

CSc 520

Principles of Programming Languages

9: Scheme — Metacircular Interpretation

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Let Expressions

- A **let-expression** binds names to values:

```
(let ((name1 value1) (name2 value2) ...)  
    expression)
```

- The first argument to let is a list of (name value) pairs. The second argument is the expression to evaluate.

```
> (let ((a 3) (b 4) (square (lambda (x)(* x x)))  
      (plus +))  
    (sqrt (plus (square a) (square b))))
```

5.0

- Let-expressions can be nested:

```
> (let ((x 5) (c 4))  
    (let ((v (* 4 x))  
          (t (* 2 c)))  
      (+ v t)))
```

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Let Expressions...

- In this lecture I'm going to show how you can define Scheme by writing a **metacircular interpreter** for the language, i.e. an interpreter for Scheme written in Scheme.
- Before we can do that, we first need to learn a few more things about the language

Imperative Features

- Scheme is an **impure** functional language.
- I.e., Scheme has **imperative** features.
- I.e., in Scheme it is possible to program with **side-effects**.

`(set! var value)` Change the value of var to value.

`(set-car! var value)` Change the car-field of the cons-cell var to value.

`(set-cdr! var value)` Change the cdr-field of the cons-cell var to value.

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Dotted Pairs

- S-expressions are constructed using **dotted pairs**.
- It is implemented as a **struct** (called a **cons-cell**) consisting of two fields (the size of a machine word) called **car** and **cdr**.
- We can manipulate these fields directly:

```
> '(1 . 2)
(1 . 2)
> (cons "stacy's" "mom")
("stacy's" . "mom")
> '(1 . (2 . 3))
(1 2 . 3)
> (cons 1 2)
(1 . 2)
```

- Example:

```
> (let ((x 2) (l '(a b)))
  (set! x 3)
  (set-car! l '(c d))
  (set-cdr! l '(e))
  (display x) (newline)
  (display l) (newline))
3
((c d) e)
```

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Dotted Pairs...

- When the second part of a dotted pair (the cdr-field) is a list, and the innermost cdr-field is the empty list, we get a “normal” Scheme list:

```
> '(1 . ( ))
(1)
> '(1 . (2 . ( )))
(1 2)
> '(1 . (2 3))
(1 2 3)
```

Dotted Pairs...

- We can use `set-car!` and `set-cdr!` to manipulate the fields of a `cons-cell` directly:

```
> (define x '(1 . 2))
> (set-car! x 'a)
> x
(a . 2)
> (set-cdr! x '(2 3))
> x
(a 2 3)
```

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Loops

Scheme's "for-loop" `do` takes these arguments:

1. A list of triples (*var init update*) which declares a variable *var*, with an initial value *init*, and which gets updated using the expression *update*, on each iteration;
2. A pair (*termination_cond return_value*) which gives the termination condition and return value of the loop; and
3. a loop body:

```
(do ((var1 init1 update1)
     (var12 init2 update2)
     ...
     )
     (termination_cond return_value)
     loop_body)
```

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Dotted Pairs...

- `(cons A B)` can be thought of as first creating a `cons-cell` on the heap (using `malloc`, for example), and then setting the `car` and `cdr` fields to `A` and `B`, respectively:

```
> (define x (cons 0 0))
> x
(0 . 0)
> (set-car! x '1)
> (set-cdr! x '())
> x
(1)
```

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Loops...

- Sum the numbers 1 to 4, printing out intermediate results:

```
> (do ((i 1 (+ i 1))
       (sum 0 (+ sum i)))
      ((= i 5) sum)
      (display sum)
      (newline)
      )
0
1
3
6
10
```

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Association Lists

- Association lists are simply lists of *key-value* pairs that can be searched sequentially:

```
> (assoc 'bob '((bob 22) (joe 32) (bob 3)))
(bob 22)
```

- The list is searched the list from beginning to end, returning the first pair with a matching key:

(assoc *key* *alist*) Search for *key*; compare using equal?.

(assq *key* *alist*) Search for *key*; compare using eq?.

(assv *key* *alist*) Search for *key*; compare using eqv?.

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Association Lists...

- We can actually have more than one value:

```
> (assoc 'bob '((bob 5 male)
                  (jane 32 'female)))
(bob 5 male)
```

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Association Lists...

```
> (define e '((a 1) (b 2) (c 3)))
> (assq 'a e)
(a 1)
> (assq 'b e)
(b 2)
> (assq 'd e)
#f
> (assq (list 'a) '(((a)) ((b)) ((c))))
#f
> (assoc (list 'a) '(((a)) ((b)) ((c))))
((a))
> (assv 5 '((2 3) (5 7) (11 13)))
(5 7)
```

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Apply

- Apply returns the result of applying its first argument to its second argument.

```
> (apply + '(6 7))
13
> (apply max '(2 5 1 7))
7
```

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Eval

- `(eval arg)` evaluates its argument.

```
> (eval '(+ 4 5))  
9  
> (eval '(cons 'a '(b c))) (a b c)
```

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Programs as Data

- Scheme is **homoiconic**, self-representing, i.e. programs and data are both represented the same (as S-expressions).
- This allows us to write programs that generate programs - useful in AI, for example.

```
> (define x 'car)  
> (define y ''(a b c))  
> (define p (list x y))  
> p  
(car '(a b c))  
> (eval p)  
a
```

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Eval...

