#### **CSc 372**

# Comparative Programming Languages

6: Haskell — Lists

Christian Collberg

collberg+372@gmail.com

Department of Computer Science
University of Arizona

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#### The List Datatype...

The cons operator ":" is right associative (it binds to the right, i.e.

SO

can be written without brackets as

#### The List Datatype

- All functional programming languages have the ConsList ADT built-in. It is called so because lists are constructed by "consing" (adding) an element on to the beginning of the list.
- Lists are defined recursively:
  - 1. The empty list [] is a list.
  - 2. An element x followed by a list L (x:L), is a list.
- Examples:

```
[ ]
2:[ ]
3:(2:[ ])
4:(3:(2:[ ]))
```

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#### The List Datatype...

Lists can also be written in a convenient bracket notation.

```
2:[] \Rightarrow [2]
3:(2:[]) \Rightarrow [3,2]
4:(3:(2:[]) \Rightarrow [4,3,2]
```

You can make lists-of-lists ([[1],[5]]), lists-of-lists-of-lists ([[[1,2]],[[3]]), etc.

### The List Datatype...

#### **Internal Representation**

More cons examples:

```
1:[2,3] \Rightarrow [1,2,3]

[1]:[[2],[3]] \Rightarrow [[1],[2],[3]]
```

Note that the elements of a list must be of the same type!

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Internally, Haskell lists are represented as linked cons-cells.

● A cons-cell is like a C struct with two pointer fields head and tail.

The head field points to the first element of the list, the tail field to the rest of the list.

■ The :-operator creates a new cons-cell (using malloc) and fills in the head and tail fields to point to the first element of the new list, and the rest of the list, respectively.

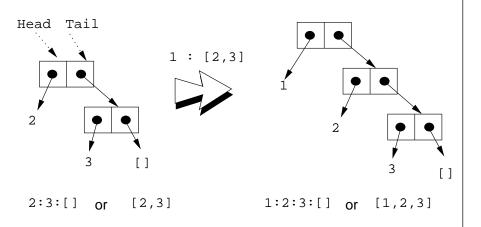
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# **Internal Representation...**

Example:

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# **Standard Operations on Lists**

#### head **and** tail

- The Standard Prelude has many built-in operations on lists.
- Two principal operators are used to take lists apart:
  - 1. head L returns the first element of L.
  - 2. tail L returns L without the first element.
- The cons operator ":" is closely related to head and tail:
  - 1. head  $(x:xs) \equiv x$
  - 2. tail  $(x:xs) \equiv xs$
- The cons operator ": " constructs new lists, head and tail take them apart.

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#### length and ++

- length xs Number of elements in the list xs.
- xs ++ ys − The elements of xs followed by the elements of ys.

#### Examples:

```
\Rightarrow 3
```

length [ ]  $\Rightarrow$  0

length [1,2,3]

 $[1,2] ++ [3,4] \Rightarrow [1,2,3,4]$ 

 $[1,2] ++ [] \Rightarrow [1,2]$  $[1] ++ [2,3] ++ [4] \Rightarrow [1,2,3]$ 

[1] ++ [2,3] ++ [4]  $\Rightarrow$  [1,2,3,4] length ([1]++[2,3])  $\Rightarrow$  3

[1] ++ [length [2,3]]  $\Rightarrow$  [1,2]

#### head and tail...

```
head [1,2,3] \Rightarrow 1

tail [1,2,3] \Rightarrow [2,3]

tail [1] \Rightarrow [] ([1] == 1:[])

head [] \Rightarrow ERROR

tail [] \Rightarrow ERROR

head (1:[2,3]) \Rightarrow 1

tail (1:[2,3]) \Rightarrow [2,3]

head (tail [1,2]) \Rightarrow [2,3]

head (tail [1]) \Rightarrow [2] \Rightarrow
```

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#### concat

concat xss – all of the lists in xss appended together.

concat 
$$[[1],[4,5],[6]] \Rightarrow [1,4,5,6]$$

Note that concat takes a list of lists as argument.

tail (map double (concat [[1],[3],[4]]))  $\Rightarrow$ 

head ([1,2] ++ [3,4])  $\Rightarrow$ 

head  $[1,2,3,4] \Rightarrow 1$ 

tail  $[2,6,8] \Rightarrow [6,8]$ 

tail (concat [[1],[3,4],[5]])  $\Rightarrow$ 

tail (map double [1,3,4])  $\Rightarrow$ 

tail  $[1,3,4,5] \Rightarrow [3,4,5]$ 

map f xs - list of values obtained by applying the function f to the values in xs.

map even [1,2,3]  $\Rightarrow$  [False,True,False] map square [1,2,3]  $\Rightarrow$  [1,4,9]

- Note that map takes a function as its first argument. A function which takes a function as an argument or delivers one as its result, is called a higher-order function.
- We will talk more about higher-order functions in future lectures.

