prolog ...
?- [foods]. (do not include the .pl suffix)
$\%$ foods compiled $0.00 \mathrm{sec}, 8$ clauses true.

Consulting a file via a query is commonly shown in texts.
The end result of the two methods is the same.

## Sidebar: food in Haskell

How might the food information be represented in Haskell?

| food "apple" | $=$ True |
| :--- | :--- |
| food "broccoli" | $=$ True |
| food "carrot" | $=$ True |
| food "lettuce" | $=$ True |
| food "rice" | True |
| food _ | $=$ False |

> food "apple"
True
Maybe a list would be better:
foods = ["apple", "broccoli", "carrot", "lettuce", "rice"]
> "pickle" `elem` foods
False
How might we represent the food information in Ruby?

## Facts and queries, continued

A query like food(apple) asks if it is known that apple is a food.
Speculate: What's the following query asking?
?- food(Edible).
Edible = apple <cursor is here>
Watch what happens when we type semicolons:
Edible = apple ;
Edible = broccoli ;
Edible = carrot ;

Edible = 'Big Mac'.

What's going on?

## Facts and queries, continued

An alternative to specifying an atom, like apple, in a query is to specify a variable. An identifier that starts with a capital letter is a Prolog variable.
?- food(Edible).
Edible $=$ apple <cursor is here>
The above query asks, "Tell me something that you know is a food."
Prolog finds the first food fact, based on file order, and responds with Edible $=$ apple, using the variable name specified in the query.

If the user is satisfied with the answer apple, pressing <ENTER> terminates the query. Prolog responds by printing a period.
?- food(Edible).
Edible $=$ apple.$\%$ User hit <ENTER>; Prolog printed the period.
?-

## Facts and queries, continued

If for some reason the user is not satisfied with the response apple, an alternative can be requested by typing a semicolon, without $\langle E N T E R\rangle$.
?- food(Edible).
Edible = apple ;
Edible = broccoli ;
Edible = carrot ;
Edible = 'Big Mac'.
?-

Facts are searched in the order they appear in foods.pl. Above, the user exhausts all the facts by typing semicolon. Prolog prints '.' after the last.

Note that a simple set of facts lets us perform two distinct computations:
(1) We can ask if something is a food.
(2) We can ask what all the foods are.

How could we make an analog for the above behavior in Java, Haskell, or Ruby?

## Extra credit!

For two points of extra credit:
(1) Get a copy of foods.pl and try the examples just shown.
(2) Create a small database (a file of facts) about something other than food and demonstrate some queries with it using swipl. Minimum: 5 facts.
(3) Copy/paste a transcript of your swipl session into a plain text file named facts.txt.
(4) Turn in facts.txt via the eca3 dropbox before the start of the next lecture.

Needless to say, feel free to read ahead in the slides and show experimentation with the following material, too.

Experiment with syntax, too. Where can whitespace appear? What can appear in a fact other than atoms like apple?

Look ahead a few slides for information about installing SWI Prolog on your machine, or just use swipl on lectura.

## Yes and no vs. true. and false.

Unlike SWI Prolog, most Prolog implementations use "yes" and "no" to indicate whether an interactive query succeeds. Here's GNU Prolog:
\% gprolog
GNU Prolog 1.4.4 (64 bits)
| ?- [foods].
compiling foods.pl for byte code...
| ?- food(apple).
yes
| ?- food(pickle).
no
Most Prolog texts, including Covington and C\&M use yes/no, too. Just read "yes" as true. and "no" as false.

Remember: we're using SWI Prolog; GNU Prolog is shown above just for contrast.

## "Can you prove it?"

One way to think about a query is that we're asking Prolog if something can be "proven" using the facts (and rules) it has been given.

The query
?- food(apple).
can be thought of as asking, "Can you prove that apple is a food?"
food(apple). is trivially proven because we've supplied a fact that says that apple is a food.

The query
?- food(pickle).
produces false. because Prolog can't prove that pickle is a food based on the database (the facts) we've supplied. (We've given it no rules, either.)

## "Can you prove it?", continued

Consider again a query with a variable:

```
?- food(F). \% Remember that an initial capital denotes a variable.
F = apple;
F = broccoli ;
F = carrot ;
F = 'Whopper' ;
F = 'Big Mac'.
```

?-

The query asks, "For what values of F can you prove that F is a food? By repeatedly entering a semicolon we see the full set of values for which that can be proven.

The collection of knowledge at hand, a set of facts about what is a food, is trivial but Prolog is capable of finding proofs for an arbitrarily complicated body of knowledge expressed as facts and rules.

## "Can you prove it?", continued

write is one of many built-in predicates. It outputs a value.
?- write('Hello, world!').
Hello, world!
true.

Speculate: Why was "true." output, too?
Prolog is reporting that it's able to prove write('Hello, world!')!

A side-effect of "proving" write(X) is outputting the value of X !

## Getting and running SWI Prolog

## Getting and running SWI Prolog

swi-prolog.org is the home page for SWI Prolog.
On lectura, just run swipl.
Downloads for Windows and OS X:
http://swi-prolog.org/download/stable
For Windows, the non-64 bit version will be fine for our purposes:
SWI-Prolog 6.6.6 for Windows XP/Vista/7/8
Pick Typical as the Install type, . pl for file extension
For OS X there's only one choice:
SWI-Prolog 6.6.6 for MacOSX 10.6 (Snow Leopard) and later...
As the install page says, you'll need XQuartz 2.7.5 for the development tools. The handiest tool is perhaps the graphical tracer, launched with the gtrace predicate. (We'll see gtrace later.)

## SWI Prolog on Windows

On Windows, assuming you associated .pl files with SWI Prolog, running foods.pl on the command line or opening foods.pl in Explorer opens a window running SWI Prolog and consults the file, as if [foods]. had been typed at the prompt.

```
cs Command Prompt
Z:\whm\Drophox\372\pl\foods . pl
Z:\whm\Drophox\372\pl>
\omega% Sw'I-Prolog -- z:/whm:IDrophox/372/pl/foods.pl
File Edit Settings Run Debug
    % z:/whm/Dropbox/372/p/foods.pl compiled 0.00 sec, 9 clauses
    Welcome to SWI-Prolog (Hulti-threaded, 32 bits, Version 6.6.4)
    Copyright (0) 1990-2013 University of Amsterdam. WU Amsterdam
    SWI-Prolog comes with ABSOLUTELY NO WARRANTY. This is free software.
    and you are welcome to redistribute it under certain conditions.
    Please visit http://www.swi-prolog.org for details.
    For help, use ?- help(Topic). or ?- apropos(Word)
    1 ?-
```

On Windows, a numbered query prompt is shown. ("l ?-" above)
Remember: You can use make. to reconsult (reload) a file.

## SWI Prolog on OS X

On my Mac, I have these two lines in my ~/.bashrc:
alias swipl='/Applications/SWI-Prolog.app/Contents/MacOS/swipl' export DISPLAY=:0

The swipl alias lets me type swipl at the command line prompt.
The export of DISPLAY (to the "environment") avoids this error:
?- help(write).
true.
?- [PCE fatal: @display/display: Failed to connect to X-server at
`/private/tmp/com.apple.launchd.gfBvlvPh7y/ org.macosforge.xquartz:0': ...

## Sidebar: bash start-up file organization

I recommend a bash start-up file organization with two parts:
(1) Have a .bash_profile with only one line: \$ cat ~/.bash_profile source ~/.bashrc
(2) Have all aliases, variable initializations, functions, etc. in your .bashrc:
\$ cat ~/.bashrc
alias $\mathrm{h}=$ "history"
alias ll="ls -l"
...
alias irb="irb --prompt simple -r irb/completion"
alias swipl="/Applications/SWI-Prolog.app/Contents/MacOS/swipl" export DISPLAY=:0
alias restart="source ~/.bashrc"
The restart alias makes it easy to reload your .bashrc after making a change, like adding a new alias.

## Getting help for predicates

To get help for a predicate, query help(predicate-name). On Windows you'll see:

```
@ SW'I-Prolog -- z:/whm/Drophox/372/pl/foods.pl
```

```
File Edit Sertinnes Run Debug Help
5 ?-help(write)
true.
```

6 ?-



OS X will be similar, assuming you've got XQuartz 2.7.5 installed and have done export DISPLAY=:0, as shown on slide 24. Or do unset DISPLAY for text-based help.

Help will be text based on lectura, but if you login to lectura from a Linux machine with "ssh -X ...", you'll get window-based help there, too.

## Getting out of SWI Prolog

On all platforms a control-D or querying halt. exits SWI Prolog. \$ swipl
?- halt.
\$
A control-C while a query is executing will produce an Action ...? prompt. Then typing h produces a textual menu:
?- food(X).
X = apple ${ }^{\text {^C }}$
Action (h for help) ? h Options:

| a: | abort | b: | break |
| :--- | :--- | :--- | :--- |
| c: | continue | e: | exit |
| g: | goals | t: | trace |
| h (?): | help |  |  |

Use a to return to the prompt; e exits to the shell.

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## Building blocks

We've seen that apple, food, and 'Big Mac' are examples of atoms.
Typing an atom as a query doesn't do what we might expect!
?- 'just\ntesting'.
ERROR: toplevel: Undefined procedure: 'just\ntesting'/0 (DWIM could not correct goal)

But we can output an atom with write.
?- write('just $\backslash$ ntesting').
just
testing
true.
Atoms composed of certain non-alphabetic characters do not require quotes:
?- write(\#\$\&*+-./:<=>?^~<br>).
\#\$\&*+-./:<=>? ${ }^{*}$ \
true.

## Atoms, continued

We can use the predicate atom to query whether something is an atom:

```
?- atom(apple).
true.
?- atom('apple sauce').
true.
?- atom(Apple).
false.
?- atom("apple").
false.
```

Alternate view: "Can you prove apple is an atom?"

Integer and floating point literals are numbers.
?- number(10).
true.
?- number(3.4). true.
?- number(3.4el00). true.
?- number('100'). false.

Numbers aren't atoms but they are "atomic" values.
?- atom(100).
false.
?- atomic(100). \% Note: atomIC, not just atom. true.

Numbers, continued
In Prolog, arithmetic doesn't work as you might expect:
?-3+4.
ERROR: toplevel: Undefined procedure: (+)/2 (DWIM could not correct goal)
?-Y $=4+5$.
$Y=4+5$.
?- write $(3+4 * 5)$.
$3+4 * 5$
true.

We'll learn about arithmetic later.

## Predicates, terms, and structures

Here are some more examples of facts:

```
color(sky, blue). color(grass, green).
odd(l). odd(3). odd(5).
number(one, l, 'English').
number(uno, l, 'Spanish').
number(dos, 2, 'Spanish').
```

We can say that the facts above define three predicates: color, odd, and number.

It's common to refer to predicates using predicate indicators like color/2, odd/l, and number/3, where the number following the slash is the number of terms.
number/3 above doesn't interfere with the built-in predicate number/l (two slides back).

## Predicates, terms, and structures, continued

A term is one of the following: atom, number, structure, variable.
Structures consist of a functor (always an atom) followed by one or more terms enclosed in parentheses.

Here are examples of structures:
color(grass, green)
odd(1)
'number'('uno', l, 'Spanish') \% 's not needed around number and uno
$+/-(3,4) \quad$ \% functor is symbolic atom
lunch(sandwich(ham), fries, drink(coke))
The structure functors are color, odd, number, $+/-$, and lunch, respectively.
Two of the terms of the lunch structure are structures themselves.
A structure can serve as a fact or a goal, depending on the context.

## (intentionally blank)

## More queries

## More queries

A new knowledgebase is to the right.

A query about green things:
?- color(Thing, green).
Thing = grass ;
Thing = broccoli ;
Thing = lettuce.

How can we state it in terms of "Can you prove...?"
For what things can you prove that their color is green?

## More queries

How could we query for each thing and its color?
?- color(Thing,Color).
Thing = sky,
Color $=$ blue ;
Thing = dirt,
Color $=$ brown ;
Thing = grass,
Color = green ;
Thing = broccoli, Color = green ;

```
color(sky, blue).
color(dirt, brown).
color(grass, green).
color(broccoli, green).
color(lettuce, green).
color(apple, red).
color(carrot, orange).
color(rice, white).
```

...
How can we state it in terms of "Can you prove...?"
For what pairs of Thing and Color can you prove color(Thing, Color)?

## Queries with multiple goals

A query can contain more than one goal.
Here's a query that directs Prolog to find a food that is green:

```
?- food(F), color(F,green).
F = broccoli ;
F = lettuce ;
false.
```

The query has two goals separated by a comma, which indicates conjunction-both goals must succeed in order for the query to succeed.

We might state it like this:
"Is there an $F$ for which you can prove both food(F) and color(F, green)?

```
$ cat foodcolor.pl
food(apple).
food(broccoli).
food(carrot).
food(lettuce).
food(orange).
food(rice).
color(sky, blue).
color(dirt, brown).
color(grass, green).
color(broccoli, green).
color(lettuce, green).
color(apple, red).
color(carrot, orange).
color(orange,orange).
color(rice, white).
```


## Queries with multiple goals, continued

Let's see if any foods are blue:
?- color(F,blue), food(F).
false.

Note that the ordering of the goals was reversed. How might the order make a difference?

Goals are always executed from left to right.

What's the following query asking?
?- food(F), color(F,F).

How about this one?
?- food(F), color(F,red), color(F, green).

```
food(apple).
food(broccoli).
food(carrot).
food(lettuce).
food(orange).
food(rice).
color(sky, blue).
color(dirt, brown).
color(grass, green).
color(broccoli, green).
color(lettuce, green).
color(apple, red).
color(carrot, orange).
color(orange, orange).
color(rice, white).
```


## Sidebar: The meaning of a fact

Which of the following is meant by color(apple,red)?
All apples are red.
Some apples are red.
Some apples have a red area.
Some apples have a red area at some point in time.
A red apple has existed.
Facts (and rules) are abstractions that we create for the purpose(s) at hand.
An abstraction emphasizes the important and suppresses the irrelevant.
Don't get bogged down by trying to perfectly model the real world!

Even more queries
Write these queries:

Who likes baseball?
?- likes(Who, baseball).

Who likes a food?
?- food(F), likes(Who,F).

Who likes green foods?
?- food(F), color(F,green), likes(Who,F).

Who likes foods with the same color as foods that Mary likes?
?- likes(mary,F), food(F),
color(F, C), food(F2), color(F2,C),
likes(Who,F2).
\$ cat fcl.pl food(apple).
...more food facts...
color(sky, blue).
...more color facts...
likes(bob, carrot). likes(bob, apple). likes(joe, lettuce).
likes(mary, broccoli).
likes(mary, tomato).
likes(bob, mary).
likes(mary, joe).
likes(joe, baseball).
likes(mary, baseball).
likes(jim, baseball).

Even more queries, continued
Are any two foods the same color?
?- food(Fl), food(F2), color(Fl,C), color(F2,C).
$\mathrm{Fl}=\mathrm{F} 2, \mathrm{~F} 2=$ apple, $\%$ an apple is the same color as an apple(!)
C = red;

$$
\begin{aligned}
& \text { F1 = F2, F2 = broccoli, } \\
& \mathrm{C}=\text { green ; }
\end{aligned}
$$

To avoid foods matching themselves we can specify "not equal" with $\backslash==$ (symbolizing a struck-through $==$ ).
?- food(Fl), food(F2), Fl \== F2, color(Fl,C), color(F2,C).
Fl = broccoli,
F2 = lettuce,
C = green ;
Fl = carrot,
F2 = C, C = orange ;

## Sidebar: Predicates in operator form

Recall that in Haskell, $3+4$ can be written as (+) 34.
In Prolog, these two queries are equivalent:
?-abc $\backslash==x y z$.
true.
?- $\backslash==(a b c, x y z)$.
true.
In fact, the sequence $\mathrm{abc} \backslash==\mathrm{xyz}$ causes Prolog to create a structure.
display/l can be used to show a structure:
?- display(abc \== xyz).
$\backslash==(\mathrm{abc}, \mathrm{xyz})$
Ultimately, abc $\backslash==\mathrm{xyz}$ means "invoke the predicate named $\backslash==$ and pass it two terms, abc and xyz".

