# CSc 372

#### **Comparative Programming Languages**

12 : Haskell — Composing Functions

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# **Composing Functions**

We want to discover frequently occurring patterns of computation. These patterns are then made into (often higher-order) functions which can be specialized and combined. map f L and filter f L can be specialized and combined:

```
double :: [Int] -> [Int]
double xs = map ((*) 2) xs
```

```
positive :: [Int] -> [Int]
positive xs = filter ((<) 0) xs</pre>
```

```
doublePos xs = map ((*) 2) (filter ((<) 0) xs)
? doublePos [2,3,0,-1,5]
[4, 6, 10]</pre>
```

## Composing Functions...

- Functional composition is a kind of "glue" that is used to "stick" simple functions together to make more powerful ones.
- In mathematics the ring symbol (°) is used to compose functions:

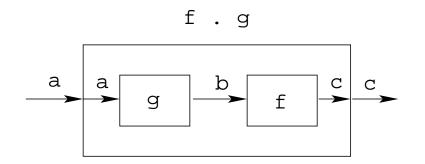
$$(f \circ g)(x) = f(g(x))$$

• In Haskell we use the dot (".") symbol:

infixr 9 .
(.) :: (b->c) -> (a->b) -> (a->c)
(f . g)(x) = f(g(x))

## Composing Functions...

(.) :: 
$$(b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow (a \rightarrow c)$$
  
(f . g)(x) = f(g(x))



- "." takes two functions f and g as arguments, and returns a new function h as result.
- g is a function of type a->b.
- f is a function of type b->c.
- h is a function of type a->c.
- (f.g)(x) is the same as z=g(x) followed by f(z).

# Composing Functions...

• We use functional composition to write functions more concisely. These definitions are equivalent:

doit x = f1 (f2 (f3 (f4 x)))
doit x = (f1 . f2 . f3 . f4) x
doit = f1 . f2 . f3 . f4

- The last form of doit is preferred. doit's arguments are implicit; it has the same parameters as the composition.
- doit can be used in higher-order functions (the second form is preferred):
- ? map (doit) xs
- ? map (f1 . f2 . f3 . f4) xs

# Example: Splitting Lines

- Assume that we have a function fill that splits a string into filled lines:
- fill :: string -> [string]
  fill s = splitLines (splitWords s)
  - fill first splits the string into words (using splitWords) and then into lines:

splitWords :: string -> [word]
splitLines :: [word] -> [line]

• We can rewrite fill using function composition:

fill = splitLines . splitWords

## Precedence & Associativity

I.e.

f.g.h.i.j = f.(g.(h.(i.j)))

Image: "." has higher precedence (binding power) than any other operator, except function application:

$$5 + f.g 6 = 5 + (f. (g 6))$$

I ... is associative:

f . (g . h) = (f . g) . h

"id" is "."'s identity element, i.e id . f = f = f . id:
 id :: a -> a
 id x = x

## The count Function

 Define a function count which counts the number of lists of length n in a list L:

```
count 2 [[1],[],[2,3],[4,5],[]] \Rightarrow 2
```

\_\_\_\_\_ Using recursion: \_\_\_\_\_

— Using functional composition: \_\_\_\_\_

count' n = length . filter (==n) . map length

## The count Function...

```
count' n = length . filter (==n) . map length
```

Note that

count' n xs = length (filter (==n) (map length xs))

### The init & last Functions

- last returns the last element of a list.
- init returns everything but the last element of a list.

\_\_\_\_\_ Definitions: \_\_\_\_\_

last = head . reverse

init = reverse . tail . reverse

\_\_\_\_\_ Simulations: \_\_\_\_\_

 $[1,2,3] \stackrel{\text{reverse}}{\Longrightarrow} [3,2,1] \stackrel{\text{head}}{\Longrightarrow} 3$ 

 $[1,2,3] \xrightarrow{\text{reverse}} [3,2,1] \xrightarrow{\text{tail}} [2,1] \xrightarrow{\text{reverse}} [1,2]$ 

## The any Function

• any p xs returns True if p x == True for some x in xs:

any ((==)0) 
$$[1,2,3,0,5] \Rightarrow$$
 True  
any ((==)0)  $[1,2,3,4] \Rightarrow$  False

\_ Using composition: \_\_\_\_\_

any p = or . map p  $[1,0,3]^{map} \xrightarrow{((==)0)} [False,True,False] \xrightarrow{or} True$ 

- Let's have another look at one simple (!) function, commaint.
- commaint works on strings, which are simply lists of characters.
- You are  $h \phi t$  now supposed to understand this!

