## 1 Introduction

The purpose of this assignment is improve your Icon programming skills. In particular, you will be using Icon tables, lists, and sets, and do parsing with Icon's string scanning procedures.

The program you will build will display arbitrary undirected graphs in a "nice" way using an iterative algorithm. Graphs are common in many applications which makes such graph drawing programs very useful. See, for example, http://www.graphviz.org which is installed on lectura as the dot program.

We will be grading on correctness and style. Every procedure should be adequately formatted and documented.

This assignment can be worked in teams of two.

## 2 A Graph Module [30 points]

The first step is to create a module graph.icn which will allow us to create new graphs. It has routines for creating an empty graph, adding nodes to this graph, traversing the nodes and edges of the graph, and printing it out. The routines that you need to implement are:

```
record GRAPH(nodes, edges)
procedure graph_create(n)
procedure graph_nodecount(g)
procedure graph_nodes(g)
procedure graph_edges(g, v)
procedure graph_addedge(g, u, v)
procedure graph_show(g)
```

Here is how you would use these routines to create a new graph:

```
g1 := graph_create(5)
graph_addedge(g1, 1, 2)
graph_addedge(g1, 2, 3)
graph_addedge(g1, 3, 4)
graph_addedge(g1, 4, 5)
```

Here's how you'd get the number of nodes, traverse the nodes and edges, and print out the graph:

```
write("Number of nodes: ", graph_nodecount(g1));
write("Outgoing edges from node 2:")
every i := graph_edges(g1, 1) do writes(" ", i)
write("\nNodes:")
every i := graph_nodes(g1) do writes(" ", i)
write("")
graph_show(g1)
g6 := graph_read("g2.gdl")
graph_show(g6)
```

This testing code can be found in the file testgraph.icn, and the output should look like this:

```
> testgraph
Number of nodes: 5
Outgoing edges from node 2:
    2
Nodes:
    12345
1: 2
2: 1 3
3: 2 4
4:3 5
5:4
Graph read from g2.gdl:
1: 2 3
2: 1 3
3: 1 2
graph_read(file) reads a graph from a file in the following format:
3
1--2
1--3
2--3
```

The first number is the number of nodes. On subsequent lines the edges are listed, one per line. graph_read (file) should be implemented using Icon's string scanning functions.

The graph should be represented as a record

```
record GRAPH(nodes, edges)
```

where nodes is simply a list of the nodes $[1,2, \ldots, n]$. edges is a table indexed by node number. For every node $i$, edges [ $i$ ] is a set of the outgoing edges from $i$. For example, if the graph contains the edges $1 \rightarrow 2,1 \rightarrow 3$, then edges [i] should be the set $\{2,3\}$.

A template file graph.icn will be provided for you. The comments give more details with respect to implementation and error handling.

## 3 A Graph Generation Module [30 points]

To have something cool to display, we next write the module graphgen.icn which generates common graph types. We write routines to generate list, cycle, star, complete, and binary tree graphs. The list graph routine has been give to you, the rest you have to write yourselves:

```
# A simple link graph where every node n is connected
# to node n+1.
procedure graphgen_List(n)
    local g
    g := graph_create(n)
    every i := 1 to n-1 do
        graph_addedge(g, i, i+1)
    return g
end
# A cycle graph where every node n is connected
# to node n+1, and the last node is connected to
# the first.
procedure graphgen_Cycle(n)
# A star graph where node number 1 is connected to
# every other node.
procedure graphgen_Star(n)
# A complete graph where every node is connected to
# every other node.
procedure graphgen_K(n)
# A binary tree graph where every node n is connected
# to nodes 2n and 2n+1, provided these exist.
procedure graphgen_BinTree(n)
```

There's a test program testgraphgen.icn given to you that prints out each graph type:

```
write("\nList graph:")
g1 := graphgen_List(5)
graph_show(g1)
write("\nCycle graph:")
g2 := graphgen_Cycle(5)
graph_show(g2)
write("\nStar graph:")
```

```
g3 := graphgen_Star(5)
graph_show(g3)
write("\nK(5) graph:")
g4 := graphgen_K(5)
graph_show(g4)
write("\nBinTree graph:")
g5 := graphgen_BinTree(5)
graph_show(g5)
```

The output should be like this:

```
> make testgraphgen
> testgraphgen
List graph:
1: 2
2: 1 3
3: 2 4
4: 3 5
5: 4
Cycle graph:
1: 2 5
2: 1 3
3: 2 4
4: 3 5
5: 14
Star graph:
1: 2 3 4 5
2: 1
3: 1
4: 1
5: 1
K(5) graph:
1: 1 2 345
2: 1 2 3 45
3: 1 2 3 4 5
4: 1 2 3 4 5
5:12345
BinTree graph:
1: 2 3
2: 145
3: 1
4: 2
5: 2
```

A template file graphgen.icn will be provided for you.

## 4 A Graph Drawing Module [40 points]

The final module is gdraw.icn which does the actual graph layout. It will be using the point.icn module from the last assignment.