## Sidebar, continued

display sheds a little light on the arithmetic oddities we saw earlier.
?- display(l + 2).
$+(1,2)$
true.
?- display ( $1+2$ * $3-5$ ).
$-(+(1, *(2,3)), 5)$
true.
Just FYI: The predicate $\mathrm{op} / 3$ is used to create operators.
?- op(200,'xf',--). \% precedence 200 postfix operator true.
?- display ( $\mathrm{x}+\mathrm{y}--$ ).
$+(\mathrm{x},--(\mathrm{y}))$
true.

Query help(op). to learn more!

## Alternative representations

A given body of knowledge may be represented in a variety of ways using Prolog facts. Here is another way to represent the food and color information.

What are orange foods?
?- thing(Name, orange, yes).
Name = carrot ;
Name = orange.

What things aren't foods?
?- thing(Name, _, no).
Name = dirt ;
Name = grass ;

```
thing(apple, red, yes).
thing(broccoli, green, yes).
thing(carrot, orange, yes).
thing(dirt, brown, no).
thing(grass, green, no).
thing(lettuce, green, yes).
thing(orange, orange, yes).
thing(rice, white, yes).
thing(sky, blue, no).
```

Name = sky.

The underscore designates an anonymous variable. It indicates that any value matches and that we don't want to have the value associated with a variable (and thus displayed).

Alternate representation, continued

What is green that is not a food?
?- thing( N, green, no ).
$\mathrm{N}=$ grass ;
false.
What color is lettuce?
?- thing(lettuce,C,_).
C = green.
What foods are the same color as lettuce?
?- thing(lettuce, C,_), thing(N,C,yes), $\mathrm{N} \backslash==$ lettuce.
C = green,
$\mathrm{N}=$ broccoli ;
false.
Is thing/ 3 a better or worse representation of the knowledge than the combination of food/l and color/2?

## Predicate/goal mismatches

Here is a predicate $\mathbf{x}$ defined by three facts:

```
x(just(testing,date(5,14,2014))).
x(10).
x(10,20).
```

The first fact's term is a structure but the second fact's term is a number. That inconsistency is not considered to be an error.

```
?- x(V).
V = just(testing, date(5, 14, 2014));
V = 10.
```

Further, is it $\mathbf{x} / \mathrm{l}$ or $\mathrm{x} / 2$ ?

$$
\begin{aligned}
& ?-x(A, B) . \\
& A=10, \\
& B=20 .
\end{aligned}
$$

## Predicate/goal mismatches, continued

At hand:
$\mathrm{x}(\mathrm{just}($ testing, date(5,14,2014))).
$\mathrm{x}(10)$. $\mathrm{x}(\mathrm{A}, \mathrm{B})$.

Here are some more queries:
?- $x(a b c)$.
false.
?- x([1,2,3]). \% A list... false.

```
?- x(a(b)).
false.
```

The goals in the queries have terms that are an atom, a list, and a structure.
There's no indication that those queries are fundamentally mismatched with respect to the terms in the facts.

Prolog says "false" in each case because nothing it knows about aligns with anything it's being queried about.

## Predicate/goal mismatches, continued

At hand:
x(just(testing,date(5,14,2014))).
$\mathrm{x}(\mathrm{l} 0)$. $\mathrm{x}(\mathrm{A}, \mathrm{B})$.
It's an error if there's no predicate defined that has the same number of terms as the goal in a query. Alternatives are suggested.
?- x(little,green,apples).
ERROR: Undefined procedure: x/3
ERROR: However, there are definitions for:
ERROR: $\mathrm{x} / \mathrm{l}$
ERROR: $\mathrm{x} / 2$

What does the following tell us?
?- write ( 1,2 ).
ERROR: write/2: Domain error: `stream_or_alias' expected, found 'l'

## (intentionally blank)

## Unification

## $==$ and $\backslash==$ are tests

Before talking about unification lets note that $==$ and $\backslash==$ are tests. They are roughly equivalent to Haskell's $==$ and $/=$, and Ruby's $==$ and $!=$.
?- $\mathrm{abc}==$ 'abc'.
true.
?-3 $3 \backslash=5$.
true.

Just like comparing tuples and lists in Haskell, and arrays in Ruby, structure comparisons in Prolog are "deep". Two structures are equal if they have the same functor, the same number of terms, and the terms are equal. (Recursive def'n.)
? $-3+4==4+3$.
false.
?- $\operatorname{abc}(3+4 * 5)==\operatorname{abc}(+(3,4 * 5))$.
true.

## Unification

The $=$ operator, which we'll read as "unify" or "unify with", provides one way to do unification.

If a variable doesn't have a value it is said to be uninstantiated. At the start of a query all variables are uninstantiated.

If we unify an uninstantiated variable with a value, the variable is instantiated and unified with that value.

$$
\begin{aligned}
& ?-A=10, \text { write }(A) . \\
& 10 \\
& A=10 .
\end{aligned}
$$

It can be read as "Unify A with 10 and write A."
That might look like assignment but it is not assignment!
Along with the output, " 10 ", the value of $A$ is shown.

## Unification, continued

At hand:

$$
\begin{aligned}
& ?-A=10, \text { write }(A) . \\
& 10 \\
& A=10 .
\end{aligned}
$$

An instantiated variable can be unified with a value only if the value equals (with $==/ 2$ ) whatever value the variable is already unified with.

```
?- A = 10, write(A), A = 20, write(A).
10
false.
```

The unification of the uninstantiated $A$ with 10 succeeds, and write(A) succeeds, but unification of $A$ with 20 fails because $10==20$ fails.

The query fails because its third goal, the unification $A=20$, fails.
In essence the query is saying $A$ must be 10 and $A$ must be 20. Impossible!

## Unification, continued

The lifetime of a variable is the query in which it is instantiated.

$$
\begin{aligned}
& ?-A=10, B=20, \text { write }(A), \text { write }(', '), \text { write(B). } \\
& 10,20 \\
& A=10 \\
& B=20 .
\end{aligned}
$$

If we use $A, B$, and (out of the blue) $C$ in the next query, we find they are uninstantiated:

```
?- write(A), write(', '), write(B), write(', '), write(C).
```

_G1571,_G1575,_G1579
true.

Writing the value of an uninstantiated variable produces _G<NUMBER>.
Some say bound variable and free variable for instantiated and not.

## Unification, continued

Consider the following:
?- A = B, C = 10, C = B, write (A).
10
$A=B, B=C, C=10$.
The code above...
Unifies A with B (but both are still uninstantiated).
Unifies C (uninstantiated) with 10.
Unifies B with C.
Because $A$ and $B$ are already unified, and $\mathbf{C}$ is instantiated with $10, A, B$, and $C$ now have the value 10 .

How will an initial instantiation for $A$ affect the query?
?- $A=3, A=B, C=10, C=B$, write(A).
false.

## Unification, continued

With uninstantiated (free) variables, unification has a behavior when unifying with values that resembles conventional assignment.

With instantiated (bound) variables, unification has a behavior when unifying with values that resembles comparison.

Unification of uninstantiated variables seems like aliasing of some sort.
But don't think of unification as assignment, comparison and aliasing rolled into one. Think of unification as a distinct new concept!

Another way to think about things:
Unification is not a question or an action, it is a demand!
$X=3$ is a goal that demands that $X$ must be 3 . If not, the goal fails.
Yet another:
Unifications create constraints that Prolog upholds.

## Unification with structures

Unification works with structures, too.

$$
\begin{aligned}
& ?-x(A, B)=x(10,20) . \\
& A=10 \\
& B=20 .
\end{aligned}
$$

?- $f(X, Y, Z)=f(j u s t$, testing, $f(a, b, c+d))$.
$\mathrm{X}=$ just,
$\mathrm{Y}=$ testing,
$Z=f(a, b, c+d)$.
?- $f(X, Y, f(P l, P 2, P 3))=f(j u s t$, testing, $f(a, b, c+d))$.
$X=$ just,
$\mathrm{Y}=$ testing,
$\mathrm{Pl}=\mathrm{a}$,
$\mathrm{P} 2=\mathrm{b}$,
P3 $=c+d$.

## Unification with structures, continued

?- $\operatorname{pair}(A, A)=\operatorname{pair}(3,5)$.
false.
?- $\operatorname{pair}(A, A)=\operatorname{pair}(3,3)$.
$A=3$.
?- lets(r,a,d,a,r) $=\operatorname{lets}(\mathrm{Cl}, \mathrm{C} 2, \mathrm{C} 3, \mathrm{C} 2, \mathrm{Cl})$.
$\mathrm{Cl}=\mathrm{r}$,
C2 $=\mathrm{a}$,
C3 $=\mathrm{d}$.
?- $f(X, 20, Z)=f(10, Y, 30), N e w=f(Z, Y, X)$.
$\mathrm{X}=10$,
$\mathrm{Z}=30$,
$\mathrm{Y}=20$,
New $=f(30,20,10)$.

## Unification with structures, continued

Consider again this interaction:
?- food(F).
F = apple;
F = broccoli ;

The query food(F) causes Prolog to search for facts that unify with food(F).
Prolog is able to unify food(apple) with food(F). It then shows that $F$ is unified with apple.

When the user types semicolon, $F$ is uninstantiated and the search for another fact to unify with food $(F)$ resumes with the fact following food(apple).
food(broccoli) is unified with food( $F$ ), $F$ is unified with broccoli, and the user is presented with $\mathrm{F}=$ broccoli.

The process continues until Prolog has found all the facts that can be unified with food $(F)$ or the user is presented with a value for $F$ that is satisfactory.

## (intentionally blank)

## (intentionally blank)

## Query evaluation mechanics

Understanding query execution with the port model
Goals, like food(fries) or color(What, Color) can be thought of as having four ports:


In the Active Prolog Tutor, Dennis Merritt describes the ports in this way:
call: Using the current variable bindings, begin to search for the clauses which unify with the goal.
exit: Set a place marker at the clause which satisfied the goal. Update the variable table to reflect any new variable bindings. Pass control to the right.
redo: Undo the updates to the variable table [that were made by this goal]. At the place marker, resume the search for a clause which unifies with the goal.
fail: No (more) clauses unify, pass control to the left.

## The port model, continued

Example:
?- food(X).
X = apple ;
$\mathrm{X}=$ broccoli ;
X = carrot ;
$\mathrm{X}=$ lettuce ;
$\mathrm{X}=$ rice.
?-


$$
\begin{aligned}
& \text { food(apple). } \\
& \text { food(broccoli). } \\
& \text { food(carrot). } \\
& \text { food(lettuce). } \\
& \text { food(rice). }
\end{aligned}
$$

trace/ 0 activates "tracing" for a query.
?- trace, food(X).
Call: (7) food(_G1571) ? creep
Exit: (7) food(apple) ? creep
X = apple ;
Redo: (7) food(_G1571) ? creep
Exit: (7) food(broccoli) ? creep
X = broccoli ;
Redo: (7) food(_G1571) ? creep
Exit: (7) food(carrot) ? creep

The port model, continued


$$
\begin{aligned}
& \text { food(apple). } \\
& \text { food(broccoli). } \\
& \text { food(carrot). } \\
& \text { food(lettuce). } \\
& \text { food(rice). }
\end{aligned}
$$

Tracing shows the transitions through each port. The first transition is a call to the goal food(X). The value shown,_G1571, stands for the uninstantiated variable X . We next see that goal being exited, with X instantiated to apple. The user isn't satisfied with the value, and by typing a semicolon forces the redo port to be entered, which causes X, previously bound to apple, to be uninstantiated. The next food fact, food(broccoli) is tried, instantiating $X$ to broccoli, exiting the goal, and presenting $\mathrm{X}=$ broccoli to the user. (etc.)

The port model, continued
Who likes green foods?
?- food(F), likes(Who,F), color(F, green).

likes(bob, carrot).
likes(bob, apple). likes(joe, lettuce). likes(mary, broccoli). likes(mary, tomato). likes(bob, mary). likes(mary, joe). likes(joe, baseball). likes(mary, baseball). likes(jim, baseball).

## Next: Trace it!

## Producing output

We've seen that write/l always succeeds and as a side effect outputs the term it is called with.
?- write(apple), write(' '), write(pie).
apple pie
true.
writeln/l is similar, but appends a newline.
?- writeln(apple), writeln(pie).
apple
pie
true.
$\mathrm{nl} / 0$ outputs a newline. (Note the blank lines before and after middle.)
?- nl, writeln(middle), nl.
middle
true.

## Producing output, continued

The predicate format/2 is much like printf in Ruby, C, and others.
?- format(' $\mathrm{x}=\sim \mathrm{w} \backslash \mathrm{n}$ ', 101).
$\mathrm{x}=101$
true.
$\sim \mathrm{w}$ is one of many format specifiers. The " w " indicates to output the value using write/l. Use help(format/2) to see all the specifiers. (Don't forget the $/ 2$ !)

If more than one value is to be output, the values must be in a list.

$$
\text { ?- format('label }=\sim w, \text { value }=\sim w, x=\sim w \backslash n ',[' a b c ', 10,3+4]) .
$$

label $=\mathrm{abc}$, value $=10, \mathrm{x}=3+4$ true.

We'll see more on lists later but for now note that we make a list by enclosing zero or more terms in square brackets. Lists are heterogeneous, like Ruby arrays.

## Producing output, continued

A first attempt to print all the foods:
?- food $(F)$, format(' $\sim \mathrm{w}$ is a food $\left.\backslash n^{\prime}, F\right)$.
apple is a food
F = apple;
broccoli is a food
F = broccoli ;
carrot is a food
F = carrot ;

Ick-we have to type semicolons to cycle through them!
Any ideas?

## Producing output, continued

Second attempt: Force alternatives by specifying a goal that always fails.
?- food( $F$ ), format( ${ }^{\prime} \sim \mathrm{w}$ is a food $\left.\backslash n^{\prime}, F\right), \mathrm{l}==2$.
apple is a food
broccoli is a food
carrot is a food


This query is a loop! food $(F)$ unifies with the first food fact and instantiates $F$ to its term, the atom apple. Then format is called, printing a string with the value of $F$ interpolated. $l==2$ always fails. Control then moves left, into the redo port of format. format doesn't erase the output but it doesn't have an alternatives either, so it fails, causing the redo port of food $(F)$ to be entered. $F$ is uninstantiated and food $(F)$ is unified with the next food fact in turn, instantiating F to broccoli. The process continues, with control repeatedly moving back and forth until all the food facts have been tried.

## At hand:

## Backtracking

?- food( F ), format(' $\sim \mathrm{w}$ is a food $\left.\backslash \mathrm{n}^{\prime}, \mathrm{F}\right), \mathrm{l}==2$.
apple is a food broccoli is a food


The activity of moving leftwards through the goals is known as backtracking.

We might say, "The query gets a food F, prints it, fails, and then backtracks to try the next food."

Prolog does not analyze things far enough to recognize that it will never be able to "prove" what we're asking. Instead it goes through the motions of trying to prove it and as side-effect, we get the output we want. This is a key idiom of Prolog programming.

## Backtracking, continued

At hand:
?- food( $F$ ), format(' $\sim \mathrm{w}$ is a food $\left.\backslash \mathrm{n}^{\prime}, \mathrm{F}\right), \mathrm{l}==2$.
apple is a food
broccoli is a food
false.

Predicates respond to "redo" in various ways. With only a collection of facts for food/l, redo amounts to advancing to the next fact, if any. If there is one, the goal exits (control goes to the right). If not, it fails (control goes to the left).

Some other possible examples of "redo" behavior:
A sequence of redos might cause a predicate to work through a series of URLs to find a current data source.

A geometry manager might force a collection of windows to produce a configuration that is mutually acceptable.

A predicate might create a file when called and delete it on redo.

## The predicate fail

The predicate fail/0 always fails. It's important to understand that an always-failing goal like $\mathrm{l}==2$ produces exhaustive backtracking but in practice we'd use fail instead:
?- food(F), format(' $\sim \mathrm{w}$ is a food $\left.\backslash n^{\prime}, F\right)$, fail.
apple is a food
broccoli is a food
rice is a food false.

In terms of the four-port model, think of fail as a box whose call port is "wired" to its fail port:


## Sidebar: between

The built-in predicate between/3 can be used to instantiate a variable to a sequence of integer values:
?- between ( $1,3, \mathrm{X}$ ).
X = 1 ;
$\mathrm{X}=2$;
$X=3$.