From the commaint documentation: \_\_\_\_

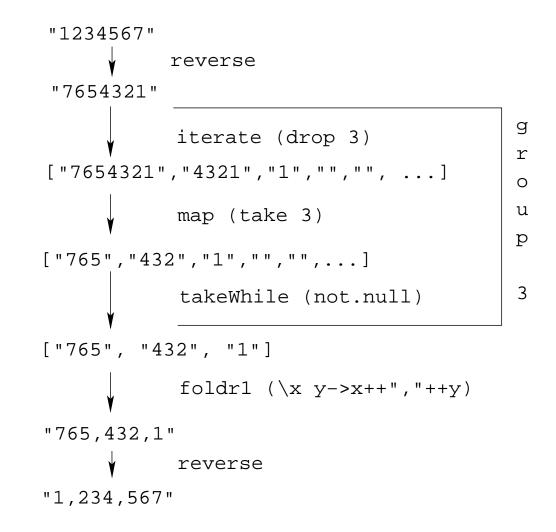
[commaint] takes a single string argument containing a sequence of digits, and outputs the same sequence with commas inserted after every group of three digits, ...

\_\_\_\_\_ Sample interaction: \_\_\_\_\_

? commaint "1234567"
 1,234,567

\_\_\_\_\_ commaint in Haskell: \_\_\_\_\_

```
commaint = reverse . foldr1 (\x y->x++","++y) .
    group 3 . reverse
    where group n = takeWhile (not.null) .
    map (take n).iterate (drop n)
```



# commaint = reverse . foldr1 (\x y->x++","++y) . group 3 . reverse where group n = takeWhile (not.null) . map (take n).iterate (drop n)

iterate (drop 3) s returns the infinite list of strings
 [s, drop 3 s, drop 3 (drop 3 s),
 drop 3 (drop 3 (drop 3 s)), ...]
 map (take n) xss shortens the lists in xss to n elements.

# commaint = reverse . foldr1 (\x y->x++","++y) . group 3 . reverse where group n = takeWhile (not.null) . map (take n).iterate (drop n)

- takeWhile (not.null) removes all empty strings from a list of strings.
- foldr1 (\x y->x++", "++y) s takes a list of strings s as input. It appends the strings together, inserting a comma in between each pair of strings.

# Lambda Expressions

- $(x y \rightarrow x + ", " + y)$  is called a lambda expression.
- Lambda expressions are simply a way of writing (short) functions inline. Syntax:

```
\land arguments -> expression
```

• Thus, commaint could just as well have been written as

```
commaint = ··· . foldr1 insert . ···
where group n = ···
insert x y = x++","++y
```

```
_ Examples: _____
```

squareAll xs = map ( $\langle x - \rangle x * x$ ) xs length = foldl' ( $\langle n - \rangle n+1$ ) 0

# Summary

- The built-in operator "." (pronounced "compose") takes two functions f and g as argument, and returns a new function h as result.
- The new function h = f . g combines the behavior of f and g: applying h to an argument a is the same as first applying g to a, and then applying f to this result.
- Operators can, of course, also be composed: ((+2).
   (\*3)) 3 will return 2 + (3 \* 3) = 11.

## Homework

- Write a function mid xs which returns the list xs without its first and last element.
  - use recursion
  - **2** use init, tail, and functional composition.
  - **③** use reverse, tail, and functional composition.
- ? mid  $[1,2,3,4,5] \Rightarrow [2,3,4]$
- ? mid []  $\Rightarrow$  ERROR
- ? mid [1]  $\Rightarrow$  ERROR
- ? mid [1,3]  $\Rightarrow$  []