## **CSc 520**

# **Principles of Programming Languages**

17: Haskell — Composing Functions

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# **Composing Functions...**

- Functional composition is a kind of "glue" that is used to "stick" simple functions together to make more powerful ones.
- In mathematics the ring symbol (○) is used to compose functions:

$$(f \circ g)(x) = f(g(x))$$

■ In Haskell we use the dot (".") symbol:

```
infixr 9 .
(.) :: (b->c) -> (a->b) -> (a->c)
(f . g)(x) = f(g(x))
```

# **Composing Functions**

We want to discover frequently occurring patterns of computation. These patterns are then made into (often higher-order) functions which can be specialized and combined. map f L and filter f L can be specialized and combined:

```
double :: [Int] -> [Int]
double xs = map ((*) 2) xs

positive :: [Int] -> [Int]
positive xs = filter ((<) 0) xs

doublePos xs = map ((*) 2) (filter ((<) 0) xs)
? doublePos [2,3,0,-1,5]
[4, 6, 10]</pre>
```

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# **Composing Functions...**

(.) :: 
$$(b->c) -> (a->b) -> (a->c)$$
  
(f. g)(x) = f(g(x))

f. g

- "." takes two functions f and g as arguments, and returns a new function h as result.
- g is a function of type a->b.
- f is a function of type b->c.
- h is a function of type a->c.
- (f.g)(x) is the same as z=g(x) followed by f(z).

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# **Composing Functions...**

• We use functional composition to write functions more concisely. These definitions are equivalent:

```
doit x = f1 (f2 (f3 (f4 x)))
doit x = (f1 . f2 . f3 . f4) x
doit = f1 . f2 . f3 . f4
```

- The last form of doit is preferred. doit's arguments are implicit; it has the same parameters as the composition.
- doit can be used in higher-order functions (the second form is preferred):

```
? map (doit) xs
? map (f1 . f2 . f3 . f4) xs
```

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# **Precedence & Associativity**

```
    "." is right associative. I.e.
    f.g.h.i.j = f.(g.(h.(i.j)))
```

2. "." has higher precedence (binding power) than any other operator, except function application:

```
5 + f.g 6 = 5 + (f. (g 6))
```

3. "." is associative:

```
f . (g . h) = (f . g) . h
```

4. "id" is "."'s identity element, i.e id . f = f = f
. id:
id :: a -> a

# **Example: Splitting Lines**

Assume that we have a function fill that splits a string into filled lines:

```
fill :: string -> [string]
fill s = splitLines (splitWords s)
```

fill first splits the string into words (using splitWords) and then into lines:

```
splitWords :: string -> [word]
splitLines :: [word] -> [line]
```

We can rewrite fill using function composition:

```
fill = splitLines . splitWords
```

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# The count Function

Define a function count which counts the number of lists of length n in a list L:

```
count 2 [[1],[],[2,3],[4,5],[]] \Rightarrow 2

Using recursion:
```

#### Using functional composition:

```
count' n = length . filter (==n) . map length
```

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id x = x

---

### The count Function...

ount' n = length . filter (==n) . map length

What does count ' do?

#### Note that

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```
count' n xs = length (filter (==n) (map length xs))

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```

# The any Function

- any p xs returns True if p x == True for some x in xs:
- any ((==)0) [1,2,3,0,5]  $\Rightarrow$  True any ((==)0) [1,2,3,4]  $\Rightarrow$  False

#### Using recursion:

any p = or . map p  $[1,0,3]^{\text{map}} \stackrel{((==)0)}{\Longrightarrow} [\text{False,True,False}] \stackrel{\text{or}}{\Longrightarrow} \text{True}$ 

### The init & last Functions

- last returns the last element of a list.
- init returns everything but the last element of a list.

#### Definitions:

```
last = head . reverse
```

#### Simulations:

$$[1,2,3]$$
 reverse  $[3,2,1]$   $\stackrel{\text{head}}{\Longrightarrow} 3$ 

$$[1,2,3]$$
 reverse  $[3,2,1]$   $\stackrel{\text{tail}}{\Longrightarrow}$   $[2,1]$  reverse  $[1,2]$ 

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## commaint Revisited...

- Let's have another look at one simple (!) function, commaint.
- commaint works on strings, which are simply lists of characters.
- You are ηρτ now supposed to understand this!

#### From the commaint documentation:

[commaint] takes a single string argument containing a sequence of digits, and outputs the same sequence with commas inserted after every group of three digits, ···

## commaint Revisited...

```
Sample interaction:
```

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#### commaint Revisited...

iterate (drop 3) s returns the infinite list of strings

```
[s, drop 3 s, drop 3 (drop 3 s),
    drop 3 (drop 3 (drop 3 s)), ...]
map (take n) xss shortens the lists in xss to n
elements.
```

#### commaint Revisited...

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#### commaint Revisited...

- takeWhile (not.null) removes all empty strings from a list of strings.
- foldr1 (\x y->x++","++y) s takes a list of strings s as input. It appends the strings together, inserting a comma in between each pair of strings.

# **Lambda Expressions**

- $(\x y->x++", "++y)$  is called a lambda expression.
- Lambda expressions are simply a way of writing (short) functions inline. Syntax:

```
\ arguments -> expression
```

● Thus, commaint could just as well have been written as

```
commaint = \cdots foldr1 insert . \cdots where group n = \cdots insert x y = x++","++y

Examples:

squareAll xs = map (\ x -> x * x) xs
```

squareAII xs = map  $(\langle x -> x ^* x)$  xs length = foldl'  $(\langle n -> n+1)$  0

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#### Homework

- Write a function mid xs which returns the list xs without its first and last element.
  - 1. use recursion
  - 2. use init, tail, and functional composition.
  - 3. use reverse, tail, and functional composition.

```
mid [1,2,3,4,5] \Rightarrow [2,3,4]
mid [] \Rightarrow ERROR
mid [1] \Rightarrow ERROR
mid [1] \Rightarrow []
```

# **Summary**

- The built-in operator " . " (pronounced "compose") takes two functions f and g as argument, and returns a new function h as result.
- The new function h = f . g combines the behavior of f and g: applying h to an argument a is the same as first applying g to a, and then applying f to this result.
- Operators can, of course, also be composed: ((+2). (\*3)) 3 will return 2 + (3 \* 3) = 11.

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