Problem: Print this sequence:
000
001
010
011
100
101
110

| How about <br> this one? |
| :--- |
|  |
| 10101000 |
| 10101001 |
| 10101010 |
| 10101011 |
| 10111000 |
| 10111001 |
| 10111010 |
| 10111011 |

111
?- between( $0,1, A$ ), between( $0,1, B$ ), between( $(0,1, C)$, format(' $\sim \mathrm{w} \sim \mathrm{w} \sim \mathrm{w} \backslash \mathrm{n} ', ~[A, B, C])$, fail.

## Rules

Facts are one type of Prolog clause. The other type of clause is a rule.
foods2.pl starts with a rule and is followed by the food facts:


Even though showfoods/0 uses food/l, it can either precede or follow the clauses for that predicate.

## showfoods, continued

At hand:
\$ cat foods2.pl showfoods :- food(F), format(' $\sim \mathrm{w}$ is a food $\backslash n ', F)$, fail.
food(apple). food(broccoli).

Usage:
\$ swipl -l foods2
?- showfoods. apple is a food broccoli is a food carrot is a food lettuce is a food orange is a food rice is a food
false.

## Sidebar: Horn Clauses

Prolog borrows from the idea of Horn Clauses in symbolic logic. A simplified definition of a Horn Clause is that it represents logic like this:

If $Q_{1}, Q_{2}, Q_{3}, \ldots, Q_{n}$, are all true, then $P$ is true.
In Prolog we might represent a three-element Horn clause with this rule:
p :- ql, q2, q3.

The query
?- p.
which asks Prolog to "prove" p , causes Prolog to try and prove ql , then q 2 , and then q 3 . If it can prove all three, and can therefore prove p , Prolog will respond with true. (If not, then false.)

Note that this is an abstract example-we haven't defined the predicates ql/0 et al.

## showfoods, continued

At hand are the following rules:
$\mathrm{p}:-\mathrm{ql}, \mathrm{q} 2, \mathrm{q} 3$.
showfoods :- food(F), format( $(\sim \mathrm{w}$ is a food $\backslash n ', F)$, fail.
We saw that we can print all the foods with this query:
?- showfoods.
apple is a food
broccoli is a food carrot is a food
rice is a food false.

In its unsuccessful attempt to "prove" showfoods, and thus trying to prove all three goals in the body of the showfoods rule, Prolog ends up doing what we want: all the foods are printed.

We send Prolog on a wild goose chase to get our work done!

## showfoods, continued

Let's print all the foods three times.
?- showfoods, showfoods, showfoods. apple is a food broccoli is a food carrot is a food lettuce is a food orange is a food rice is a food false.

What's wrong?

## showfoods, continued

At hand:

```
showfoods :- food(F), format('~w is a food\n', F), fail.
```

?- showfoods, showfoods, showfoods.
apple is a food
broccoli is a food
rice is a food false.
(Just one listing of the foods)
Why does Prolog say false. after printing the foods?
The showfoods rule above always fails-we can't get past the fail at the end!

We get the output we want but because the first showfoods goal ultimately fails Prolog doesn't try the second two goals-it can't get past the first goal!

## showfoods, continued

The problem: We're using a fail to force display of all the foods but we want showfoods to ultimately succeed. Any ideas?
showfoods :- food(F), format(' $\sim \mathrm{w}$ is a food $\backslash n ', F)$, fail. showfoods.

Result:
?- showfoods.
apple is a food
broccoli is a food
rice is a food
true. \% Very important: Now it says true., not false.
Prolog tries the two clauses for the predicate showfoods in turn. The first clause, a rule, isultimately a failure but prints the foods as a side-effect. Because the first clause fails, Prolog tries the second clause, a fact which is trivially proven.

## showfoods, continued

At hand:
showfoods :- food(F), format(' $\sim \mathrm{w}$ is a food $\backslash n^{\prime}$, $F$ ), fail. showfoods.
?- showfoods. apple is a food broccoli is a food
true. $\%$ Very important: Now it says true., not false.

The underlying rule:
If a clause fails, Prolog tries the predicate's next clause. It continues until a clause succeeds or no clauses remain.

This is the same mechanism we've been using to go through foods, colors, and more.

## Rules with arguments

Here is a one-rule predicate that asks if there is a food with a particular color:
food_color(Color) :- food(F), color(F,Color). \% in foods2.pl
Usage:
?- food_color(green).
true
To prove the goal food_color(green), Prolog first searches its clauses for one that can be unified with the goal. It finds a rule (above) whose head can be unified with the goal. That unification causes Color to be instantiated to the atom green.

It then attempts to prove food( $F$ ), and $\operatorname{color}(F$, green) for some value $F$.
The response true tells us that at least one green food exists, but that's all we know.

## Rules with arguments, continued

At hand:
food_color(Color) :- food(F), color(F,Color).
The last slide didn't tell the whole truth. The cursor pauses right after true:
?- food_color(green).
true _ (blink...blink...blink)
If we type semicolons we see this:
?- food_color(green).
true;
true ;
false.
It reveals that food_color(green) is actually finding two green foods but we don't know what they are.

A failure:
?- food_color(blue).
false.

## Rules with arguments, continued

At hand:
food_color(Color) :- food(F), color(F,Color).
Does food_color let us do anything other than asking if there is a food with a particular color?

We can ask for all the colors of foods.
?- food_color(C).
C = red ;
C = green ;
C = orange ;
C = green ;
C = white.
We get green twice because there are two green foods. We'll later see ways to deal with that.

At hand:

```
food_color(Color) :- food(F), color(F,Color).
```

?- food_color(C).
C = red;
C = green ;

A very important rule:
These are unified

When a variable is supplied in a query and it matches a fact or the head of a rule with a variable in the corresponding term, the two variables are unified. (Instantiating one instantiates the other.)

In the above case the variable $\mathbf{C}$ first has the value red because $\mathbf{C}$ in the query was unified with Color in the head of the rule, AND the goals in the body of the rule succeeded, AND Color was instantiated to red.

When we type a semicolon in response to $\mathbf{C}=$ red, Prolog backtracks and ultimately comes up with green.

At hand:

```
    food_color(Color) :- food(F), color(F,Color).
```

Prolog has no analog for "return x"! In Prolog there is no way to say something like this,
?- Color = food_color(), writeln(Color), fail.
or this,
?- writeln(food_color()), fail.
Instead, predicates "return" values by instantiating logical variables.
?- food_color(C), writeln(C), fail. red green

Some examples of instantiation as "return" with built-in predicates:
?- atom_length(testing, Len).
Len $=7$.
?- upcase_atom(testing, Caps).
Caps = 'TESTING'.
?- term_to_atom(date(10,1,1891), A).
A = 'date(10,1,1891)'.
?- term_to_atom(T, 'date(10,1,1891)').
$\mathrm{T}=\operatorname{date}(10,1,1891)$.
?- term_to_atom(date(M,D,Y), 'date(10,1,1891)').
$\mathrm{M}=10$,
$\mathrm{D}=1$,
$\mathrm{Y}=1891$.

## Instantiation as "return", continued

Problem: Using term_to_atom write a predicate with this behavior:
?- swap('ten-four', R).
R = 'four-ten'.

First cut:
swap(A, Result) :term_to_atom(T,A), First-Second = T, Swapped = Second-First, term_to_atom(Swapped, Result).

How many variables are used in swap/2 above?

Better:
swap2(A, Result) :-
term_to_atom(First-Second, A), term_to_atom(Second-First, Result).

Problem: Write a predicate with these three behaviors:
?- describe_food(apple-X).
$\mathrm{X}=$ red.
?- describe_food(X-green).
X = broccoli ;
$\mathrm{X}=$ lettuce ;
false.
?- describe_food(X).
X = apple-red;
$\mathrm{X}=$ broccoli-green ;
$\dddot{\mathrm{X}}=$ orange-orange ;
$\mathrm{X}=$ rice-white.
Solution:
describe_food(Food-Color) :- food(Food), color(Food,Color).

## Sidebar: Describing predicates

Recall between(1,10,X). Here's what help(between) shows:
between(+Low, +High, ?Value)
Low and High are integers, High >= Low. If Value is an integer, Low $=<$ Value $=<$ High. When Value is a variable it is successively bound to all integers between Low and High. ...

If an argument has a plus prefix, like +Low and +High, it means that the argument is an input to the predicate and must be instantiated. A question mark indicates that the argument can be input or output, and thus may or may not be instantiated.

The documentation implies that between can (1) generate values and (2) test for membership in a range.
?- between ( $1,10, \mathrm{X}$ ).
$\mathrm{X}=1$;

> Note: This is a documentation convention; do not use the + and ? symbols in code!
?- between(1,10,5). true.

## Describing predicates, continued

Another:
term_to_atom(?Term, ?Atom)
True if Atom describes a term that unifies with Term. When Atom is instantiated, Atom is converted and then unified with Term. ...

Here is a successor predicate:
succ(? $\operatorname{lnt} 1, ? \operatorname{lnt} 2)$
True if $\operatorname{Int} 2=\ln t 1+1$ and $\operatorname{Int1}>=0$. At least one of the arguments must be instantiated to a natural number. ...
?- $\operatorname{succ}(10, N)$.
$\mathrm{N}=1 \mathrm{l}$.

There's no pred (predecessor) predicate. Why?
?- $\operatorname{succ}(\mathrm{N}, 10)$.
$\mathrm{N}=9$.

## Describing predicates, continued

Here is the synopsis for format/2:
format(+Format, +Arguments)
Speculate: What does sformat/3 do?
sformat(-String, +Format, +Arguments)
The minus in -String indicates that the term should be an uninstantiated variable.
?- sformat( $\mathrm{S}, \mathrm{x}=\sim \mathrm{w}$ ', l).
S = "x = 1".
?- sformat("x = l", 'x = ~w', l).
false.

## (intentionally blank)

## (intentionally blank)

## (intentionally blank)

## Arithmetic

## Arithmetic

We've seen that Prolog builds structures out of expressions with operators.
?- display $(1+2 * 3)$.
$+(1, *(2,3))$
?- display(1/2 + (3*4)).
$+(/(1,2), *(3,4))$
?- display $(300.0 / X *(3+A * 0.7 * * Y))$.
*(/(300.0,_G204),+(3,*(_G212,**(0.7,_G210))))
Unlike $==$ and $\backslash==$, there are no predicates for the arithmetic operators.
?- $\backslash==(3,4)$.
true.
?- + $(3,4)$.
ERROR: toplevel: Undefined procedure: (+)/2 ...
Question: Why are there no predicates for arithmetic operators?
$\mathrm{X}==\mathrm{Y}$ works fine as a goal but what we would do with the result of $3+4$ ?
There's simply no notion of expressions producing a value!

## Arithmetic, continued

The predicate is/ 2 evaluates a structure representing an arithmetic expression and unifies the result with a logical variable.

$$
\begin{aligned}
& \text { ?- is }(X, 3+4 * 5) . \\
& X=23 .
\end{aligned}
$$

is/2 is usually used as an infix operator:
?- X is $3+4, \mathrm{Y}$ is $7 * 5, \mathrm{Z}$ is $\mathrm{X} / \mathrm{Y}$.
$\mathrm{X}=7$,
$Y=35$,
$\mathrm{Z}=0.2$.

All variables in the structure being evaluated by is $/ 2$ must be instantiated:
?- $A$ is $3+X$.
ERROR: is/2: Arguments are not sufficiently instantiated

## Arithmetic, continued

It is not possible to directly specify an arithmetic expression as an argument of most predicates, but we'll later see some exceptions.
?- write(3+4).
3+4
true.
?-3+4 == 7 .
false.
?- between(1,5+5, 7).
ERROR: between/3: Type error: 'integer' expected, found `5+5'

## Arithmetic, continued

A full set of arithmetic operations is available. Here are some of them:


## Arithmetic, continued

Here are some predicates that use arithmetic. Remember that we have to "return" values via instantiation.

```
around(Prev,X,Next) :- Prev is X - l,Next is X + l.
area(rectangle(W,H), A) :- A is W * H.
area(circle(R), A) :- A is pi * R ** 2.
length(point(Xl,Y1), point(X2,Y2), Length) :-
    Length is sqrt((X1-X2)**2+(Y1-Y2)**2). % note structure as sqrt arg!
?- around(P,7,N).
P = 6,
N = 8.
?- area(circle(3),A).
A = 28.274333882308138.
?- area(rectangle(2*3,2+2),Area).
Area = 24.
?- length(point(3,0),point(0,4),Len).
Len =5.0.
```


## Comparisons

There are several numeric comparison operators.
$\mathrm{X}=:=\mathrm{Y} \quad$ numeric equality
$\mathrm{X}=\backslash=\mathrm{Y} \quad$ numeric inequality
$\mathrm{X}<\mathrm{Y} \quad$ numeric less than
$\mathrm{X}>\mathrm{Y} \quad$ numeric greater than
$\mathrm{X}=<\mathrm{Y} \quad$ numeric equal or less than (NOTE the order, not $<=$ !)
$\mathrm{X}>=\mathrm{Y} \quad$ numeric greater than or equal
Just like is $/ 2$, they evaluate their operands. Examples of usage:
?- $3+5=:=2 * 3+2$.
true.
? X is $3 / 5, \mathrm{X}>\mathrm{X} * \mathrm{X}$.
$\mathrm{X}=0.6$.
?- X is random(10), $\mathrm{X}>5$.
false.
?- X is random(10), $\mathrm{X}>5$.
$\mathrm{X}=9$.
Note that the comparisons produce no value; they simply succeed or fail.

## NOTE: REPLACEMENT for slide 108

## Example: Grade computation (and "cut")

## Example: grade computation

Here is grade(+Score, ?Grade):
grade(Score, 'A') :- Score >= 90.
grade(Score, 'B') :- Score >= 80, Score < 90.
grade(Score, 'C') :- Score >= 70, Score < 80.
grade(Score, 'F') :- Score < 70.
Usage:
?- grade(95,G).
$\mathbf{G}=$ 'A' ; (user entered semicolon)
false.
?- grade(82,G).
$\mathbf{G}=$ ' B '; (user entered semicolon)
false.
?- grade(50,G).
G = 'F'.
(swipl printed period)
Why did the first two prompt the user?
There were still untried clauses for grade/2.

## Grade computation, continued

Here are some student facts:
student('Ali', 85).
student('Chris',92).
student('Kendall', 89).
Problem: write grades/0, which behaves like this:
?- grades.
Current Grades
Ali: B
Chris: A
Kendall: B
true.

Solution:
grades :- writeln('Current Grades'), student(Student,Score), grade(Score, Grade), format(' $\sim \mathrm{w}: \sim \mathrm{w} \backslash \mathrm{n}$ ', [Student, Grade]), fail.
grades.

Here's a new version of grade/2:

## Grade computation, continued

grade(Score, 'A') :- Score >= 90.
grade(Score, 'B') :- Score >= 80.
grade(Score, 'C') :- Score >= 70.
grade(_, 'F'). :- Grade = 'F'. Note use of underscore for "don't care".

Let's try grades/0 again:
?- grades.
Current Grades
Ali: B
Ali: C
Ali: F
Chris: A
Chris: B
Chris: C
Chris: F
Kendall: B
Kendall: C
Kendall: F
true.
What's wrong?

Here is grades/0:
grades :- writeln('Current Grades'),
student(Student,Score), grade(Score,Grade), format(' $\sim \mathrm{w}: \sim \mathrm{w} \backslash \mathrm{n}$ ', [Student, Grade]), fail. grades.

The old grade/2:
grade(Score, 'A') :- Score >= 90.
grade(Score, 'B') :- Score >= 80, Score < 90.
grade(Score, 'C') :- Score >=70, Score < 80.
grade(Score, 'F') :- Score < 70.

The fail in grades is driving grade to try subsequent rules. Ali's 85 satisfies the last three rules in the new version of grade/2! Chris' 92 satisfies all four!

The predicate ! is "cut". It's just an exclamation mark.
Cut is a control predicate, like fail/0. It affects the flow of control.
When a cut is encountered in rule it means,
"If you get to here, you have picked the right rule to produce a final answer for this call of this predicate."

We can fix grade/ 2 with some cuts: grade(Score, 'A') :- Score >=90, !. grade(Score, 'B') :- Score $>=80$, !.
grade(Score, 'C') :- Score >=70, !. grade(_, 'F'). :- Grade = 'F'.

The rule grade(Score, 'A') :- Score >= 90, !. says,
If score $>=90$ then the grade is an "A", and that's my final answer.

