CSc 372

Comparative Programming Languages

10: Haskell — Polymorphic Functions

Christian Collberg

collberg+372@gmail.com

Department of Computer Science
University of Arizona

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Polymorphic Functions

In many languages we can't write a generic sort routine, i.e. one that can sort arrays of integers as well as arrays of reals:

```
procedure Sort (
    var A : array of <type>;
    n : integer);
```

- In Haskell (and many other FP languages) we can write polymorphic ("many shapes") functions.
- Functions of polymorphic type are defined by using type variables in the signature:

```
length :: [a] -> Int
length s = ...
```

Polymorphic Functions...

length is a function from lists of elements of some (unspecified) type a, to integer. I.e. it doesn't matter if we're taking the length of a list of integers or a list of reals or strings, the algorithm is the same.

```
length [1,2,3] \Rightarrow 3 (list of Int) length ["Hi ", "there", "!"] \Rightarrow 3 (list of String length "Hi!" \Rightarrow 3 (list of Char)
```

Polymorphic Functions...

- We have already used a number of polymorphic functions that are defined in the standard prelude.
- head is a function from "lists-of-things" to "things":

```
head :: [a] -> a
```

tail is a function from lists of elements of some type, to a list of elements of the same type:

```
tail :: [a] -> [a]
```

cons "(:)" takes two arguments: an element of some type a and a list of elements of the same type. It returns a list of elements of type a:

```
(:) :: a -> [a] -> [a]
```

Polymorphic Functions...

- Note that head and tail always take a list as their argument. tail always returns a list, but head can return any type of object, including a list.
- Note that it is because of Haskell's strong typing that we can only create lists of the same type of element. If we tried to do

```
? 5 : [True]
```

the Haskell type checker would complain that we were consing an Int onto a list of Bools, while the type of ":" is

```
(:) :: a -> [a] -> [a]
```

Context Predicates

The remdups Function

Remember the remdups function:

```
remdups [1] \Rightarrow [1] remdups [1,2,1] \Rightarrow [1,2,1] remdups [1,2,1,1,2] \Rightarrow [1,2,2] remdups [1,1,1,2] \Rightarrow [1,2,1]
```

Algorithm in Haskell:

Context Predicates

- Obviously remdups should work for any list, not just lists of Ints. Removing duplicates from a list of strings is no different from removing duplicates from a list of integers.
- However, there's a complication. In order to remove duplicates from a list, we must be able to compare list elements for equality.
- The polymorphic type

is therefore a bit too general, since it would allow any type, even one for which equality is not defined.

Context Predicates...

Haskell uses context predicates to restrict polymorphic types:

```
remdups :: Eq [a] => [a] -> [a]
```

Now, remdups may only be applied to list of elements where the element type has == and \= defined.

■ Eq is called a type class. Ord is another useful type class. It is used to restrict the polymorphic type of a function to types for which the relational operators (<, <=, >, >=) have been defined.

Multiple Context Predicates

Consider the signum Function:

- signum can be applied to any type that is a number (hence the Num a predicate), and for which the relational operators are defined (Ord a).
- Without these restrictions, the polymorphic signum function could have been applied to lists, for example, which would not have made sense.

Conclusion

Summary...

- We want to define functions that are as reusable as possible.
 - 1. Polymophic functions are reusable because they can be applied to arguments of different types.
 - 2. Curried functions are reusable because they can be specialized; i.e. from a curried function f we can create a new function f' simply by "plugging in" values for some of the arguments, and leaving others undefined.

Summary

- A polymorphic function is defined using type variables in the signature. A type variable can represent an arbitrary type.
- All occurences of a particular type variable appearing in a type signature must represent the same type.
- An identifier will be treated as an operator symbol if it is enclosed in backquotes: " \ ".
- An operator symbol can be treaded as an identifier by enclosing it in parenthesis: (+).

Homework

Define a polymorphic function dup x which returns a tuple with the argument duplicated.

Example:

```
? dup 1
  (1,1)

? dup "Hello, me again!"
  ("Hello, me again!",
  "Hello, me again!")

? dup (dup 3.14)
  ((3.14,3.14), (3.14,3.14))
```

Homework

Define a polymorphic function copy n x which returns a list of n copies of x.

Example:

Homework

Let f be a function from Int to Int, i.e.

```
f:: Int -> Int. Define a function total f \times so that total f is the function which at value n gives the total f 0 + f 1 + \cdots + f n.
```

Example:

```
double x = 2*x
pow2 x = x^2
totDub = total double
totPow = total pow2
? totDub 5
    30
? totPow 5
    55
```