The basic idea of the algorithm can be seen from the main routine, which will be given to you:

```
procedure gdraw_layout(g, W, L, iters, tweak, delay)
    local area, pos, disp, temperature, i
    # Make tweak global so we don't have to carry it
    # around everywhere.
    TWEAK := tweak
    # Will become smaller with each iteration so
    # that changes to the node positions will be
    # less and less.
    temperature := W/10
    # Start with all nodes at random positions.
    pos := point_randomList(graph_nodecount(g),W,L)
    every i := 1 to iters do {
            rdisp := gdraw_repulsiveForce(g, pos, W, L)
            adisp := gdraw_attractiveForce(g, pos, W, L)
            pos := gdraw_positionNodes(g, pos, rdisp, adisp, W, L, temperature)
            temperature -:= W/10/iters
            if delay>0 then
            graph_draw(g, pos, W, L, delay)
    }
    return pos
end
```

The algorithm is iterative. It starts out by placing each node in a random position. In each iteration it computes two forces acting on each node. These are given in the variables rdisp and adisp (both are lists of POINTs, one per node). rdisp[i] is the repulsive force acting on node i. adisp[i] is the attractive force acting on node i. Nodes that are attached with an edge attract each other. Nodes which are not attached to each other try to push each other away. temperature gets smaller with each iteration, making the movements of the nodes smaller and smaller, as they settle in on their final positions.

Your job is to implement the routines

```
procedure gdraw_repulsiveForce(g, pos, W, L)
procedure gdraw_attractiveForce(g, pos, W, L)
procedure gdraw_positionNodes(g, pos, rdisp, adisp, W, L, temp)
```

gdraw_repulsiveForce ( g , pos, W, L) takes the graph g and the current position pos as argument. pos is a a list of POINTs, one per node, giving the current location of each node.disp is a a list of POINTs, one per node, giving the current location of each node.

```
set \(\operatorname{disp}_{v}\) to \((0,0)\) for all nodes \(v\)
for every node \(v\) do
        for every node \(u \neq v\) do
            \(\Delta \leftarrow \operatorname{pos}_{v}-\operatorname{pos}_{u}\)
            \(\Delta_{\text {normal }} \leftarrow \operatorname{normal}(\Delta)\)
            if \(\Delta_{\text {normal }}\) is \(<0.01\) set it to 0.01
            \(\operatorname{disp}_{v} \leftarrow \operatorname{disp}_{v}+\Delta / \Delta_{\text {normal }} * \operatorname{fr}\left(g, W, L, \Delta_{\text {normal }}\right)\)
return disp
```

The normal routine is already implemented in the point module. fr is a "magic" function that is given to you in gdraw.icn.
gdraw_attractiveForce ( g , pos, $\mathrm{W}, \mathrm{L}$ ) takes the same arguments and returns the same type of result as gdraw_repulsiveForce. Here's the pseudo-code:

```
set disp}v\mathrm{ to (0,0) for all nodes v
for every node v do
    for every edge ( }v,u\mathrm{ ) do
        \Delta\leftarrow\mp@subsup{\operatorname{pos}}{v}{}-\mp@subsup{\operatorname{pos}}{u}{}
        \Deltanormal }\leftarrow\operatorname{normal}(\Delta
        if }\mp@subsup{\Delta}{\mathrm{ normal is < 0.01 set it to 0.01}}{
        \mp@subsup{\operatorname{disp}}{v}{}\leftarrow\mp@subsup{\operatorname{disp}}{v}{}-\Delta/\mp@subsup{\Delta}{\mathrm{ normal }}{}*\textrm{fa}(g,W,L,\mp@subsup{\Delta}{\mathrm{ normal }}{})
        \mp@subsup{\operatorname{disp}}{u}{}\leftarrow\mp@subsup{\operatorname{disp}}{u}{}+\Delta/\mp@subsup{\Delta}{\mathrm{ normal }}{}*\textrm{fa}(g,W,L,\mp@subsup{\Delta}{\mathrm{ normal }}{})
return disp
```

fa is another "magic" function that is given to you in gdraw.icn.
Finally, we're implementing the function gdraw_positionNodes (g, pos, rdisp, adisp, W, L, temp). It takes the old position of the nodes pos and computes new ones, based on what gdraw_repulsiveForce and gdraw_attractiveForce returned (rdisp and adisp). temp is the current "temperature" (how much we want the nodes to move), a real number. Here's the pseudo-code:

```
disp \(\leftarrow\) rdisp + adisp
for every node \(v\) do
    \(\operatorname{pos}_{v} \leftarrow \operatorname{pos}_{v}+\operatorname{disp}_{v} / \operatorname{normal}^{\left(\operatorname{disp}_{v}\right) * \text { temp }}\)
    \(x \leftarrow \min \left(W / 2, \max \left(-W / 2, \operatorname{pos}_{v} \cdot x\right)\right)\)
    \(y \leftarrow \min \left(L / 2, \max \left(-L / 2, \operatorname{pos}_{v} \cdot y\right)\right)\)
    \(\operatorname{pos}_{v} \leftarrow(x, y)\)
return pos
```

The first line simply adds the results of gdraw_repulsiveForce and gdraw_attractiveForce together. (We could tweak this, if we wanted to, by weighting the addition (multiplying adisp with some constant to make the drawing prettier), but we won't.) The two lines with min and max in them simply make sure that the new $x$ and $y$ coordinates are inside the drawing window.

## 5 The Main Program

The main program has been written for you. It simply parses the command line, generates a graph (or reads one from a file), and invokes the graph layout routine. Here is an example:

```
> main -g tree -n 10 -i 50 -d 0
```

-g tree -n 10 specifies to generate a binary tree with 10 nodes. -i 50 tells the program to run 50 iterations and -d 0 to not display intermediate graphs. The result should look like this:

main -h will print out all options.

## 6 Submission and Assessment

The deadline for this assignment is midnight, Wed Dec 7. It is worth $10 \%$ of your final grade.
You should submit the assignment electronically using the Unix command
turnin cs372.8 point.icn graph.icn main.icn graphgen.icn gdraw.icn makefile README

The README file should give the members of your team. your code with anyone. If you need help with the assignment see the instructor or the TA.

