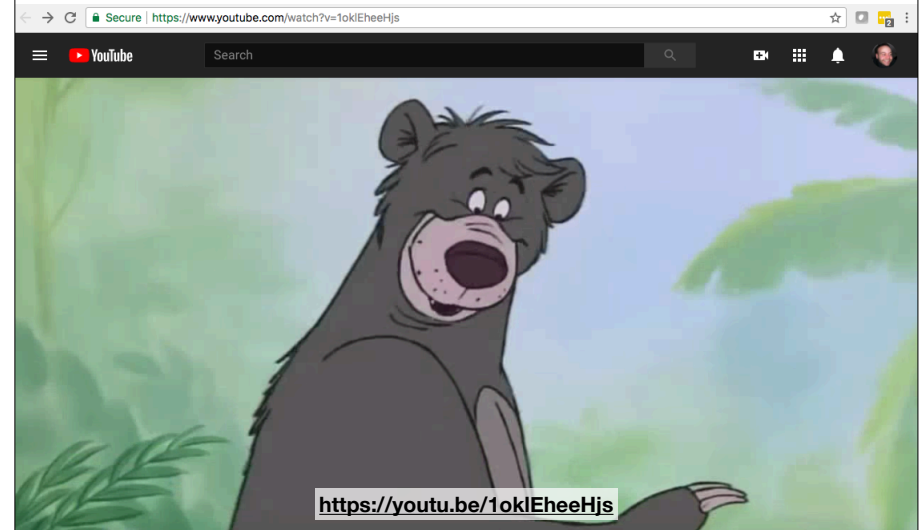
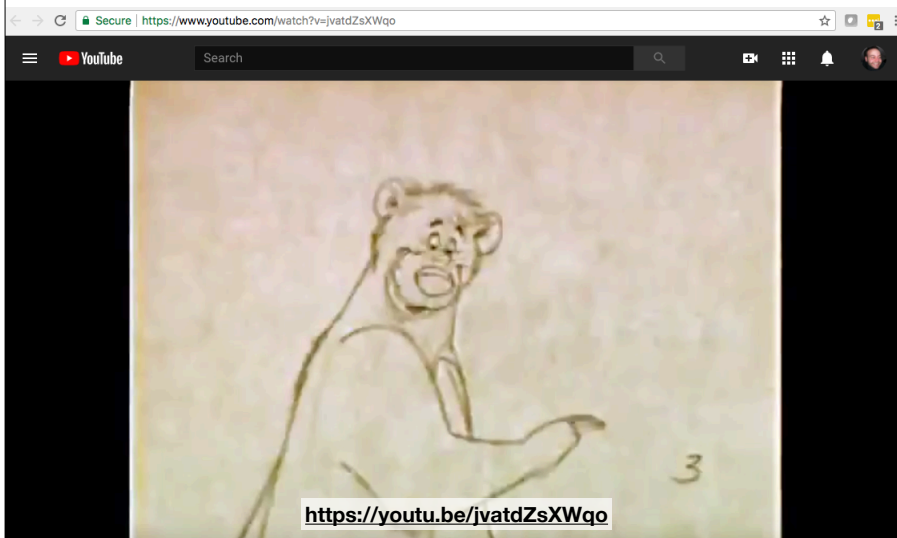


Animation

Jungle Book (1967)



Pencil Test

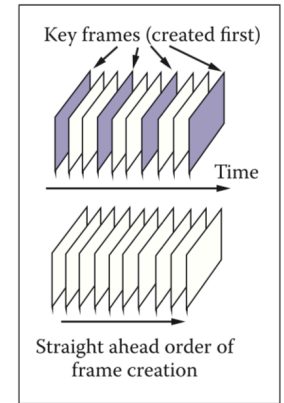


Computer Animation

Keyframing

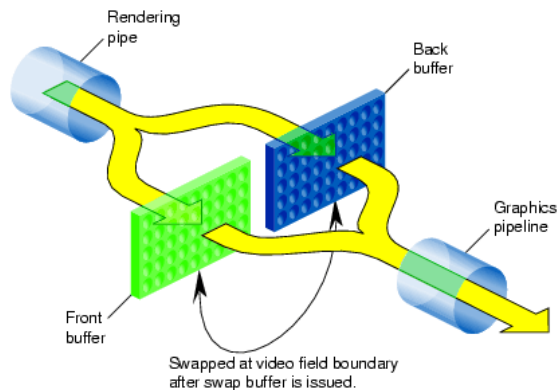
Keyframe Animation

- Idea: Draw a subset of important frames (called **key frames**) and fill in the rest with *in-betweens*
- In hand-drawn animation, the head animator would draw the poses and the assistants would do the rest
- In computer animation, the artist draws the keys and the computer does the in-betweening
 - Interpolation is used to fill in the rest!