## Cut, continued

How does the behavior change if we do the cut first instead of last?
grade(Score, 'A') :- !, Score >= 90.
grade(Score, 'B') :- !, Score $>=80$.
grade(Score, 'C') :- !, Score >= 70.
grade(_, 'F'). :- Grade = 'F'.

```
student('Ali', 85).
student('Chris',92).
student('Kendall', 89).
```

Execution:
?- grades.
Current Grades
Chris: A
true.

```
grades :- writeln('Current Grades'),
    student(Student,Score),
    grade(Score,Grade),
    format(' ~w: ~w\n', [Student, Grade]),
    fail.
grades.
```

Why?
For Ali, grade(85,Grade) is called and grade(Score, 'A') :- !, Score >=90. is executed. The cut is done first thing, commiting this rule to producing the final answer for grade(85, Grade). It then fails on Score $>=90$.
grades then backtracks and continues with the next student, Chris.

## Cut, continued

Here's one way to write max: (Adapted from Clause and Effect by Clocksin) $\max (\mathrm{X}, \mathrm{Y}, \mathrm{X}):-\mathrm{X}>=\mathrm{Y}$. $\max (\mathrm{X}, \mathrm{Y}, \mathrm{Y}):-\mathrm{X}<\mathrm{Y}$.

Usage:
?- $\max (10,3, \operatorname{Max})$.
Max $=10$; (Prolog pauses because of possible alternative.)
false.

Can we shorten it with a cut?
$\max (\mathrm{X}, \mathrm{Y}, \mathrm{X}):-\mathrm{X}>=\mathrm{Y}$, !.
$\max \left(\_, Y, Y\right)$.

Usage:
?- $\max (10,3, \mathrm{Max})$.
$\operatorname{Max}=10 . \quad$ (Prolog prints period because no alternatives.)

## Cut, continued

Cuts can be used to limit backtracking in a query or a rule.

Queries and cuts:

```
?- f(F), write(F), g(G), write(G), fail.
    fl gl g2 g3 f2 gl g2 g3 f3 gl g2 g3
```

    ?- \(f(F)\), write( \(F\) ), !, \(g(G)\), write(G), fail.
    fl gl g2 g3
    ?- \(f(F)\), write(F), \(g(G)\), write(G), !, fail.
    fl gl
    Another analogy: A cut is like a door that locks behind you.
There is far more to know about "cut" but for now we'll use it for only one thing: "If you get to here, this rule will produce a final answer for this call to this predicate."

## The "singleton" warning(!)

# The "singleton" warning 

Here's a predicate add( $+\mathrm{X},+\mathrm{Y}$, ?Sum):
\$ cat add.pl $\operatorname{add}(\mathrm{X}, \mathrm{Y}$, Sum $):-\mathrm{S}$ is $\mathrm{X}+\mathrm{Y}$.

```
Usage:
    ?- add(3,4,X).
    true.
```

Bug: Sum is used in the head but S is used in the body!

Observe what happens when we load it:
\$ swipl -l add.pl
\% /Users/whm/.plrc compiled 0.00 sec, 4 clauses
Warning: /Users/whm/372/pl/add.pl:l:
Singleton variables: [Sum,S]
What is Prolog telling us with that warning?
The variables Sum and S appear only once in the rule on line 1.
Fact: If a variable appears only once in a rule, its value is never used.
A singleton warning may indicate a misspelled or misnamed variable.
Pay attention to singleton warnings!

## Singletons, continued

print_stars $(+\mathrm{N})$ prints N asterisks:
?- print_stars(10).
**********
true.

Here's a first version of it. Does it have any singletons?
print_stars(N) :- between(1,N,X), write('*'), fail. print_stars(N).

Let's see...
\$ swipl -l print_stars
Warning: print_stars.pl:1: ... Singleton variables: [X] Warning: print_stars.pl:2: ... Singleton variables: [N]

Should we worry about the warnings? How could we eliminate them?
print_stars(N) :- between(l,N,_), write('*'), fail.
print_stars(_).

## Singleton warnings are easy to overlook!

Note that singleton warnings appear before "Welcome to SWI-Prolog"!

```
$ swipl -l print_stars.pl (old version)
% /Users/whm/.plrc compiled 0.00 sec, 4 clauses
Warning:/Users/whm/372/pl/print_stars.pl:l:
Singleton variables: [X]
Warning: /Users/whm/372/pl/print_stars.pl:2:
    Singleton variables: [N]
% /Users/whm/372/pl/print_stars.pl compiled 0.00 sec, 3 clauses
Welcome to SWI-Prolog (Multi-threaded, }64\mathrm{ bits, Version 6.6.6)
Copyright (c) 1990-2013 University of Amsterdam, VU Amsterdam
SWI-Prolog comes with ABSOLUTELY NO WARRANTY. This is free
software, and you are welcome to redistribute it under certain
conditions.
Please visit http://www.swi-prolog.org for details.
For help, use ?- help(Topic). or ?- apropos(Word).
?-
```


## More with rules

Here is a set of facts for parents and children:

## Parents and children

| male(tom). |
| :--- |
| male(jim). |
| male(bob). |
| male(mike). |
| male(david). |
|  |
| female(jane). |
| female(betty). |
| female(mary). |
| female(alice). |


| parent(tom,betty). |
| :--- |
| parent(tom,bob). |
| parent(jane,betty). |
| parent(jane,bob). |
| parent(jim,mike). |
| parent(jim,david). |
| parent(betty,mike). |
| parent(betty,david). |
| parent(bob,alice). |
| parent(mary,alice). |

(parents.pl)


Parents and children, continued

Here is a set of facts for parents and children:
male(tom).
male(jim).
male(bob).
male(mike).
male(david).

female(jane).
female(betty).
female(mary).
female(alice).

```
parent(tom,betty).
parent(tom,bob).
parent(jane,betty).
parent(jane,bob).
parent(jim,mike).
parent(jim,david).
parent(betty,mike).
parent(betty,david).
parent(bob,alice).
parent(mary,alice).
```



Mike David

Define grandmother(GM,C).
grandmother(GM,C) :-
female(GM), parent(GM, P), parent(P, C).
?- grandmother(GM,C).
GM = jane,
C = mike;
GM = jane,
C = david;
GM = jane,
C = alice ;
false.

Or, we could have defined mother(M,C) and written grandmother using mother.

## Parents and children, continued

For who is Tom the father?
?- father(tom, C).
C = betty ;
$\mathrm{C}=\mathrm{bob}$.

What are all the father/daughter relationships?
?- father (F,D), female(D).
$\mathrm{F}=$ tom,
D = betty ;
F = bob,
D = alice ;
false.

Who is the father of Jim?
?- father ( $\mathrm{F}, \mathrm{jim}$ ).
false.


## Recursive predicates

Consider an abstract set of parent/child relationships:

```
parent(a,b). parent(c,d).
parent(a,c). parent(b,f).
parent(c,e). parent(f,g).
```



Here is a recursive predicate for the relationship that $\underline{\mathbb{A}}$ is an ancestor of $\underline{X}$. (swapped) ancestor(A,X) :- parent(A, X).
ancestor $(\mathrm{A}, \mathrm{X})$ :- $\operatorname{parent}(\mathrm{P}, \mathrm{X})$, ancestor $(\mathrm{A}, \mathrm{P})$. Exercise: reverse these!
In English:
" $A$ is an ancestor of $X$ if $A$ is the parent of $X$ or $P$ is the parent of $X$ and $A$ is an ancestor of P."

Usage:
?- ancestor(a,f). $\quad$ Is a an ancestor of $f$ ? true
?- ancestor(c,b). \% Is c an ancestor of b? false.

## Recursive predicates

At hand:
parent(a,b). parent(c,d).
ancestor(A,X) :- parent(A, X).
ancestor $(A, X)$ :- parent $(P, X)$, ancestor (A,P).
More examples:
?- ancestor(c,Descendant). \% Who are the descendants of c?
Descendant = e;
Descendant = ; false.

What's the following query asking?
?- ancestor (A, e), ancestor (A,g).
A = a;
false.

## Iteration with recursion

A recursive rule can be used to perform an iterative computation.
Here is a predicate that prints the integers from 1 through N :

```
printN(0).
printN(N):- N > 0, M is N - l, printN(M), writeln(N).
```

Usage:
?- printN(3).
1
2
3
true.
Note that we're asking if printN(3) can be proven. The side effect of Prolog proving it is that the numbers 1,2 , and 3 are printed.

Is printN(0). needed?
Which is better-the above or using between/3?

More recursion
A predicate to sum the integers from 0 to N : (ignoring Gauss...)
$\operatorname{sumN}(0,0)$. $\operatorname{sumN}(N, S u m)$ :$\mathrm{N}>0, \mathrm{M}$ is $\mathrm{N}-\mathrm{l}, \operatorname{sumN}(\mathrm{M}$, Temp $)$, Sum is Temp +N .

Usage:

$$
\begin{aligned}
& ?-\operatorname{sumN}(4, \mathrm{X}) . \\
& \mathrm{X}=10 .
\end{aligned}
$$

Note that this predicate can't be used to determine N for a given sum:
?- sumN(N, 10).
ERROR: $>/ 2$ : Arguments are not sufficiently instantiated
Could we write sumN using between?

## Sidebar: A common mistake with arithmetic

Here's the correct definition for sumN:

```
sumN(0,0).
sumN(N,Sum) :-
    N>0,M is N-1, sumN(M, Temp), Sum is Temp + N.
```

Here is a common mistake:

```
sumN(0,0).
sumN(N,Sum) :-
    N > 0, M is N - l, sumN(M, Sum), Sum is Sum + N.
```

Unless N is zero, Sum is Sum +N fails every time!
Remember that is/2 unifies its left operand with the result of arithmetically evaluating its right operand. Further remember that unification is neither assignment nor comparison.

## Recursion, continued

Here's the common example of recursion-factorial computation:

```
factorial(0,1).
factorial(N,F) :-
    N > 0,
    Nl is N-1,
    factorial(Nl,Fl),
    F is N * Fl.
```

The above example comes from
http://www.csupomona.edu/~jrfisher/www/prolog_tutorial/2_2.html
Near the bottom the page is an excellent animation of the computation factorial(3,X). Try it if you don't mind dealing with a Java applet.

## Sidebar: graphical tracing with gtrace

gtrace is the graphical counterpart of trace. Start it like this:
?- gtrace, sumN(4,Sum).
\% The graphical front-end will be used for subsequent tracing


Type space to through step goals one at a time. Click on call stack elements to show bindings in that call. The ancestor predicate makes a good demo, too.
gtrace should work immediately on Windows and Macs. On a Linux machine in the labs use "ssh -X ..." to login to lectura, and it should work there, too.

## Generating alternatives with recursion

Here is a predicate that tests whether a number is odd:

$$
\operatorname{odd}(\mathrm{N}):-\mathrm{N} \bmod 2=:=1 .
$$

Note that $\mathrm{N} \bmod 2$ works because $=:=$ evaluates its operands.
An alternative:

```
odd(l).
odd(N) :- odd(M), N is M + 2.
```

How does the behavior of the two differ?

## Generating alternatives, continued

For reference:
odd(1). $\operatorname{odd}(\mathrm{N}):-\operatorname{odd}(\mathrm{M}), \mathrm{N}$ is $\mathrm{M}+2$.

Usage:
?- odd(5). true.
?- odd(X).
$\mathrm{X}=1$;
$\mathrm{X}=3$;
$\mathrm{X}=5$;

What does odd(2) do?
How does odd(X) work?


## Generating alternatives, continued

For reference:
odd(l).
$\operatorname{odd}(\mathrm{N}):-\operatorname{odd}(\mathrm{M}), \mathrm{N}$ is $\mathrm{M}+2$.
The key point with generative predicates:
If an alternative is requested, another activation of the predicate is created.

As a contrast, think about how execution differs with this set of clauses:

```
odd(l).
odd(3).
odd(5).
odd(N) :- odd(M), N is M + 2.
```

Try gtrace with both the two-clause version at the top and the four-clause version just above.

## Lists

## List basics

A Prolog list can be literally specified by enclosing a comma-separated series of terms in square brackets:
[1,2,3]
[just, a, test, here]
[l, [one], l.0, [a,[b,['c this']]]]
Note that there's no evaluation of the terms:

$$
\begin{aligned}
& ?-\mathrm{L}=[1,2, \operatorname{odd}(3), 4+5, \operatorname{atom}(6)] . \\
& \mathrm{L}=[1,2, \operatorname{odd}(3), 4+5, \operatorname{atom}(6)] .
\end{aligned}
$$

A common mistake is entering a list literal as a query. That's taken as a request to consult files!
?- [abc, l23].
ERROR: source_sink `abc' does not exist ...

## Unification with lists

Here are some unifications with lists:

```
?- \([1,2,3]=[\mathrm{X}, \mathrm{Y}, \mathrm{Z}]\).
\(\mathrm{X}=1\),
\(\mathrm{Y}=2\),
\(\mathrm{Z}=3\).
?- \([\mathrm{X}, \mathrm{Y}]=[1,[2,[3,4]]] . \quad\) Note unification of \(Y\) with list of lists.
\(\mathrm{X}=1\),
\(\mathrm{Y}=[2,[3,4]]\).
?- \([\mathrm{X}, \mathrm{Y}]=[1]\).
false.
```

?- $\mathrm{Z}=[\mathrm{X}, \mathrm{Y}, \mathrm{X}], \mathrm{X}=1, \mathrm{Y}=[2,3] . \quad$ Note that X occurs twice in Z .
$\mathrm{Z}=[1,[2,3], 1]$,
$\mathrm{X}=1$,
$\mathrm{Y}=[2,3]$.

We'll later see a head-and-tail syntax for lists.

## Unification with lists, continued

Write a predicate empty $(\mathrm{L})$ that succeeds $\operatorname{iff} \mathrm{L}$ is an empty list. Be sure it succeeds only on lists and no other types! empty([]).

Write a predicate $\operatorname{asl} \operatorname{l23}(\mathrm{X})$ that succeeds iff X is a list with one, two, or three identical elements.

$$
\begin{aligned}
& \text { asl23([_]). } \\
& \text { asl23([X,X]). } \\
& \text { asl23([X,X,X]). }
\end{aligned}
$$

```
Not "getting it" with unification:
    asl23([X]).
    asl23([X,Y]) :- X = Y.
    asl23([X,Y,Z]):- X = Y,Y = Z.
```

Usage:
?- asl23([a]), asl23([b,b]), write(ok), asl23([l,2,3]), write('oops').
ok
false.
?- asl23(L).
L = [_G2456] ;
L = [_G2456, _G2456] ;
$\mathrm{L}=$ [_G2456, _G2456, _G2456].

## Built-in list-related predicates

SWI Prolog has a number of built-in predicates that operate on lists. One is nth0: nth0(?Index, ?List, ?Elem)

True when Elem is the Index'th element of List. Counting starts at 0.
Usage:
?- nth0 (2, [a,b,a,d,c], X). What is the third element of $[a, b, a, d, c]$ ?
$\mathrm{X}=\mathrm{a}$.
?- nth0 ( $0,[\mathrm{a}, \mathrm{b}, \mathrm{a}, \mathrm{d}, \mathrm{c}], \mathrm{b}) . \quad$ Is b the first element of $[\mathrm{a}, \mathrm{b}, \mathrm{a}, \mathrm{d}, \mathrm{c}]$ ? false.
?- nth0(N, [a,b,a,d,c], a). Where are a's in $[a, b, a, d, c]$ ?
$\mathrm{N}=0$;
$\mathrm{N}=2$;
false.
?- nth0 (N, [a,b,a,d,c], X). What are the positions and values for all?
$\mathrm{N}=0$,
$\mathrm{X}=\mathrm{a}$;
$\mathrm{N}=\mathrm{l}$,
$\mathrm{X}=\mathrm{b}$;

NOTE: nth0 makes for a good example here, but use indexing judiciously! There are usually better alternatives!

Recall:

## Built-ins for lists, continued

asl23([_]).
asl23([X,X]).
asl23([X,X,X]).
Problem: Using as 123 and nth0, write a predicate with this behavior:

```
?- f3(test, L).
L = [test];
L = [test, test];
L = [test, test, test].
```

Solution:
f3(X,L) :- asl23(L), nth0(0, L, X).
Does the order of the goals matter?
More:
?- f3(test, [test]). true.
?- f3(test, [a,b]).
false.