- eval and quote are each other's inverses:

```
> (eval ''(+ 4 5))  
(+ 4 5)  
> (eval (eval ''(+ 4 5)))  
9  
> (eval (eval (eval ''''(+ 4 5))))  
9
```

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Evaluation Order

- So far, we have said that to evaluate an expression `(op arg1 arg2 arg3)` we first evaluate the arguments, then apply the operator `op` to the resulting values.
- This is known as **applicative-order** evaluation.
- Example:

```
(define (double x) (* x x))  
  
> (double (* 3 4))  
⇒ (double 12)  
⇒ (+ 12 12)  
⇒ 24
```

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Evaluation Order...

- This is not the only possible order of evaluation
- In **normal-order** evaluation parameters to a function are always passed unevaluated.
- This sometimes leads to extra work:

```
(define (double x) (* x x))

> (double (* 3 4))
⇒ (+ (* 3 4) (* 3 4))
⇒ (+ 12 (* 3 4))
⇒ (+ 12 12)
⇒ 24
```

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Evaluation Order...

- Ordinary Scheme functions (such as +, car, etc) use applicative-order evaluation.
- Some **special forms** (cond, if, etc) must use normal order since they need to consume their arguments unevaluated:

```
> (if #t (display 5) (display 6))
5
> (cond (#f (display 5))
         (#f (display 6))
         (#t (display 7)))
```

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Evaluation Order...

- Applicative-order can sometimes also lead to more work than normal-order:

```
(define (switch x a b c)
  (cond
    ((< x 0) a)
    ((= x 0) b)
    ((> x 0) c)))

> (switch -1 (+ 1 2) (+ 2 3) (+ 3 4))
```

- Here, applicative-order evaluates all the arguments, although only one value will ever be needed.

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A Metacircular Interpreter

- One way to define the semantics of a language (the effects that programs written in the language will have), is to write a **metacircular interpreter**.
- I.e, we define the language by writing an interpreter for it, in the language itself.
- A metacircular interpreter for Scheme consists of two mutually recursive functions, mEval and mApply:

```
(define (mEval Expr)
  ...
)
(define (mApply Op Args)
  ...
)
```

A Metacircular Interpreter...

- We want to be able to call our interpreter like this:

```
> (mEval (+ 1 2))  
3  
> (mEval (+ 1 (* 3 4)))  
13  
> (mEval (quote (2 3)))  
(2 3)  
> (mEval (car (quote (1 2))))  
1
```

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A Metacircular Interpreter...

```
> (mEval (cdr (quote (1 2))))  
(2)  
> (mEval (cons (quote 5) (quote (1 2))))  
(5 1 2)  
> (mEval (null? (quote (1 2))))  
#f  
> (mEval (null? (quote ())))  
#t  
> (mEval (if (eq? 1 1) 5 6))  
5
```

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A Metacircular Interpreter...

- mEval handles **primitive special forms** (lambda, if, const, define, quote, etc), itself.
- Note that, for these forms, we must use normal-order evaluation.
- For other expressions, mEval evaluates all arguments and calls mApply to perform the required operation:

A Metacircular Interpreter...

```
(define (mEval Expr)  
  (cond  
    [(null? Expr) '()]  
    [(number? Expr) Expr]  
    [(eq? (car Expr) 'if)  
     (mEvalIf (cadr Expr)  
              (caddr Expr)  
              (caddar Expr))]  
    [(eq? (car Expr) 'quote) (cadr Expr)]  
    [else (mApply (car Expr)  
                  (mEvalList (cdr Expr)))]  
    ))
```

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A Metacircular Interpreter...

- mApply checks if the operation is one of the builtin primitive ones, and if so performs the required operation:

```
(define (mApply Op Args)
  (case Op
    [(car) (caar Args)]
    [(cdr) (cdar Args)]
    [(cons) (cons (car Args) (cadr Args))]
    [(eq?) (eq? (car Args) (cadr Args))]
    [(null?) (null? (car Args))]
    [(+) (+ (car Args) (cadr Args))]
    [(*) (* (car Args) (cadr Args))])
  )
)
```

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A Metacircular Interpreter...

- Note that this little interpreter lacks many of Scheme's functions.
- We don't have symbols, lambda, define.
- We can't define or invoke user-defined functions.
- There are no way to define or lookup variables, local or global. To do that, mEval and mApply pass around environments (association lists) of variable/value pairs.

A Metacircular Interpreter...

- Some auxiliary functions:

```
(define (mEvalIf b t e)
  (if (mEval b) (mEval t) (mEval e)))
)

(define (mEvalList List)
  (cond
    [(null? List) '()]
    [else (cons (mEval (car List))
                (mEvalList (cdr List)))]))
)
```

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Readings and References

- Read Scott, pp. 592–606, 609-610

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