

CSc 372 — Comparative Programming Languages

9 : Haskell — Polymorphic Functions

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1 Polymorphic Functions

- In many languages we can't write a **generic** sort routine, i.e. one that can sort arrays of integers as well as arrays of reals:

```
procedure Sort (  
    var A : array of <type>;  
    n : integer);
```

- In Haskell (and many other FP languages) we can write **polymorphic** (“many shapes”) functions.
- Functions of polymorphic type are defined by using **type variables** in the signature:

```
length :: [a] -> Int  
length s = ...
```

2 Polymorphic Functions...

- `length` is a function from lists of elements of some (unspecified) type `a`, to integer. I.e. it doesn't matter if we're taking the length of a list of integers or a list of reals or strings, the algorithm is the same.

```
length [1,2,3]           => 3 (list of Int)  
length ["Hi ", "there", "!"] => 3 (list of String)  
length "Hi!"           => 3 (list of Char)
```

3 Polymorphic Functions...

- We have already used a number of polymorphic functions that are defined in the standard prelude.
- `head` is a function from “lists-of-things” to “things”:

```
head :: [a] -> a
```

- `tail` is a function from lists of elements of some type `a`, to a list of elements of the same type:

```
tail :: [a] -> [a]
```

- `cons "(:)"` takes two arguments: an element of some type `a` and a list of elements of the same type. It returns a list of elements of type `a`:

```
(:) :: a -> [a] -> [a]
```

4 Polymorphic Functions...

- Note that `head` and `tail` always take a list as their argument. `tail` always returns a list, but `head` can return any type of object, including a list.
- Note that it is because of Haskell's strong typing that we can only create lists of the same type of element. If we tried to do

```
? 5 : [True]
```

the Haskell type checker would complain that we were consing an `Int` onto a list of `Bools`, while the type of `"5"` is

```
(:) :: a -> [a] -> [a]
```

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Context Predicates

6 The `remdups` Function

- Remember the `remdups` function:

```
remdups [1]           => [1]
remdups [1,2,1]      => [1,2,1]
remdups [1,2,1,1,2] => [1,2,2]
remdups [1,1,1,2]   => [1,2,1]
```

- Algorithm in Haskell:

```
remdups :: [Int] -> [Int]
remdups x:y:xs =
  if x == y then
    remdups y:xs      <- case 1
  else
    x : remdups y:xs <- case 2
remdups xs = xs      <- case 3
```

7 Context Predicates

- Obviously `remdups` should work for any list, not just lists of `Ints`. Removing duplicates from a list of strings is no different from removing duplicates from a list of integers.
- However, there's a complication. In order to remove duplicates from a list, we must be able to compare list elements for equality.
- The polymorphic type

```
[a] -> [a]
```

is therefore a bit too general, since it would allow any type, even one for which equality is not defined.

8 Context Predicates...

- Haskell uses **context predicates** to restrict polymorphic types:

```
remdups :: Eq [a] => [a] -> [a]
```

Now, `remdups` may only be applied to list of elements where the element type has `==` and `\=` defined.

- `Eq` is called a **type class**. `Ord` is another useful type class. It is used to restrict the polymorphic type of a function to types for which the relational operators (`<`, `<=`, `>`, `>=`) have been defined.

9 Multiple Context Predicates

- Consider the `signum` Function:

```
signum :: (Num a, Ord a) => a -> Int
signum n | n == 0   = 0
          | n > 0   = 1
          | n < 0   = -1
```

- `signum` can be applied to any type that is a number (hence the `Num a` predicate), and for which the relational operators are defined (`Ord a`).
- Without these restrictions, the polymorphic `signum` function could have been applied to lists, for example, which would not have made sense.

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Conclusion

11 Summary...

- We want to define functions that are as **reusable** as possible.
 1. **Polymorphic** functions are reusable because they can be applied to arguments of different types.
 2. **Curried** functions are reusable because they can be **specialized**; i.e. from a curried function `f` we can create a new function `f'` simply by “plugging in” values for some of the arguments, and leaving others undefined.

12 Summary

- A polymorphic function is defined using **type variables** in the signature. A type variable can represent an **arbitrary** type.
- All occurrences of a particular type variable appearing in a type signature must represent the same type.
- An identifier will be treated as an operator symbol if it is enclosed in backquotes: ``.
- An operator symbol can be treated as an identifier by enclosing it in parenthesis: (+).

13 Homework

- Define a polymorphic function **dup x** which returns a tuple with the argument duplicated.

_____ Example: _____

```
? dup 1
(1,1)

? dup "Hello, me again!"
("Hello, me again!",
 "Hello, me again!")

? dup (dup 3.14)
((3.14,3.14), (3.14,3.14))
```

14 Homework

- Define a polymorphic function **copy n x** which returns a list of **n** copies of **x**.

_____ Example: _____

```
? copy 5 "five"
["five","five","five",
 "five","five"]

? copy 5 5
[5,5,5,5,5]

? copy 5 (dup 5)
[(5,5), (5,5), (5,5), (5,5), (5,5)]
```

15 Homework

- Let **f** be a function from **Int** to **Int**, i.e. **f :: Int -> Int**. Define a function **total f x** so that **total f** is the function which at value **n** gives the total **f 0 + f 1 + ... + f n**.

_____ Example: _____

```
double x = 2*x
pow2 x = x^2
totDub = total double
totPow = total pow2
? totDub 5
  30
? totPow 5
  55
```