## Built-ins for lists, continued

What do you think length(?List, ?Len) does?
Get the length of a list:
?- length([10,20,30],Len).
Len $=3$
And?
Make a list of uninstantiated variables:

```
        ?- length(L,3).
        L = [_G907,_G910,_G913].
```

Speculate-what will length( $\mathrm{L}, \mathrm{N}$ ) do?
?- length(L,N).
$\mathrm{L}=[$,
$\mathrm{N}=0$;
L = [_G919],
$\mathrm{N}=1$;
L = [_G919, _G922],
N = 2 ...

What does reverse(?List, ?Reversed) do?
Unifies a list with a reversed copy of itself.
?- reverse([1,2,3],R).
$R=[3,2,1]$.
?- reverse([1,2,3],[1,2,3]).
false.
Write palindrome(L).
palindrome(L) :- reverse(L,L).
Speculate-what's the result of reverse $(\mathrm{X}, \mathrm{Y})$.?
?- reverse( $\mathrm{X}, \mathrm{Y}$ ).
$\mathrm{X}=\mathrm{Y}, \mathrm{Y}=[]$;
$\mathrm{X}=\mathrm{Y}, \mathrm{Y}=$ [_G913];
X = [_G913, _G916],
Y = [_G916,_G913];
X = [_G913, _G922, _G916],
Y = [_G916,_G922,_G913];

## Built-ins for lists, continued

How about numlist(+Low, +High, -List)?
?- numlist( $5,10, \mathrm{~L})$.
$\mathrm{L}=[5,6,7,8,9,10]$.
How can we make $[7,6, \ldots, 1]$ ?
?- numlist( $1,7, \mathrm{~L})$, reverse( $\mathrm{L}, \mathrm{R}$ ).
$\mathrm{L}=[1,2,3,4,5,6,7]$,
$R=[7,6,5,4,3,2,1]$.
sumlist(+List, -Sum) unifies Sum with the sum of the values in List, which must all be numbers or structures that can be evaluated with is/ 2 .

```
?- numlist(l,5,L), sumlist(L,Sum).
L = [l, 2, 3, 4, 5],
Sum = 15.
?- sumlist([1+2, 3*4, 5-6/7],X).
X = 19.142857142857142.
```

Sidebar: Developing a list-based predicate goal-by-goal Write a predicate sumGreater(+Target, $-\mathrm{N},-$ Sum) that finds the smallest N for which the sum of 1.. N is greater than Target.

```
?- sumGreater(50, N, Sum).
\(\mathrm{N}=10\),
Sum \(=55\).
?- sumGreater(1000000, N, Sum).
\(\mathrm{N}=1414\),
Sum \(=1000405\).
```

Let's ignore Gauss and have some fun with lists!

## Sidebar, continued

Step one: Have a goal that instantiates N to $1,2, \ldots$
?- between(l, inf, N). What's inf?
$\mathrm{N}=1$;
$\mathrm{N}=2$;
$\mathrm{N}=3$;

Step two: instantiate L to lists [1], [1,2], ...
?- between(l, inf, N ), numlist( $\mathrm{l}, \mathrm{N}, \mathrm{L}$ ).
$\mathrm{N}=1$,
$\mathrm{L}=[1]$;
$\mathrm{N}=2$,
$\mathrm{L}=[1,2]$;
$\mathrm{N}=3$,
$\mathrm{L}=[1,2,3]$;

## Sidebar, continued

Step three: Compute sum of 1..N.
?- between(l, inf, N), numlist(l,N,L), sumlist(L,Sum).
$\mathrm{N}=$ Sum, Sum = l,
$\mathrm{L}=[1]$;
$\mathrm{N}=2$,
$\mathrm{L}=[1,2]$,
Sum $=3$;

Step four: Test sum against target value.
?- between(l, inf, N), numlist(l,N,L), sumlist(L,Sum), Sum > 20.
$\mathrm{N}=6$,
$\mathrm{L}=[1,2,3,4,5,6]$,
Sum $=21$.
Note the incremental process followed, adding goals one-by-one and being sure the results for each step are what we expect.

## Sidebar, continued

Step four, for reference:
?- between(l, inf, N), numlist(l,N,L), sumlist(L,Sum), Sum > 20.
$\mathrm{N}=6$,
$\mathrm{L}=[1,2,3,4,5,6]$,
Sum $=21$.
Step five: Package as a predicate.
\$ cat sg.pl
sumGreater(Target,N,Sum) :between(l,inf,N), numlist(1,N,L), sumlist(L,Sum), Sum > Target.
\% pl -l sg
?- sumGreater(1000,N,Sum).
$\mathrm{N}=45$,
Sum = 1035 ;
$N=46$,
Sum = 1081 ;
Is it good or bad that it produces alternatives?

Built-ins for lists, continued
Here's atom_chars(?Atom, ?Charlist):
?- atom_chars(abc,L).
$\mathrm{L}=[\mathrm{a}, \mathrm{b}, \mathrm{c}]$.
?- atom_chars(A, [a, b, c]).
$\mathrm{A}=\mathrm{abc}$.
Problem: write rev_atom/2.
?- rev_atom(testing,R).
R = gnitset.
?- rev_atom(testing,gnitset).

Problem: write eqlen( $+\mathbb{A} 1,+\mathbb{A} 2)$, to test whether two atoms are the same length.
?- eqlen(test,this).
true.
?- eqlen(test,it).
false.
rev_atom(A,RA) :- Note: a rule shown in the middle of queries! atom_chars(A,AL), reverse(AL,RL), atom_chars(RA,RL).
?- rev_atom(X, gnitset).
ERROR: atom_chars/2: Arguments are not sufficiently instantiated
How should rev_atom's arguments be described with + , ?, and - ?

## Built-ins for lists, continued

msort(+List, -Sorted) unifies Sorted with a sorted copy of List:
?- msort([3, l,7], L).
$\mathrm{L}=[1,3,7]$.
?- atom_chars(prolog, L), msort(L,S), atom_chars(A,S).
$\mathrm{L}=[\mathrm{p}, \mathrm{r}, \mathrm{o}, \mathrm{l}, \mathrm{o}, \mathrm{g}]$,
$\mathrm{S}=[\mathrm{g}, \mathrm{l}, \mathrm{o}, \mathrm{o}, \mathrm{p}, \mathrm{r}]$,
A = gloopr.
If the list is heterogeneous, elements are sorted in "standard order":
?- msort([xyz, 5, [1,2], abc, 1, 5, x(a)], Sorted).
Sorted $=[1,5,5, a b c, x y z, x(a),[1,2]]$.
sort/2 is like msort/2 but also removes duplicates.
?- $\operatorname{sort}([x y z, 5,[1,2], a b c, 1,5, x(a)]$, Sorted).
Sorted $=[1,5, a b c, x y z, x(a),[1,2]]$.

## The member predicate

member(?Elem, ?List) succeeds when Elem can be unified with a member of List.
member can be used to check for membership:
?- member(30, [10, twenty, 30]).
true.
member can be used to generate the members of a list:
?- member(X, [10, twenty, 30]).
$\mathrm{X}=10$;
$\mathrm{X}=$ twenty ;
$\mathrm{X}=30$.

Problem: Print the numbers from 100 through 1.
?- numlist( $1,100, L$ ), reverse(L,R), member( $\mathrm{E}, \mathrm{R}$ ), writeln( E ), fail. 100
99

Problem: Write a predicate has_vowel(+Atom) that succeeds iff Atom has a lowercase vowel.
?- has_vowel(ack). true
?- has_vowel(pfft).
false.

Solution:
has_vowel(Atom) :-
atom_chars(Atom,Chars), member(Char,Chars), member(Char,[a,e,i,o,u]).

Explain it!

## The append predicate

Here's how the documentation describes append/3:
?- help(append/3).
append(?Listl, ?List2, ?Listl AndList2)
ListlAndList2 is the concatenation of Listl and List2

Usage:
?- append([1,2], [3,4,5], R).
$R=[1,2,3,4,5]$.
?- numlist(1,4,Ll), reverse(Ll, L2), append(Ll ,L2,R).
$\mathrm{Ll}=[1,2,3,4]$,
$\mathrm{L} 2=[4,3,2,1]$,
$R=[1,2,3,4,4,3,2,1]$.
What else can we do with append?

## append, continued

What will the following do?
?- append(A, B, [1,2,3]).
A = [],
$B=[1,2,3]$;
A $=$ [l],
$\mathrm{B}=[2,3]$;
$A=[1,2]$,
B = [3] ;
$A=[1,2,3]$,
$\mathrm{B}=[]$;
false.
The query can be thought of as asking, "For what values of $A$ and $B$ is their concatenation [ $1,2,3]$ ?

Think of append as demanding a relationship between the three lists: List3 must consist of the elements of Listl followed by the elements of List2. If Listl and List2 are instantiated, List3 must be their concatenation. If only List3 is instantiated then Listl and List2 represent (in turn) all the possible ways to divide List3.

## append, continued

Let's write some more predicates using append.
starts_with(L, Prefix) :append(Prefix, _, L).

Usage:
?- starts_with([1,2,3,4], [1,2]).
true.
?- starts_with([1,2,3,4], L).
$\mathrm{L}=[]$;
$\mathrm{L}=[1]$;
$\mathrm{L}=[1,2]$;
$\mathrm{L}=[1,2,3]$;
$\mathrm{L}=[1,2,3,4]$;
false.

## append, continued

Haskell meets Prolog:
take(L, N, Result) :length(Result,N), append(Result, _, L).
?- take([1,2,3,4,5], 3, L).
$\mathrm{L}=[1,2,3]$.
?- take([1,2,3,4,5], N, L).
$\mathrm{N}=0$,
$\mathrm{L}=[]$;
$\mathrm{N}=1$,
$\mathrm{L}=$ [1];
$\mathrm{N}=2$,
$\mathrm{L}=[1,2]$;
drop(L, N, Result) :-
append(Dropped, Result, L), length(Dropped, N).

## append, continued

Here is a predicate that generates successive N -long chunks of a list:
chunk(L,N,Chunk) :-
length(Chunk,N), append(Chunk,_,L).
chunk(L,N,Chunk) :-
length(Junk, N), append(Junk,Rest,L), chunk(Rest,N,Chunk).
Usage:
?- chunk([1,2,3,4,5],2,L).
$\mathrm{L}=[1,2]$;
$\mathrm{L}=[3,4]$;
false.
?- numlist(1,100,L), chunk(L,5,C), sumlist(C,Sum), between(300,350,Sum).
$\mathrm{L}=[1,2,3,4,5,6,7,8,9 \mid \ldots]$,
$C=[61,62,63,64,65]$,
Sum = 315;
$\mathrm{L}=[1,2,3,4,5,6,7,8,9 \mid \ldots]$,
C = [66, 67, 68, 69, 70],
Sum = 340 ;
false.

## The findall predicate

findall can be used to create a list of values that satisfy a goal. A simple example:
?- findall( $F$, food( $F$ ), Foods).
Foods = [apple, broccoli, carrot, lettuce, orange, rice].
SWI's documentation:
findall(+Template, :Goal, -Bag)
Create a list of the instantiations Template gets successively on backtracking over Goal and unify the result with Bag. Succeeds with an empty list if Goal has no solutions.

Template is not limited to being a single variable. It might be a structure.
The second argument can be a single goal, or several goals joined with conjunction.

The third argument is instantiated to a list of terms whose structure is determined by the template. Above, each term is just an atom.

## findall, continued

For reference:
findall(+Template, :Goal, -Bag) (The colon in :Goal means"meta-argument")
?- findall(F, food(F), Foods).
Foods = [apple, broccoli, carrot, lettuce, orange, rice].
Examples to show the relationship of the template and the resulting list:
?- findall(x, food(F), Foods).
Foods $=[\mathrm{x}, \mathrm{x}, \mathrm{x}, \mathrm{x}, \mathrm{x}, \mathrm{x}]$.
?- findall( $x(F)$, food( $F$ ), Foods).
Foods $=[\mathrm{x}($ apple $), \mathrm{x}($ broccoli), $\mathrm{x}($ carrot $), \mathrm{x}($ lettuce $), \mathrm{x}$ (orange), x (rice)].
?- findall(l-F, food(F), Foods).
Foods = [l-apple, l-broccoli, l-carrot, l-lettuce, l-orange, l-rice].
What does findall remind you of?

## Important:

findall is said to be a higher-order predicate. It's a predicate that takes a predicate, $f$ ood $(F)$ in this case.

## findall, continued

Here's a case where the :Goal is a conjunction of two goals.
?- findall(F-C, (food(F), color(F,C)), FoodsAndColors).
FoodsAndColors = [apple-red, broccoli-green, carrot-orange, lettuce-green, orange-orange, rice-white].
display sheds some light on that conjunction:
?- display((food(F), color(F,C))).
,(food(_G835),color(_G835,_G838))
true.

It's a two-term structure whose functor is ',' (just a comma).

## findall, continued

For reference:

```
findall(+Template, :Goal, -Bag)
```

Describe the following computation.

```
?- numlist(l,9,L),
    findall(
    sum(Pfx,Sum),
    (append(Pfx,_,L), sumlist(Pfx,Sum),Sum<l0),
    Sums).
L = [l, 2, 3, 4, 5, 6, 7, 8, 9],
Sums = [sum([],0), sum([l], l), sum([l, 2], 3), sum([1, 2, 3], 6)].
```

Find all prefixes of the list $[1,2,3,4,5,6,7,8,9]$ whose sum is less than 10. Instantiate Sums to a list of sum structures whose terms are the list and the sum of its elements.

## (no longer intentionally blank)

See https://piazza.com/class/i43g61msngm4uz?cid=213, "Three more append examples" for some more practice with append

## (no longer intentionally blank)

Here are more findall examples....
?- findall(pos(N,X), nth0(N, [a,b,a,d,c], X), Posns).
Posns $=[\operatorname{pos}(0, a), \operatorname{pos}(1, b), \operatorname{pos}(2, a), \operatorname{pos}(3, d), \operatorname{pos}(4, c)]$.
?- findall(X, (between(1,100,X), X rem $13=:=0$ ), Nums).
Nums $=[13,26,39,52,65,78,91]$.
Note the following have compound goals (underlined).
?- X=[t,e,s,t,i,n,g],V=[a,e,i,o,u], findall(C, (member(C,X), member(C,V)), Common).
$\mathrm{X}=[\mathrm{t}, \mathrm{e}, \mathrm{s}, \mathrm{t}, \mathrm{i}, \mathrm{n}, \mathrm{g}]$,
$\mathrm{V}=[\mathrm{a}, \mathrm{e}, \mathrm{i}, \mathrm{o}, \mathrm{u}]$,
Common $=[e, i]$.
?- findall(Len-F, (food(F), atom length(F,Len)), LFs).
LFs = [5-apple, 8-broccoli, 6-carrot, 7-lettuce, 4-rice, l 1-'bell pepper', 7-'Whopper'].
?- findall(Len-F, (food(F), atom_length(F,Len)), LFs), keysort(LFs,Sorted). LFs = [5-apple, 8-broccoli, 6-carrot, 7-lettuce, 4-rice, ll-'bell pepper', 7-'Whopper'],
Sorted = [4-rice, 5-apple, 6-carrot, 7-lettuce, 7-'Whopper', 8-broccoli, ll-'bell pepper'].

## (intentionally blank)

## Next set of slides

## Low-level list processing

## Heads and tails

The list $[1,2,3]$ can be specified in terms of a head and a tail, like this:
[1 | [2,3]]
More generally, a list can be specified as a sequence of initial elements and a tail.