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## **The String Type**

A Haskell string is a list of characters:

type String = [Char]

⇔ "Have a cow, man!"

- All list manipulation functions can be applied to strings.
- Note that " " == [].

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**Recursion Over Lists** 

#### **Recursion on the Tail**

- Compute the length of a list.
- This is called recursion on the tail.

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# **Map Function**

- Map a list of numbers to a new list of their absolute values.
- In the previous examples we returned an Int here we're mapping a list to a new list.
- This is called a map function.

## **Variable Naming Conventions**

- When we write functions over lists it's convenient to use a consistent variable naming convention. We let
  - x, y, z, ··· denote list elements.
  - xs, ys, zs, ... denote lists of elements.
  - xss, yss, zss, ... denote lists of lists of elements.

```
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```

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# **Map Function...**

```
> abslist []
[]
> abslist [1]
[1]
  abslist [1,-2]
[1,2]
```

#### **Recursion Over Two Lists**

listed xs ys returns True if two lists are equal.

```
True
> listeq [1] [1,2]
False
> listeq [1,2] [1,2]
True
```

False

**Recursion Over Two Lists...** 

> listeq [1] [2]

> listeq [1] [1]

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## **Append**

- append xs ys takes two lists as arguments and returns a new list, consisting of the elements of xs followed by the elements of ys.
- To do this recursively, we take xs apart on the way down into the recursion, and "attach" them to ys on the way up:

# Append...

```
> append [] []
[]
> append [1] []
[1]
> append [1] [2]
[1,2]
> append [1,2,3] [4,5,6]
[1,2,3,4,5,6]
```

# **Arithmetic Sequences**

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## **Arithmetic Sequences...**

Or, in English

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"m and k are the first two elements of the sequence. All consecutive pairs of elements have the same difference as m and k. No element is greater than n."

Or, in some other words,

"m and  ${\bf k}$  form a prototype for consecutive element pairs in the list."

Later in the course we will talk about infinite lists. Haskell has the capability to create infinite arithmetic sequences:

$$\begin{array}{lll} [3..] & \Rightarrow & [3,4,5,6,7,\cdots] \\ [4,3..] & \Rightarrow & [4,3,2,1,0,-1,-2,\cdots] \end{array}$$

## **Arithmetic Sequences**

Haskell provides a convenient notation for lists of numbers where the difference between consecutive numbers is constant.

$$[1..3] \Rightarrow [1,2,3]$$
  
 $[5..1] \Rightarrow []$ 

• A similar notation is used when the difference between consecutive elements is  $\neq 1$ : Examples:

```
    \begin{bmatrix}
      1,3..9 \\
      9,8..5 \\
      \end{bmatrix}
    \Rightarrow [1,3,5,7,9] 

    \Rightarrow [9,8,7,6,5] 

    \Rightarrow [9,8..11]
    \Rightarrow []
```

Or, in general:

$$[m,k..n] \Rightarrow$$
  
 $[m,m+(k-m)*1,m+(k-m)*2,\cdots,n]$ 

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#### **Summary**

- The bracketed list notation [1,2,3] is just an abbreviation for the list contructor notation 1:2:3:[].
- Lists can contain anything: integers, characters, tuples, other lists, but every list must contain elements of the same type only.
- :, ++, concat, and list comprehensions create lists.
- head and tail take lists apart.

# **Summary...**

- The notation [m..n] generates lists of integers from m to n.
- If the difference between consecutive integers is  $\neq 1$ , we use the slightly different notation [m,k..n]. The first two elements of the generated list are  ${\tt m}$  and  ${\tt k}$ . The remaining elements are as far appart as m and k.

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Homework

- Show the lists generated by the following Haskell list expressions.
- 1. [7..11]

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- 2. [11..7]
- 3. [3,6..12]
- 4. [12,9..2]

#### **Homework**

Which of the following are legal list constructions? First work out the answer in your head, then try it out with the hugs interpreter.

- 1. 1 : []
- 2. 1 : []: []
- 3. 1 : [1]
- 4. []: [1]
- 5. [1] : [1] : []

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#### **Homework**

- 1. Write a function getelmt xs n which returns the n:th element of a list of integers.
- 2. Write a function evenelmts xs which returns a new list consisting of the 0:th, 2:nd, 4:th, ... elements of an integer list xs.