Double Buffering

- If you draw directly to video buffer, the user will see the drawing happen
- Particularly noticeable artifacts when doing animation



http://techpubs.sgi.com/library/dynweb_docs/linux/SGI_Developer/books/Perf_GetStarted/sgi_html/figures/double_buffering.gif

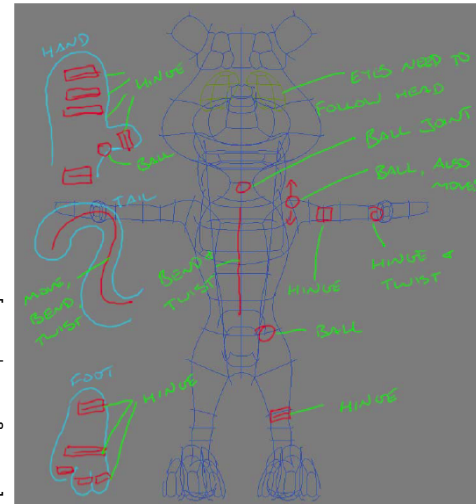
Controlling geometry conveniently

- Manually place every control point at every keyframe?
 - labor intensive
 - hard to get smooth, consistent motion
- Animate using smaller set of meaningful *degrees of freedom*
 - modeling DOFs are inappropriate for animation
e.g. “move one square inch of left forearm”
 - animation DOFs need to be higher level
e.g. “bend the elbow”

Controlling shape for animation

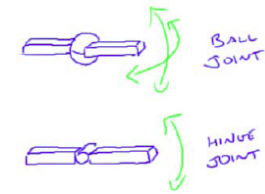
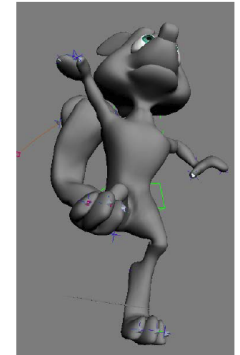
- Start with *modeling DOFs* (control points)
- *Deformations* control those DOFs at a higher level
 - Example: move first joint of second finger on left hand
- *Animation controls* control those DOFs at a higher level
 - Example: open/close left hand
- Both cases can be handled by the same kinds of deformers

Character with DOFs

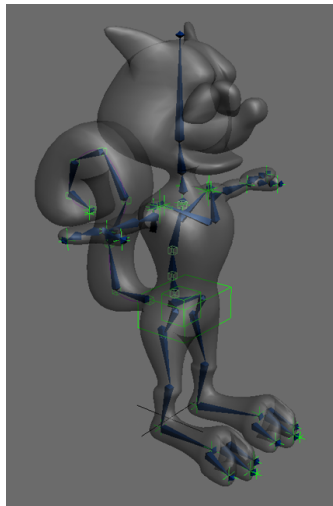


[Greenberg/Pellacini | CIS 565]

A visual description of the possible movements for the squirrel



Rigged character



- Surface is deformed by a set of *bones*
- Bones are in turn controlled by a smaller set of *controls*
- The controls are useful, intuitive DOFs for an animator to use

[CIS 565 staff]

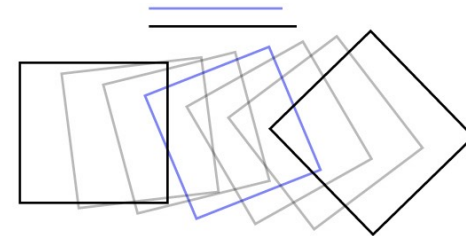
Interpolating Rotations

The most basic animation control

- Affine transformations position things in modeling
- Time-varying affine transformations move things around in animation
- A hierarchy of time-varying transformations is the main workhorse of animation
 - and the basic framework within which all the more sophisticated techniques are built

Interpolating transformations

- Move a set of points by applying an affine transformation
- How to animate the transformation over time?
 - interpolate the matrix entries from keyframe to keyframe?
this is fine for translations but bad for rotations



Interpolating Rotations

$$\frac{1}{2} \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} + \frac{1}{2} \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$$

90° CW *90° CCW*

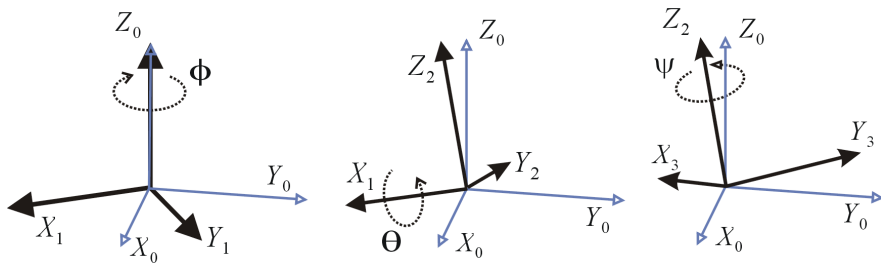
Not a rotation matrix!