The list $[1,2,3,4]$ can be specified in any of these ways:
Haskell equivalents:
[1| [2,3,4]]
$[1,2 \mid[3,4]]$
[1,2,3| [4]]
[1,2,3,4 | []]
l:[2,3,4]
$1: 2:[3,4]$
1:2:3:[4]
1:2:3:4:[]

## Unifications with lists

Consider this unification:

$$
\begin{aligned}
& \stackrel{?-}{-}[\mathrm{H} \mid \mathrm{T}]=[1,2,3,4] . \\
& \mathrm{H}=1, \\
& \mathrm{~T}=[2,3,4] .
\end{aligned}
$$

What instantiations are produced by these unifications?

$$
\begin{aligned}
& ?-[\mathrm{X}, \mathrm{Y} \mid \mathrm{T}]=[1,2,3] . \\
& \mathrm{X}=1, \\
& \mathrm{Y}=2, \\
& \mathrm{~T}=[3] . \\
& ?-[\mathrm{X}, \mathrm{Y} \mid \mathrm{T}]=[1,2] . \\
& \mathrm{X}=1, \\
& \mathrm{Y}=2, \\
& \mathrm{~T}=[] . \\
& ?-\quad[1,2 \mid[3,4]]=[\mathrm{H} \mid \mathrm{T}] . \\
& \mathrm{H}=1, \\
& \mathrm{~T}=[2,3,4] . \\
& ?-\mathrm{A}=[1], \mathrm{B}=[\mathrm{A} \mid \mathrm{A}] . \\
& \mathrm{A}=[1], \\
& \mathrm{B}=[[1], 1] .
\end{aligned}
$$

## Simple list predicates

Here is a rule that describes the relationship between a list and and its head:
head $(\mathrm{L}, \mathrm{H}):-\mathrm{L}=[\mathrm{H} \mid-]$.
The head of $L$ is $H$ if $L$ unifies with a list whose head is $H$.
Usage:
?- head([1,2,3],H).
$\mathrm{H}=1$.
?- head([2],H).
$\mathrm{H}=2$.
?- head([],H).
false.
?- L = [X,X, b, c], head( $\mathrm{L}, \mathrm{a}$ ).
$\mathrm{L}=[\mathrm{a}, \mathrm{a}, \mathrm{b}, \mathrm{c}]$,
$\mathrm{X}=\mathrm{a}$.
Can we make better use of unification and define head/2 more concisely?
head ([H|_], H).
The head of a list whose head is $H$ is $H$.

## Implementing member

Here is one way to define the built-in member/2 predicate:

```
member(X,L) :- L = [X|_].
member(X,L):- L = [_|T], member(X,T).
```

Usage:
?- member ( $1,[2,1,4,5]$ ).
true ;
false.
?- member (a, [2, $1,4,5]$ ).
false.

## member, continued

For reference:
member (X,L) :- L = [X|_].
member (X,L) :- L = [_|T], member $(\mathrm{X}, \mathrm{T})$.
Problem: Define member more concisely.
member(X,[X|_]).
$X$ is a member of the list having $X$ as its head
member(X,[_|T]) :- member(X,T).
$X$ is a member of the list having $T$ as its tail if $X$ is a member of $T$
Exercise: Following the example of slide 133, trace through how member generates elements from a list, like this:
?- member (X, [a,b,c]).
$\mathrm{X}=\mathrm{a}$;
$\mathrm{X}=\mathrm{b}$;

## Implementing last

Problem: Define a predicate last $(\mathrm{L}, \mathrm{X})$ that describes the relationship between a list L and its last element, X .
?- last([a,b,c],X).
$\mathrm{X}=\mathrm{c}$.
?- last([],X).
false.
?- last(L,last), head(L,first), length(L,2).
$\mathrm{L}=$ [first, last $]$.
last is a built-in predicate but here's how we'd write it.
last([X],X).
$\operatorname{last}([\mid T], X):-\operatorname{last}(T, X)$.

## Exercises

Write last in terms of head/l and reverse/2.
Write htsame(?L), which succeeds iff its first and last element are the same.

Create a list that unifies with a three-element list whose first and last elements are the same.

## Implementing length

Problem: Write a predicate len/2 that behaves like the built-in length/2

```
?- len([],N).
N = 0.
?- len([a,b,c,d],N).
N = 4.
?- len(L,1).
L = [_G901].
?- len(L,N).
L = [],
N = 0;
L = [_G913],
N = 1;
L = [_G913, _G916],
N = 2;
```

Problem: Define a predicate allsame(L) that describes lists in which all elements have the same value.
?- allsame([a,a,a]).
true
?- allsame([a,b,a]).
false.
?- $L=[A, B, C]$, allsame $(L), B=7$, write $(L)$.
[7,7,7]
$\mathrm{L}=[7,7,7]$,
$A=B, B=C, C=7$.
?- length( $\mathrm{L}, 5$ ), allsame( L ), head( $\mathrm{L}, \mathrm{x}$ ).
$\mathrm{L}=[\mathrm{x}, \mathrm{x}, \mathrm{x}, \mathrm{x}, \mathrm{x}]$.
Solution:
allsame([_]).
allsame([X,X|T]) :- allsame([X|T]).

Recall the description of the built-in append predicate:
?- help(append/3).
append(?List1, ?List2, ?List1AndList2)
List1AndList2 is the concatenation of List1 and List2
The usual definition of append:
append([], X, X).
append([X|Ll], L2, [X|L3]) :- append(Ll, L2, L3).
How does it work?
Try tracing it. To avoid getting the built-in version, define the above as myapp instead of append. Then try these:
?- gtrace, myapp $([1,2,3,4],[a, b, c, d], X)$.
?- gtrace, myapp([a,b,c,d,e,f,g],[],X).

Actually, execution is maybe easier to understand with trace than gtrace!

Note that all of the Exit: lines in a trace show an append relationship that's true:
Exit: (l l) myapp([], [a, b, c, d], [a, b, c, d]) ?
Exit: (10) myapp([4], [a, b, c, d], [4, a, b, c, d]) ?
Exit: (9) myapp ([3, 4], [a, b, c, d], [3, 4, a, b, c, d]) ?

## Lists are structures

In fact, lists are structures:
?- display([1,2,3]).
.(l,.(2,.(3,[])))
Essentially, ./2 is the "cons" operation in Prolog.
By default, lists are shown using the [...] notation:
?- $\mathrm{X}=.(\mathrm{a}, .(\mathrm{b},[]))$.
$\mathrm{X}=[\mathrm{a}, \mathrm{b}]$.
We can write member/2 like this:

```
member(X,.(X,_)).
member(X, .(_,T)) :- member(X,T).
```

What does the following produce?
?- X='.'(3,4).
$\mathrm{X}=[3 \mid 4] . \quad$ A Lisp programmer would call this a "dotted-pair".

## "Can't prove"

The query $\backslash+$ goal succeeds if goal fails.
?- food(computer).
false.
?- $\backslash+$ food(computer). true.

An incomplete set of facts can produce oddities.
?- \+food(cake).
true.
\+ is often spoken as "can't prove" or "fail if".

## "can't prove", continued

Example: What foods are not green?

```
?- food(F), \+color(F,green).
F = apple;
F = carrot;
F = orange ;
F = rice;
F = 'Big Mac'.
```

If there's no color fact for a food, will the query above list that food?

How can we see if there are any foods don't have a color fact?
?- food(F), \+color(F,_).
F = 'Big Mac'.

## "can't prove", continued

Describe the behavior of inedible/l: inedible(X) :- \+food(X).
inedible $(\mathrm{X})$ succeeds if something is not known to be a food.
?- inedible(rock). true.

What will the query ?- inedible(X). do?
?- inedible(X).
false.

## "can't prove", continued

What's the following query asking?
?- color(X,_), \+food(X).
X = sky ;
$\mathrm{X}=\operatorname{dirt}$;
$\mathrm{X}=$ grass ;
false.
What are things with known colors that aren't food?
Let's try reversing the goals:
?- \+food(X), color(X,_).
false.
Why do the results differ?

Important: variables are never instantiated by a "can't prove" goal.
Example:
?- $\backslash+$ food (X).
false.
Consider this attempt to ask for things that aren't purple.
?- \+color(Thing, purple). true.

There are many such things but Thing is not instantiated.

## "cut-fail"

## The "cut-fail" idiom

Predicates naturally fail when a desired condition is absent but sometimes we want a predicate to fail when a particular condition is present.

Here is a recursive predicate that succeeds iff all numbers in a list are positive:

$$
\begin{aligned}
& \text { allpos([X]) :- X > 0. } \\
& \text { allpos([X|T]) :- X }>0 \text {, allpos(T). }
\end{aligned}
$$

Another way to write it is with a "cut-fail":

```
allpos(L) :- member(X, L), X =< 0, !, fail.
allpos(_).
```

Remember that a cut effectively eliminates all subsequent clauses for the active predicate. If a non-positive value is found, the cut eliminates allpos(_). and then the rule fails.

Another way to think about cut-fail: "My final answer is No!"
average_taxpayer(X) :foreigner(X), !, fail.

A person is not an average taxpayer if they are a foreigner.
average_taxpayer(X) :spouse(X,Spouse), gross_income(Spouse, SpouseIncome), SpouseIncome > 3000, !, fail.

A person is not an average taxpayer if they've got a spouse and the spouse makes over 3000 .
average_taxpayer(X) :gross income(X, Inc),
Inc > 2000, Inc $=<20 \_000$.

A person is an average taxpayer if their income is between 2000 and 20,000.
gross_income(X,GrossIncome) :receives_pension(X, GrossIncome), GrossIncome < 5000, !, fail.
gross_income(X, GrossIncome) :-
gross_salary(X, GrossSalary),
investment_income(X,InvestmentIncome),
GrossIncome is GrossSalary + InvestmentIncome.
investment_income(X, InvestmentIncome) :- ...
Straight from Clocksin and Mellish, p. 91

A person is not considered to have a gross income if they receive a pension of less than 5000 .

A cut says, "If you get this far, you've picked the right rule for this goal." - C\&M

Here's how we could implement $\backslash+$ (can't prove) using the higher-order predicate call/l and a cut-fail:

```
cant_prove(G) :- call(G), !, fail.
cant_prove(_).
```

Usage:
?- cant_prove(food(apple)). false.
?- cant_prove(food(computer)). true.
?- cant_prove(color(_,purple)). true.

Is cant_prove a higher-order predicate?

# Database (knowledgebase) manipulation 

## assert and retract

A Prolog program is a database of facts and rules.
The database can be changed dynamically by adding facts with assert/l and deleting facts with retract/l.

A predicate to establish that certain things are foods: makefoods :assert(food(apple)), assert(food(broccoli)), assert(food(carrot)), assert(food(lettuce)), assert(food(rice)).

Evaluating makefoods adds facts to the database:
?- food(F). ("positive-control" test-be sure no foods already!)
ERROR: toplevel: Undefined procedure: food/l
?- makefoods.
true.
?- findall(F,food(F),L).
L = [apple, broccoli, carrot, lettuce, rice].

A fact can be "removed" with retract:
?- retract(food(carrot)).
true.
?- food(carrot).
false.
retractall removes all matching facts.
?- retractall(food(_)).
true.
?- food(X).
false.

If we query makefoods multiple times, it makes multiple sets of food facts.
?- makefoods.
true.
?- makefoods.
true.
?- findall(F,food(F),Foods).
Foods = [apple, broccoli, carrot, lettuce, rice, apple, broccoli, carrot, lettuce |...].

Let's start makefoods with a retractall to get a clean slate every time.
makefoods :-
retractall(food(_)), assert(food(apple)),
assert(food(broccoli)), assert(food(carrot)),
assert(food(lettuce)), assert(food(rice)).

Important: asserts and retracts are not undone with backtracking.

```
?- assert(f(1)), assert(f(2)), fail.
```

false.
?- f(X).
$\mathrm{X}=1$;
$X=2$.
?- retract(f(1)), fail.
false.
?- $\mathrm{f}(\mathrm{X})$. A redo of retract( $f(\mathrm{l})$ ) did not restore $\mathrm{f}(\mathrm{l})$.
$X=2$.

There is no ability to directly change a fact. Instead, a fact is changed by retracting it and then asserting it with different terms.

A rule to remove foods of a given color (assuming the color/2 facts are present):
rmfood(C) :- food(F), color(F,C),
retract(food(F)), write('Removed '), write(F), nl, fail.

Usage:
?- rmfood(green).
Removed broccoli
Removed lettuce false.
?- findall(F, food(F), L).
$\mathrm{L}=$ [apple, carrot, rice].
The color facts are not affected-color(broccoli, green) and color(lettuce, green) still exist.

## A simple calculator

Here's a very simple calculator:

```
?- calc.
> print.
0
> add(20).
> sub(7).
> print.
13
> set(40).
> print.
40
> exit.
true.
```

Note that the commands themselves are Prolog terms.
Code is in www/pl/calc.pl

## Simple calculator, continued

A loop that reads and prints terms:

```
calc0 :- prompt(_, '> '),
repeat, read(T), format('Read ~w~n',T),T = exit, !.
```

Interaction:
?- calc0.
$>$ a.
Read a
$>a b(c, d, e)$.
Read ab(c,d,e)
$>$ exit.
Read exit
true.
How does the loop work?
prompt/ 2 sets the prompt that's printed when read/l is called.
repeat/0 always succeeds. If repeat is backtracked into, it simply sends control back to the right. (Think of its redo port being wired to its exit port.)

The predicate read $(-X)$ reads a Prolog term and unifies it with X .

## Simple calculator, continued

Partial implementation:

```
init :-
    retractall(value(_)),
    assert(value(0)).
do(set(V)) :-
    retract(value(_)),
    assert(value(V)).
do(print) :- value(V), writeln(V).
do(exit).
calc:-
    init, prompt(_,'> '),
```

?- calc.
$>$ print.
0
$>$ add(20).
$>$ sub(7).
$>$ print.
13
$>\operatorname{set}(40)$.
$>$ print.
40
$>$ exit.
true.

How can $\operatorname{add}(\mathbb{N})$ and $\operatorname{sub}(\mathbb{N})$ be implemented? (No repetitious code, please!)
add and subtract:

## Simple calculator, continued

```
do(add(X)) :-
    value(V0),
    V is VO + X,
    do(\operatorname{set}(\textrm{V})).\quadIs this a nested call to set(V)?!
do(sub(X0)) :-
    X is -X0,
    do(add(X)).
```

Tangent: Could sub be shortened to the following? do(sub(X)) :- do(add(-X)).

Try add $(3+4 * 5)$, too.

Exercise: Add double and halve commands.

## Word tally

We can use facts like we might use a Java map or a Ruby hash.
Imagine a word tallying program in Prolog:

```
?- tally.
|: to be or
|: not to be ought not
|: to be the question
| : (Empty line ends the input.)
-- Results --
be 3
not 2
or 1
ought 1
question 1
the 1
to 3
true.
```


## Input handling for tally

read_line_to_codes produces a list of ASCII character codes for a line of input.
?- read_line_to_codes(user_input, Codes).
|: ab CD 12
Codes $=[97,98,32,67,68,32,49,50]$.
?- read_line_to_codes(user_input, Codes).
|: (hit ENTER)
Codes $=[]$.
atom_codes can be used to form an atom from a list of codes.
?- atom_codes(Atom, [97, 98, 10, 49, 50]).
Atom $=$ 'ab\nl2'.
readline reads a line and produces an atom.
readline(Line) :-
read_line_to_codes(user_input, Codes), atom_codes(Line, Codes).
?- readline(Line).
|: a test of this
Line = 'a test of this'.

Counting words
Let's use word(Word, Count) facts to maintain counts. Let's write a count(Word) predicate to create and update word/2 facts.

Example of operation:
?- retractall(word(_,_)). true.
?- count(test). true.
?- word(W,C).
$\mathrm{W}=$ test,
$\mathrm{C}=1$.
?- count(this), count(test), count(now). true.
?- findall(W-C, word(W,C), L).
$\mathrm{L}=[$ this -1, test-2, now-1].

## count implementation

For reference:
?- retractall(word(_,_)).
?- count(test), count(this), count(test), count(now).
?- findall(W-C, word(W,C), L).
$\mathrm{L}=[$ this-1, test-2, now-1].
Problem: implement count

```
count(Word) :-
    word(Word,Count0),
    retract(word(Word,_)),
    Count is Count0+l,
    assert(word(Word,Count)),!.
```

count(Word) :- assert(word(Word, l)).

## Top-level and a helper

tally clears the counts then loops, reading lines and processing each.
tally :-
retractall(word(_,_)),
repeat,
readline(Line),
do_line(Line),
Line == ", !, note that " is an empty atom
show_counts.
How does tally terminate?
do_line breaks up a line into words and calls count on each word. do_line(").
do_line(Line) :-
atomic_list_concat(Words, ' ', Line), \% splits Line on blanks
member(Word, Words),
count(Word), fail.
do_line(_).

## Showing the counts

keysort/2 sorts a list of $A-B$ structures on the value of the $A$ terms.
?- keysort([zoo-3, apple-l, noon-4],L).
$\mathrm{L}=$ [apple-1, noon-4, zoo-3].
With keysort in hand we're ready to write show_counts.
show_counts :-
writeln('\n-- Results --'), findall(W-C, word(W,C), Pairs), keysort(Pairs, Sorted), member(W-C, Sorted), format( $\left.{ }^{\sim} \sim \mathrm{w} \sim \mathrm{t} \sim 12 \mid \sim \mathrm{w} \sim \mathrm{n} ',[\mathrm{~W}, \mathrm{C}]\right)$, fail. show_counts.

Full source is in www/pl/tally.pl

```
-- Results --
be 3
not 2
or 1
ought 1
question 1
the 1
to 3
```

Facts vs. Java maps, Ruby hashes, etc.
What's a key difference between using Prolog facts and maps/hashes/etc. to maintain word counts?

A hash or map can be passed around as a value, but Prolog facts are fundamentally objects with global scope. The collection of word/2 facts can be likened to a Ruby global, like \$words = \{\}

If we wanted to maintain multiple tallies simultaneously we could add an id of some sort to word facts.

Example: We might tally word counts for quotations in a document separately from word counts for body content. Calls to count might look like this, count(Type,Word)
and create facts like these:
word(quotes, testing, 3)
word(body, testing, 10)

## Example: Unstacking blocks

Consider a stack of blocks, each of which is uniquely labeled with a letter:


This arrangement could be represented with these facts:

$$
\begin{array}{lll}
\text { on(a,c). } & \text { on(c,e). } & \text { on(e,floor). } \\
\text { on(a,d). } & \text { on(c,f). } & \text { on(f,floor). } \\
\text { on(b,d). } & \text { on(d,f). } & \text { on(g,floor). } \\
& \text { on(d,g). } & \\
\hline
\end{array}
$$

Problem: Define a predicate clean that will print a sequence of blocks to remove from the floor such that no block is removed until nothing is on it.

A suitable sequence of removals for the above diagram is: $a, c, e, b, d, f, g$. Another is a, b, c, d, e, f, g.

## Unstacking blocks, continued

Here's one solution: (blocks.pl)

```
removable(B) :- \+on(_,B).
remove(B) :-
        removable(B),
        retractall(on(B,_)),
        format('Remove ~w\n', B).
```

remove(B) :-
on(Above,B),
remove(Above),
remove(B).
clean :- on(B,floor), remove(B), clean, !.
clean :- \+on(_,_).

How long would in be in Java or Ruby?
Can we tighten it up?
?- clean.
Remove a Remove c Remove e Remove b Remove d Remove f Remove $g$ true.

## Unstacking blocks, continued

A more concise solution:
clean :-

$$
\begin{aligned}
& \text { on(Block,_), \+on(_,Block), } \\
& \text { format('Remove } \sim W \backslash n ', ~ B l o c k), ~ \\
& \text { retractall(on(Block,_)), clean, !. }
\end{aligned}
$$

| a |  | b |  |
| :---: | :---: | :---: | :---: |
| c |  | d |  |
| e | f | g |  |
| floor |  |  |  |

clean :- \+on(_,_).
on( $a, c$ ). on( $a, d$ ). on(b,d)....

Output:
?- clean.
Remove a Remove b Remove c Remove d Remove e Remove f Remove $g$ true.

> Previous sequence: ?- clean.
> Remove a Remove c Remove e Remove b Remove d Remove f Remove g true.

## Brick laying puzzle

## Brick laying

Consider six bricks of lengths $7,5,6,4,3$, and 5 . One way they can be laid into three rows of length 10 is like this:

| 7 |  | 3 |
| :---: | :---: | :---: |
| 5 | 5 |  |
| 6 |  | 4 |

Problem: Write a predicate laybricks that produces a suitable sequence of bricks for three rows of a given length:

$$
\begin{aligned}
& \text { ?- laybricks([7,5,6,4,3,5], 10,Rows). } \\
& \text { Rows }=[[7,3],[5,5],[6,4]] ; \\
& \text { Rows }=[[7,3],[5,5],[4,6]] ; \\
& \text { Rows }=[[7,3],[6,4],[5,5]] . \\
& \text { ?- laybricks([7,5,6,4,3,5],12,Rows). } \\
& \text { false. }
\end{aligned}
$$

In broad terms, how can we approach this problem?

Helper getone
Here is a helper predicate getone(X, List, Remaining) that produces in Remaining a copy of List with X removed:

```
getone(X, [X|T],T).
getone(X, [H|T], [H|N]) :- getone(X, T, N).
```

Usage:

```
?- getone(X,[a,b,a,d],R).
\(\mathrm{X}=\mathrm{a}\),
\(\mathrm{R}=[\mathrm{b}, \mathrm{a}, \mathrm{d}]\);
\(\mathrm{X}=\mathrm{b}\),
R = [a, a, d] ;
\(\mathrm{X}=\mathrm{a}\),
R = [a, b, d] ;
\(\mathrm{X}=\mathrm{d}\),
\(\mathrm{R}=[\mathrm{a}, \mathrm{b}, \mathrm{a}]\);
false.
```

```
?- getone(a,[a,b,a],R).
\(\mathrm{R}=[\mathrm{b}, \mathrm{a}]\);
\(\mathrm{R}=[\mathrm{a}, \mathrm{b}]\);
false.
?- getone(a, [a,b,c,a],R).
\(R=[b, c, a]\);
\(\mathrm{R}=[\mathrm{a}, \mathrm{b}, \mathrm{c}]\);
false.
```

Built-in equivalent: select/3

## Helper layrow

layrow produces a sequence of bricks for a row of a given length:

```
?- layrow([3,2,7,4], 7, BricksLeft, Row).
BricksLeft = [2, 7],
Row = [3,4];
BricksLeft = [3, 2, 4],
Row = [7];
BricksLeft = [2, 7],
Row = [4, 3] ;
false.
```

Implementation:
layrow(Bricks, 0, Bricks, []). \% A row of length zero consists of no
\% bricks and doesn't touch the supply.
layrow(Bricks, RowLen, Left, [Brick|MoreBricksForRow]) :getone(Brick, Bricks, Left0),
RemLen is RowLen - Brick, RemLen $>=0$, layrow(Left0, RemLen, Left, MoreBricksForRow).

## Three rows of bricks

Let's write lay3rows, which is hardwired for three rows:
lay3rows(Bricks, RowLen, [Rowl,Row2,Row3]) :layrow(Bricks, RowLen, LeftAfterl, Rowl), layrow(LeftAfterl, RowLen, LeftAfter2, Row2), layrow(LeftAfter2, RowLen, LeftAfter3, Row3), LeftAfter3 = [].

Usage:
?- lay3rows([2, 1,3,1,2], 3, Rows).
Rows $=[[2,1],[3],[1,2]]$;
Rows $=[[2,1],[1,2],[3]]$;

What is the purpose of LeftAfter3 = []?
How can we generalize it to N rows?

## N rows of bricks

laybricks(+Bricks, +NRows, +RowLen, ?Rows) works like this:
?- laybricks([5, 1,6,2,3,4,3], 3, 8, Rows).
Rows $=[[5,3],[1,4,3],[6,2]]$.
?- laybricks([5, 1,6,2,3,4,3], 8, 3, Rows).
false.
?- laybricks([5, 1,6,2,3,4,3], 2, 12, Rows).
Rows $=[[5,1,6],[2,3,4,3]]$.
?- laybricks([5, 1,6,2,3,4,3], 4, 6, Rows).
Rows = [[5, 1], [6], [2, 4], [3, 3]].
Implementation:
laybricks([], 0, , []).
laybricks(Bricks, Nrows, RowLen, [Row|Rows]) :-
layrow(Bricks, RowLen, BricksLeft, Row),
RowsLeft is Nrows - 1,
laybricks(BricksLeft, RowsLeft, RowLen, Rows).

## N rows of bricks, continued

At hand:
laybricks([], 0, _, []).
laybricks(Bricks, Nrows, RowLen, [Row|Rows]) :-
layrow(Bricks, RowLen, BricksLeft, Row),
RowsLeft is Nrows - 1,
laybricks(BricksLeft, RowsLeft, RowLen, Rows).
laybricks requires that all bricks be used. How can we remove that requirement?
laybricks2(_, 0, _, []).
...second rule the same, but with a call to laybricks2...
?- laybricks2([4,3,2,1], 2, 3, Rows).
Rows $=[[3],[2,1]]$.

Some facts for testing:

```
b(1, [7,5,6,4,3,5]).
b(2, [5, 1,6,2,3,4,3]).
b(3, [8,5,1,4,6,6,2,3,4,3,3,6,3,8,6,4]). % 6xl2
b(4, [8,5,1,4,6,6,2,3,4,3,3,6,3,8,6,4,1]). % 6xl2 with extra l
```

We can query b ( $N$, Bricks) to set Bricks to a particular list.
?- b(l,Bricks), laybricks(Bricks, 2, 10, Rows). false.
?- b(l,Bricks), laybricks2(Bricks, 2, 10, Rows). \% laybricks2
Bricks = [7, 5, 6, 4, 3, 5],
Rows $=[[7,3],[5,5]]$.
?- b(3,Bricks), laybricks(Bricks,6,12,Rows).
Bricks $=[8,5,1,4,6,6,2,3,4 \mid \ldots]$,
Rows $=[[8,1,3],[5,4,3],[6,6],[2,4,3,3],[6,6],[8,4]]$.

## Testing, continued

Let's try a set of bricks that can't be laid into six rows of twelve:
?- b(4,Bricks), laybricks(Bricks,6,12,Rows).
...[the sound of a combinatorial explosion]...
${ }^{\wedge}$ CAction (h for help) ? abort
\% Execution Aborted
?- statistics.
8.240 seconds cpu time for $74,996,337$ inferences
true.
The speed of a Prolog implementation is sometimes quoted in LIPSlogical inferences per second.

2006 numbers, for contrast:
?- statistics.
8.05 seconds cpu time for $25,594,610$ inferences

## The Zebra Puzzle

## The Zebra Puzzle

The Wikipedia entry for "Zebra Puzzle" presents a puzzle said to have been first published in the magazine Life International on December 17, 1962. The facts:

- There are five houses.
- The Englishman lives in the red house.
- The Spaniard owns the dog.
- Coffee is drunk in the green house.
- The Ukrainian drinks tea.
- The green house is immediately to the right of the ivory house.
- The Old Gold smoker owns snails.
- Kools are smoked in the yellow house.
- Milk is drunk in the middle house.
- The Norwegian lives in the first house.
- The man who smokes Chesterfields lives in the house next to the man with the fox.
- Kools are smoked in the house next to the house where the horse is kept.
- The Lucky Strike smoker drinks orange juice.
- The Japanese smokes Parliaments.
- The Norwegian lives next to the blue house.

The article asked readers, "Who drinks water? Who owns the zebra?"

## Zebra Puzzle, continued

We can solve this problem by creating a set of goals and asking Prolog to find the condition under which all the goals are true.

A good starting point is these three facts:

- There are five houses.
- The Norwegian lives in the first house.
- Milk is drunk in the middle house.

Those facts can be represented as this goal:

$$
\begin{aligned}
& \text { Houses }=[\text { house(norwegian, _, _, _, _), \% First house } \\
& \text { house(_, _, _, milk, _), } \\
& \text { _, _] } \\
& \text { \% Second house } \\
& \text { \% Middle house } \\
& \% 4^{\text {th }} \text { and } 5^{\text {th }} \text { houses }
\end{aligned}
$$

Instances of house structures represent knowledge about a house.
house structures have five terms: nationality, pet, smoking preference (remember, it was 1962!), beverage of choice and house color.

Anonymous variables are used to represent "don't-knows".

## Zebra Puzzle, continued

Some facts can be represented with goals that specify structures as members of the list Houses, but with unknown position:

The Englishman lives in the red house. member(house(englishman, _, _, _, red), Houses)

The Spaniard owns the dog. member(house(spaniard, dog, _, _, _), Houses)

Coffee is drunk in the green house. member(house(_, _, _, coffee, green), Houses)

How can we represent The green house is immediately to the right of the ivory house.?

## Zebra Puzzle, continued

At hand:
The green house is immediately to the right of the ivory house.
Here's a predicate that expresses left/right positioning:
left_right(L, R, [L, R | _]).
left_right(L, R, [_ | Rest]) :- left_right(L, R, Rest).
Testing:
?- left_right(Left,Right, [1,2,3,4]).
Left = l,
Right = 2 ;
Left $=2$,
Right $=3$;

Goal: left_right(house(_,_,_,_, ivory), house(_, _, _, _, green), Houses)

## Zebra Puzzle, continued

We have these "next to" facts:

- The man who smokes Chesterfields lives in the house next to the man with the fox.
- Kools are smoked in the house next to the house where the horse is kept.
- The Norwegian lives next to the blue house.

How can we represent these?
We can say that two houses are next to each other if one is immediately left or right of the other:

```
next_to(X,Y, List) :- left_right(X,Y, List).
next_to(X,Y, List) :- left_right(Y, X, List).
```


## Zebra Puzzle, continued

These "next to" facts are at hand:

- The man who smokes Chesterfields lives in the house next to the man with the fox.
- Kools are smoked in the house next to the house where the horse is kept.
- The Norwegian lives next to the blue house.

The facts above expressed as goals:
next_to(house(_,_, chesterfield,_,_),
house(_, fox, _, _, ), Houses)
next_to(house(_, _, kool,_,_),
house(_, horse, _, _, _), Houses)
next_to(house(norwegian, _, _, _,_), house(_, _, _, _, blue), Houses)

## Zebra Puzzle, continued

A few more simple house \& member goals complete the encoding:

- The Ukrainian drinks tea.
member(house(ukrainian, _, _, tea, _), Houses)
- The Old Gold smoker owns snails. member(house(_, snails, old_gold, _, _), Houses)
- Kools are smoked in the yellow house. member(house(_, _, kool, _, yellow), Houses)
- The Lucky Strike smoker drinks orange juice. member(house(_, _, lucky_strike, orange_juice, _), Houses)
- The Japanese smokes Parliaments. member(house(japanese, _, parliment, _, _), Houses)


## Zebra Puzzle, continued

A rule that comprises all the goals:

```
zebra(Zebra_Owner, Water_Drinker) :-
    Houses = [house(norwegian, _, _, _, _), _,
    house(_, _, _, milk, _), _, _],
member(house(englishman, _, _, _, red), Houses),
member(house(spaniard, dog, _, _, _), Houses),
member(house(_, , _, coffee, green), Houses),
member(house(ukrainian, _, _, tea, _), Houses),
left_right(house(_,_,_,_, ivory), house(_,_,_,_, green), Houses),
member(house(_, snails, old_gold, _,_), Houses),
member(house(_, _, kool, _, yellow), Houses),
next_to(house(_,_,chesterfield,_,_),house(_, fox,_,_,_), Houses),
next_to(house(_,, kool,_,_), house(_, horse, _, _, _), Houses),
member(house(_, _, lucky_strike, orange_juice, _), Houses),
member(house(japanese, _, parliment, _, _), Houses),
next_to(house(norwegian,_,_,_,_), house(_,_,_, blue), Houses),
member(house(Zebra_Owner, zebra, _, _, _), Houses),
member(house(Water_Drinker, _, _, water, _), Houses).
```

Note that the last two goals ask the questions of interest.

## Zebra Puzzle, continued

The moment of truth:
?- zebra(_, Zebra_Owner, Water_Drinker).
Zebra_Owner = japanese,
Water_Drinker = norwegian ;
false.
The whole neighborhood:
?- zebra(Houses,_,_), member(H,Houses), writeln(H), fail.
house(norwegian,fox,kool,water,yellow)
house(ukrainian,horse,chesterfield,tea,blue)
house(englishman,snails,old_gold,milk,red)
house(spaniard,dog,lucky_strike,orange_juice,ivory)
house(japanese,zebra,parliment,coffee,green)
false.
Credit: The code above was adapted from sandbox.rulemaker.net/ ngps/l19, by Ng Pheng Siong, who in turn apparently adapted it from work by Bill Clementson in Allegro Prolog.

## Parsing and grammars

Credit: The first part of this section borrows heavily from chapter 12 in Covington.

## A very simple grammar

Here is a grammar for a very simple language. It has four productions.
Sentence => Article Noun Verb

Article $\quad=>$ the | a
Noun $\quad=>$ dog | cat | girl | boy
Verb $\quad=>$ ran | talked | slept
Here are some sentences in the language:
the dog ran
a boy slept
the cat talked
the, dog, cat, etc. are terminal symbols-they appear in the strings of the language. Generation terminates with them.

Sentence, Article, Noun and Verb are non-terminal symbols-they can produce something more.