Interpolating transformations

- Linear interpolation of matrices is not effective
 - leads to shrinkage when interpolating rotations
- One approach: always keep transformations in a canonical form (e.g. translate-rotate-scale)
 - then the pieces can be interpolated separately
 - rotations stay rotations, scales stay scales, all is good

Issues occurs when the source and target angles are not close to each other

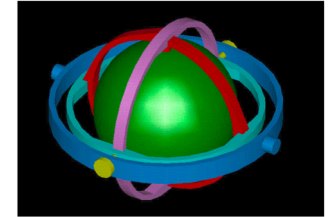
Could Instead Decompose Rotation by Euler Angles



<http://upload.wikimedia.org/wikipedia/commons/7/73/EulerG.png>

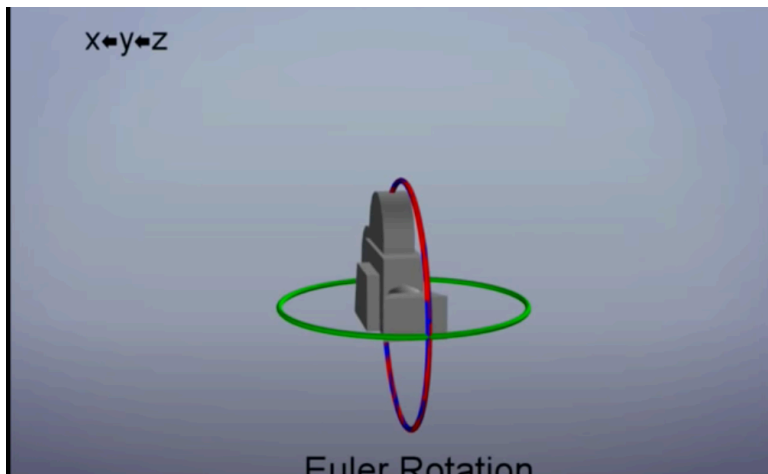
Parameterizing rotations

- Euler angles
 - rotate around x, then y, then z
 - nice and simple
- $$R(\theta_x, \theta_y, \theta_z) = R_z(\theta_z)R_y(\theta_y)R_x(\theta_x)$$

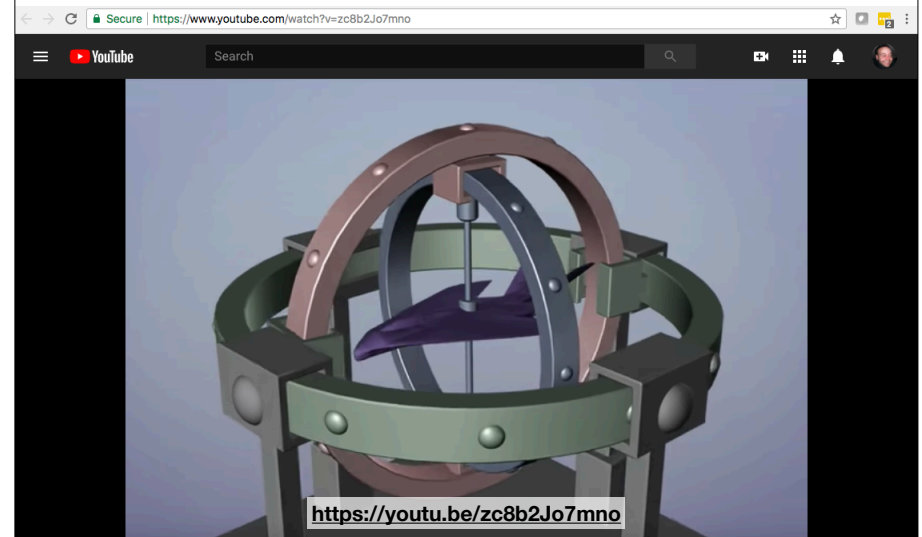


© 2018 Steve Marschner • 20
(with previous instructors James Bab)