Sentence is the start symbol. We can generate sentences by starting with it and replacing non-terminals with terminals and non-terminals until only terminals remain.

## A very simple parser

Here is a simple parser for the grammar, expressed as clauses: (parser0.pl)

## sentence(Words) :-

article(Words, Left0), noun(Left0, Leftl), verb(Leftl, []).
article([the| Left], Left).
article([a| Left], Left).
noun([Noun| Left], Left) :- member(Noun, [dog,cat,girl,boy]).
verb([Verb|Left], Left) :- member(Verb, [ran,talked,slept]).

Usage:
?- sentence([the,dog,ran]). true.
?- sentence([the,dog,boy]). false.

```
Sentence => Article Noun Verb
Article => the | a
Noun => dog | cat | girl | boy
Verb => ran | talked | slept
```

?- sentence(S). \% Generates all valid sentences
S = [the, dog, ran];
S = [the, dog, talked] ;
S = [the, dog, slept] ;

## A very simple parser, continued

For reference:
sentence(Words) :-
article(Words, Leftl), noun(Leftl, Left2), verb(Left2, []).
article([the|Left], Left).
article([a| Left], Left).
noun([Noun|Left], Left) :- member(Noun, [dog,cat,girl,boy]).
verb([Verb|Left], Left) :- member(Verb, [ran,talked,slept]).
Note that the heads for article, noun, and verb all have the same form.
Let's look at a clause for article and a unification:

```
article([the|Left], Left).
```

?- article([the,dog,ran], Remaining).
Remaining $=$ [dog, ran].
If Words begins with the or a, then article(Words, Remaining) succeeds and unifies Remaining with the rest of the list. The key idea: article, noun, and verb each consume an expected word and produce the remaining words.
sentence(Words) :-
article(Words, Leftl), noun(Leftl, Left2), verb(Left2, []).
A query sheds light on how sentence operates:
?- article(Words, Left l), noun(Leftl, Left2), verb(Left2, Left3), Left3 = [].
Words = [the, dog, ran],
Leftl = [dog, ran],
Left2 $=[r a n]$,
Left3 = [].
?- sentence([the, dog,ran]).
true.
Each goal consumes one word. The remainder is then the input for the next goal.

Why is verb's result, Left3, unified with the empty list?

## A very simple parser, continued

Here's a convenience predicate that splits up a string and calls sentence.
s (String) :concat_atom(Words, ' ', String), sentence(Words).
sentence(Words) :article(Words, Leftl), noun(Leftl, Left2), verb(Left2, []).

Usage:
?- s('the dog ran'). true.
?- s('ran the dog').
false.

## Grammar rule notation

Prolog's grammar rule notation provides a convenient way to express these stylized rules. Instead of this,

```
sentence(Words) :-
    article(Words, Left0), noun(Left0, Leftl), verb(Leftl, []).
article([the| Left], Left).
article([a| Left], Left).
noun([Noun| Left], Left) :- member(Noun, [dog,cat,girl,boy]).
verb([Verb|Left], Left) :- member(Verb, [ran,talked,slept]).
```

we can take advantage of grammar rule notation and say this,

```
sentence --> article, noun, verb.
article --> [a]; [the].
noun --> [dog]; [cat]; [girl]; [boy].
verb --> [ran]; [talked]; [slept].
```

Note that the literals (terminals) are specified as singleton lists.
The semicolon is an "or". Alternative: noun --> [dog]. noun --> [cat]....

## Grammar rule notation, continued

```
$ cat parserl.pl
sentence --> article, noun, verb.
article --> [a]; [the].
noun --> [dog]; [cat]; [girl]; [boy].
verb --> [ran]; [talked]; [slept].
```

listing can be used to see the clauses generated for that grammar.
?- [parserl].
...
?- listing(sentence).
sentence ( $A, D$ ) :- $\operatorname{article}(A, B)$, noun( $B, C), \operatorname{verb}(C, D)$.
?- listing(article).
article(A, B) :-
( $\mathrm{A}=[\mathrm{a} \mid \mathrm{B}]$
; $A=[$ the|B]
).
Note that the predicates generated for sentence, article and others have an arity of 2 .

## Grammar rule notation, continued

At hand: (a definite clause grammar)
sentence --> article, noun, verb.
article --> [a]; [the].
noun --> [dog]; [cat]; [girl]; [boy]. verb --> [ran]; [talked]; [slept].
?- listing(sentence).
sentence(A, D) :- $\operatorname{article}(A, B)$, noun(B, C), verb(C, D).
?- listing(article).
$\operatorname{article}(A, B):-(A=[a \mid B] ; \quad A=[$ the $\mid B])$.
?- sentence([a,dog,talked,to,me], Leftover).
Leftover $=$ [to, me].
?- sentence([a,bird,talked,to,me], Leftover). false.

Remember that sentence, article, verb, and noun are non-terminals. dog, cat, ran, talked, are terminals, represented as atoms in singleton lists.

## Grammar rule notation, continued

Below we've added a second term to the call to sentence, and mixed in a regular rule for verb along with the grammar rule.

```
s(String) :- % parserla.pl
    concat_atom(Words,' ', String), sentence(Words,[]).
sentence --> article, noun, verb.
article --> [a]; [the].
noun --> [dog]; [cat]; [girl]; [boy].
verb --> [ran]; [talked]; [slept].
verb([Verb|Left], Left) :- verb0(Verb).
verb0(jumped). verb0(ate). verb0(computed).
?- s('a boy computed').
true.
?- s('a boy computed pi').
false.
```


## Goals in grammar rules

We can insert ordinary goals into grammar rules by enclosing the goal(s) in curly braces.

Here is a chatty parser that recognizes the language described by the regular expression $\mathrm{a}^{*}$ :
parse(S) :- atom_chars(S,Chars), string(Chars, []). \% parser6.pl
string --> as.
as --> [a], \{writeln('got an a')\}, as.
as --> [], \{writeln('empty match')\}.

Usage:
?- parse(aaa). got an a got an a got an a empty match true.
?- parse(aab). got an a got an a empty match empty match empty match false.

| What if the as clauses are |
| :--- |
| swapped? |
| ?- parse(aaa). |
| empty match |
| got an a |
| empty match |
| got an a |
| empty match |
| got an a |
| empty match |
| true. |

What if the as clauses are
swapped?
?- parse(aaa).
empty match
got an a
empty match
got an a
empty match
got an a
empty match
true.

## Parameters in non-terminals

We can add parameters to the non-terminals in grammar rules. The following grammar recognizes a* and produces the length, too.

```
parse(S, Count) :-
string(N) --> as(N).
as(N) --> [a], as(M), {N is M + l}.
as(0) --> [].
```

\% parser6a.pl
atom_chars(S,Chars), string(Count,Chars, []).

Usage:
?- parse(aaa, N).
$\mathrm{N}=3$.
?- parse(aaab, N).
false.

## Parameters in non-terminals, continued

Here is a grammar that recognizes $\mathrm{a}^{\mathrm{N}} \mathrm{b}^{2 \mathrm{~N}} \mathbf{c}^{3 \mathrm{~N}}$ : (parser7a.pl)

```
parse(S,L) :- atom_chars(S,Chars), string(L, Chars, []).
string([N,NN,NNN]) -->
            as(N),{NN is 2*N}, bs(NN),{NNN is 3*N}, cs(NNN).
as(N) --> [a], as(M), {N is M+l}.
as(0) --> [].
bs(N) --> [b], bs(M), {N is M+l}.
bs(0) --> [].
cs(N) --> [c], cs(M),{N is M+l}.
cs(0) --> [].
?- parse(aabbbbcccccc, L).
L = [2,4,6] .
?- parse(aabbc, L).
false.
```

Can this language be described with a regular expression?

## Parameters in non-terminals, continued

How could we handle $\mathbf{a}^{\mathrm{X}} \mathbf{b}^{\mathrm{Y}} \mathbf{c}^{\mathrm{Z}}$ where $\mathrm{X}<=\mathrm{Y}<=\mathrm{Z}$ ?

```
?- parse(abbbccc, L).
L=[l,3,3] .
?- parse(ccccc, L).
L}=[0,0,5] .
?- parse(aaabbc, L).
false.
parse(S,L) :- atom_chars(S,Chars), string(L, Chars, []). % parser7b.pl
string([X,Y,Z]) --> as(X), bs(Y), {X =< Y}, cs(Z), {Y =< Z}.
as(N) --> [a], as(M), {N is M+l}.
as(0) --> [].
bs(N) --> [b], bs(M), {N is M+l}.
bs(0) --> [].
cs(N) --> [c], cs(M),{N is M+l}.
cs(0) --> [].
```

Problem: Write a parser that recognizes a string of digits and creates an integer from them:

```
?- parse('4341', N).
N=4341 .
?- parse('lx3', N).
false.
```

Solution:
parse(S,N) :- \% parser8.pl
atom_chars(S, Chars), intval(N,Chars,[]),integer(N).
intval(N) --> digits(Digits), $\{$ atom_number(Digits,N) \}.
digits(Digit) --> [Digit], \{digit(Digit)\}.
digits(Digits) --> [Digit], \{digit(Digit) \},
digits(More), \{concat_atom([Digit,More],Digits)\}.
$\operatorname{digit(}{ }^{\prime} 0$ '). $\operatorname{digit(}{ }^{\prime} 1$ '). $\operatorname{digit(}(2 ') . .$.

How do the digits(...) rules work?

## A list recognizer

Consider a parser that recognizes lists consisting of positive integers and lists:
?- parse('[1,20,[30,[[40]],6,7],[]]'). true.
?- parse('[1,20,,[30,[[40]],6,7],[]]').
false.
?- parse('[ 1, 2 , 3 ]'). \% Whitespace! How could we handle it? false.

Implementation: (list.pl)
parse(S) :- atom_chars(S, Chars), list(Chars, []).

```
list --> ['['], values, [']'].
```

list --> ['['], [']'].
values --> value.
values --> value, [','], values.
value --> digits(_). \% digits(...) from previous slide
value --> list.

## "Real" compilation

These parsing examples are far short of what's done in a compiler. The first phase of compilation is typically to break the input into "tokens". Tokens are things like identifiers, individual parentheses, string literals, etc.

Input text like this,
[ 1, [30+400], 'abc']
might be represented as a stream of tokens with this Prolog list:
[lbrack, integer(l), comma, lbrack, integer(30), plus, integer(400), rbrack, comma, atom(abc), rbrack]

The second phase of compilation is to parse the stream of tokens and generate code (traditional compilation) or execute it immediately (interpretation).

We could use a pair of Prolog grammars to parse source code:

- The first one would parse character-by-character and generate a token stream like the list above. (A scanner.)
- The second grammar would parse that token stream.


## Odds and ends

## Collberg's Architecture Discovery Tool

In the mid-1990s Dr. Collberg developed a system that is able to discover the instruction set, registers, addressing modes and more for a machine given only a C compiler for that machine.

The basic idea is to use the C compiler of the target system to compile a large number of small but carefully crafted programs and then examine the machine code produced for each program to make inferences about the architecture. The end result is a machine description that in turn can be used to generate a code generator for the architecture.

The system is written in Prolog. What makes Prolog well-suited for this task?

Paper: http://www.cs.arizona.edu/~collberg/content/research/ papers/collberg02automatic.pdf

## The Prolog 1000

The Prolog 1000 is a compilation of applications written in Prolog and related languages. Here is a sampling of the entries:

AALPS
The Automated Air Load Planning System provides a flexible spatial representation and knowledge base techniques to reduce the time taken for planning by an expert from weeks to two hours. It incorporates the expertise of loadmasters with extensive cargo and aircraft data.

## ACACIA

A knowledge-based framework for the on-line dynamic synthesis of emergency operating procedures in a nuclear power plant.

ASIGNA
Resource-allocation problems occur frequently in chemical plans. Different processes often share pieces of equipment such as reactors and filters. The program ASIGNA allocates equipment to some given set of processes. (2,000 lines)

## The Prolog 1000, continued

Coronary Network Reconstruction
The program reconstructs a three-dimensional image of coronary networks from two simultaneous X-Ray projections. The procedures in the reconstruction-labelling process deal with the correction of distortion, the detection of center-lines and boundaries, the derivation of 2-D branch segments whose extremities are branching, crossing or end points and the 3-D reconstruction and display.

All algorithmic components of the reconstruction were written in the C language, whereas the model and resolution processes were represented by predicates and production rules in Prolog. The user interface, which includes a main panel with associated control items, was developed using Carmen, the Prolog by BIM user interface generator.

## DAMOCLES

A prototype expert system that supports the damage control officer aboard Standard frigates in maintaining the operational availability of the vessel by safeguarding it and its crew from the effects of weapons, collisions, extreme weather conditions and other calamities. ( $>68,000$ lines)

## The Prolog 1000, continued

## DUST-EXPERT

Expert system to aid in design of explosion relief vents in environments where flammable dust may exist. (> 10,000 lines)

## EUREX

An expert system that supports the decision procedures about importing and exporting sugar products. It is based on about 100 pages of European regulations and it is designed in order to help the administrative staff of the Belgian Ministry of Economic Affairs in filling in forms and performing other related operations. ( $>38,000$ lines)

## GUNGA CLERK

Substantive legal knowledge-based advisory system in New York State Criminal Law, advising on sentencing, pleas, lesser included offenses and elements.

## MISTRAL

An expert system for evaluating, explaining and filtering alarms generated by automatic monitoring systems of dams. (1,500 lines)

The full list is in www/pl/Prologl000.txt. Several are over 100K lines of code.

## Lots of Prologs

For a Fall 2006 honors section assignment Maxim Shokhirev was given the task of finding as many Prolog implementations as possible in one hour. His results:

1. DOS-PROLOG
http://www.lpa.co.uk/dos.htm
2. Open Prolog
http://www.cs.tcd.ie/open-prolog/
3. Ciao Prolog
http://www.clip.dia.fi.upm.es/Software/Ciao
4. GNU Prolog
http://pauillac.inria.fr/~diaz/gnu-prolog/
5. Visual Prolog (PDC Prolog and Turbo Prolog)
http://www.visual-prolog.com/
6. SWI-Prolog
http://www.swi-prolog.org/
7. tuProlog
http://tuprolog.alice.unibo.it/
8. HiLog
ftp://ftp.cs 9. ?Prolog
http://www.lix.polytechnique.fr/Labo/Dale.Miller/
1Prolog/
9. F-logic
http://www.cs.umbc.edu/771/papers/flogic.pdf
10. OW Prolog
http://www.geocities.com/owprologow/
11. FLORA-2
http://flora.sourceforge.net/
12. Logtalk
http://www.logtalk.org/
13. WIN Prolog
http://www.lpa.co.uk/
14. YAP Prolog
http://www.ncc.up.pt/~vsc/Yap
15. AI::Prolog
http://search.cpan.org/~ovid/AI-Prolog-0.734/lib/AI/
Prolog.pm
16. SICStus Prolog
http://www.sics.se/sicstus/
17. ECLiPSe Prolog
http://eclipse.crosscoreop.com/
18. Amzi! Prolog
http://www.amzi.com/
19. B-Prolog
http://www.probp.com/
20. MINERVA
http://www.ifcomputer.co.jp/MINERVA/
21. Trinc Prolog
http://www.trinc-prolog.com/

## And 50 more!

## Ruby meets Prolog

http://www.artima.com/forums/flat.jsp?forum=123\&thread=182574 describes a "tiny Prolog in Ruby".

Here is member:

```
member[cons(:X,:Y),:X].fact
member[cons(:Z,:L), :X] <<= member[:L,:X]
```

Here's the common family example:

```
sibling[:X,:Y] <<= [parent[:Z,:X], parent[:Z,:Y], noteq[:X,:Y]]
parent[:X,:Y] <<= father[:X,:Y]
parent[:X,:Y] <<= mother[:X,:Y]
# facts: rules with "no preconditions"
father["matz", "Ruby"].fact
mother["Trude", "Sally"].fact
query sibling[:X, "Sally"]
# >> l sibling["Erica", "Sally"]
```


## In conclusion...

Parsing with definite clause grammars (slides 225-240)
More with...
Puzzle solving
Higher-order predicates
Expert systems
Natural language processing
Constraint programming
Look at Prolog implementation with the Warren Abstract Machine.
Continued study:
More in Covington and Clocksin \& Mellish.
The Art of Prolog by Sterling and Shapiro