<https://youtube.com/clip/UgkxUmrgadPxcCNZAFuTCBA0ZUc0yRb3KGWk>

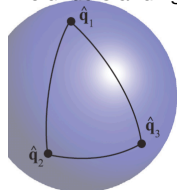


Gimbal Lock



Quaternions Representation and their properties

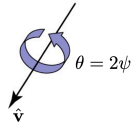
- Representing each rotation as a 4 values
- Encapsulate a rotation axis, and amount of rotation
- (if rotation axis is X,Y,Z, then we are back to Euler Coordinates)
- Corresponds to points in the 4D unit sphere. Yet lets stick to the 3D unit sphere
- Represent rotations by source and destination on unit sphere, with the understanding that rotation is along a geodesic (shortest path).
- No Gimble lock
- Could be represented as 4×4 matrices, so could be concatenated easily (matrix multiplication)



Rotation from $q_1 \rightarrow q_2$ could be specified by the axis of rotation $(o - q_1) \times (o - q_2)$ and the length (in radians) of this arc

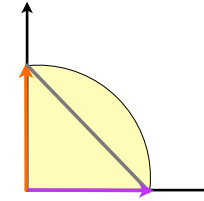
This is a good start. This solves the Gimble Lock issue, but fail to address

- 1) Rotation around its own axis (the missing degree of freedom)
- 2) Concatenations of rotations



Interpolating between quaternions

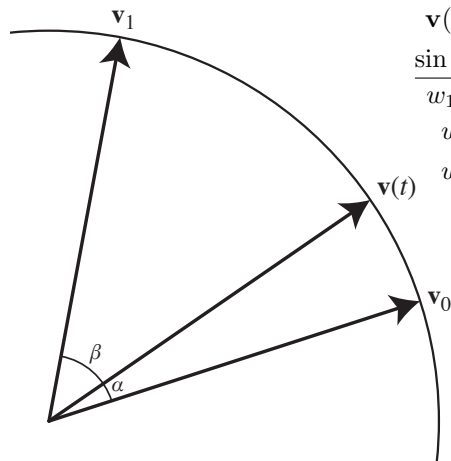
- Why not linear interpolation?
 - Need to be normalized
 - Does not have constant rate of rotation



$$\frac{(1 - \alpha)x + \alpha y}{\|(1 - \alpha)x + \alpha y\|}$$

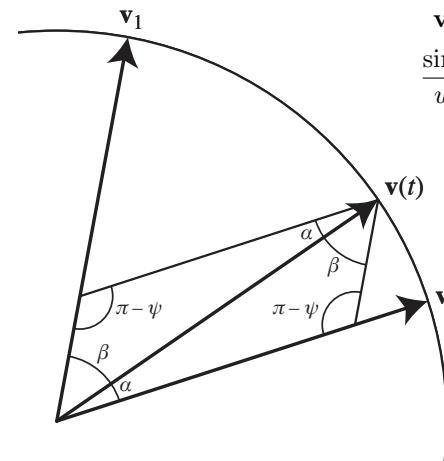
<https://www.geogebra.org/m/mwuczhiw>

Spherical linear interpolation (“slerp”)



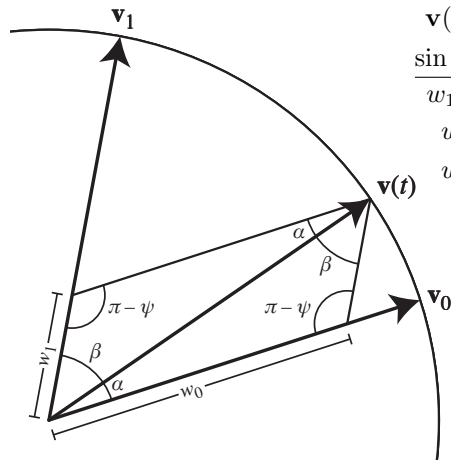
$$\begin{aligned} \alpha + \beta &= \psi \\ \mathbf{v}(t) &= w_0 \mathbf{v}_0 + w_1 \mathbf{v}_1 \\ \frac{\sin \alpha}{w_1} &= \frac{\sin \beta}{w_0} = \frac{\sin(\pi - \psi)}{1} = \sin \psi \\ w_0 &= \sin \beta / \sin \psi \\ w_1 &= \sin \alpha / \sin \psi \\ \psi &= \cos^{-1}(\mathbf{v}_0 \cdot \mathbf{v}_1) \end{aligned}$$

Spherical linear interpolation (“slerp”)



$$\begin{aligned} \alpha + \beta &= \psi \\ \mathbf{v}(t) &= w_0 \mathbf{v}_0 + w_1 \mathbf{v}_1 \\ \frac{\sin \alpha}{w_1} &= \frac{\sin \beta}{w_0} = \frac{\sin(\pi - \psi)}{1} = \sin \psi \\ w_0 &= \sin \beta / \sin \psi \\ w_1 &= \sin \alpha / \sin \psi \\ \psi &= \cos^{-1}(\mathbf{v}_0 \cdot \mathbf{v}_1) \end{aligned}$$

Spherical linear interpolation (“slerp”)



$$\alpha + \beta = \psi$$

$$\mathbf{v}(t) = w_0 \mathbf{v}_0 + w_1 \mathbf{v}_1$$

$$\frac{\sin \alpha}{w_1} = \frac{\sin \beta}{w_0} = \frac{\sin(\pi - \psi)}{1} = \sin \psi$$

$$w_0 = \sin \beta / \sin \psi$$

$$w_1 = \sin \alpha / \sin \psi$$

$$\psi = \cos^{-1}(\mathbf{v}_0 \cdot \mathbf{v}_1)$$

Quaternion Interpolation

- Spherical linear interpolation naturally works in any dimension
- Traverses a great arc on the sphere of unit quaternions
 - Uniform angular rotation velocity about a fixed axis

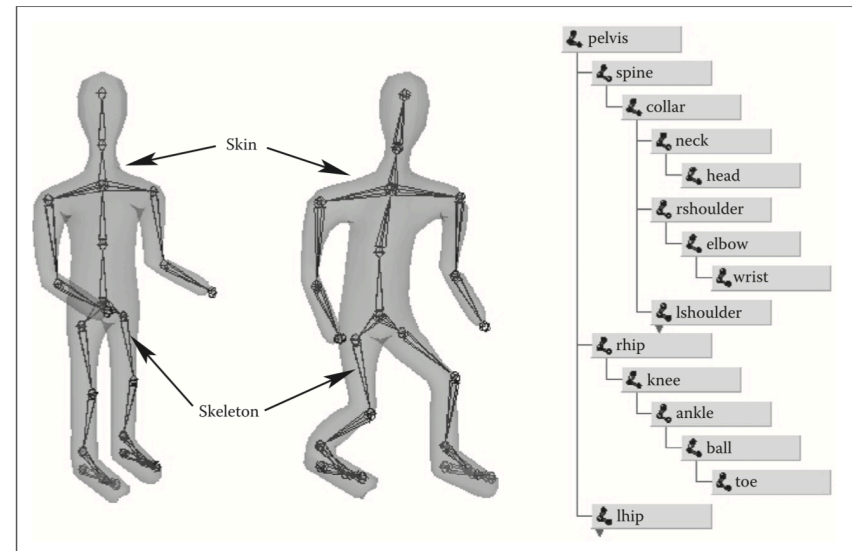
$$\psi = \cos^{-1}(q_0 \cdot q_1)$$

$$q(t) = \frac{q_0 \sin(1-t)\psi + q_1 \sin t\psi}{\sin \psi}$$

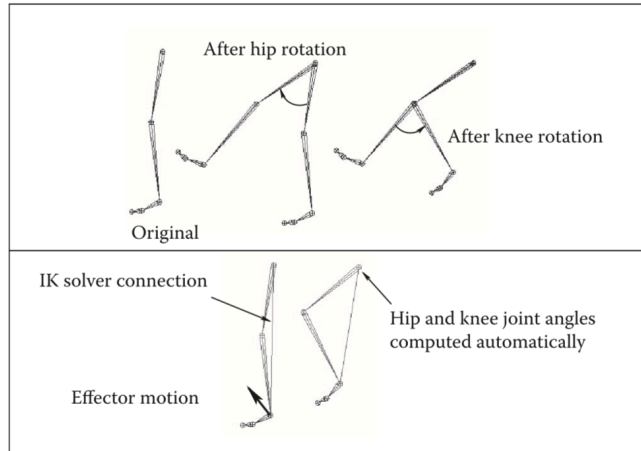
<https://www.geogebra.org/m/mwuczjw>

Character Animation

Animating w/ Skeletal Hierarchies



Forward vs. Inverse Kinematics



Inverse Kinematics Solves for all Intermediate Constraints

The image shows a YouTube video player interface. The video title is 'FORWARD vs. INVERSE KINEMATICS'. The thumbnail is split into two halves: a green half on the left and a blue half on the right. The green half shows a skeletal model of a two-link arm with joints labeled 'BONE 1' and 'BONE 2'. The blue half shows a similar model with a dashed line indicating a target position for the end effector. A URL is displayed at the bottom: <https://youtu.be/0a9qlj7kwiA?t=50>