

## Software Similarity Analysis

(c) April 28, 2011 Christian Collberg

## Clone detection

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- Problem during maintenance - all copies of bugs need to be fixed.


## Clone detection

- Detection phase: locating similar pieces of code in a program.



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- Detection phase: locating similar pieces of code in a program.
- Abstraction phase: clones are extracted out into functions.



## Clone detection algorithm - Finding Clones

Detect ( $P$, threshold, minsize):
(1) Build a representation rep of $P$ from which it is convenient to find clone pairs. Collect code pairs that are sufficiently similar and sufficiently large to warrent their own abstraction:

```
res}\leftarrow
rep}\leftarrow\mathrm{ convenient representation of P
for every pair of code segments f,g\inrep,f}\not=g\mathrm{ do
    if similarity(f,g) > threshold &&
            size}(f)\geq\mathrm{ minsize && size (g) }\\mathrm{ minsize then
            res}\leftarrowres\cup\langlef,g
```


## Clone detection algorithm — Replace Clones

Detect ( $P$, threshold, minsize):
(2) Break out the code-pairs found in the previous step into their own function and replace them with parameterized calls to this function:

```
for every pair of code segments f,g\inres do
    h(r)\leftarrow a parameterized version of f and g
    P\leftarrowP\cuph(r)
    replace f with a call to h(r1) and g with h(r r)
```

(3) Return res, $P$

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- The code becomes naturally "obfuscated" because of the specialization process.
- The programmer renames variables and replace literals with new values in the copied code.
- More complex changes are unusual.


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- Skype binary was protected by adding several hundred hash functions.
- Could a clone dector have found them?


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- Fishing code out of the trash can.
- Nabbing code off the printer.
- Outsource the assignments to an unscrupulous third party ("programming-mills").


## Plagiarism detection

- Make pair-wise comparisons between all the programs handed in by the students:



## Plagiarism detection - Algorithm

Detect ( $U$, threshold):

```
res}\leftarrow
for each pair of programs f,g do
        sim}\leftarrow similarity (f,g
        if sim> threshold then
        res }\leftarrowres\cup\langlef,g, sim
res \leftarrowres sorted on similarity
return res
```


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- Renaming windowSize to sizeOfWindow - OK.
- Renaming windowSize to x93 - not OK.
- Replace a while-loop with a for-loop - OK.
- Unroll the for-loop - not OK.



## ssEFM: AST-based clone detection

Look for clones in this program:

$$
(5+(a+b)) *(7+(c+9))
$$

Parse and build an AST S:


## An inefficient clone detector. . .

- Construct all tree patterns.


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- Construct all tree patterns.
- A tree pattern is a subtree of $S$ where one or more subtrees have been replaced with a wildcard.
- We'll color the ASTs themselves blue and the tree patterns pink.


## Some of the tree patterns



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- What's a clone in the context of an AST?
- Simply a tree pattern for which there's more than one match!
- Which patterns would make a good clone?
(1) has a large number of nodes
(2) occurs a large number of times in the AST
(3) has few holes


## Which patterns would make good clones?

- This pattern seems like it might make a good choice



## Which patterns would make good clones?

- This pattern seems like it might make a good choice

- It matches two large subtrees of $S$ :



## Extract clones!

- Now you can extract the clones and turn them into macros:

$$
\begin{aligned}
& \text { \#define } \operatorname{CLONE}(x, y, z)((x)+((y)+(z))) \\
& \text { CLONE }(5, a, b) * \operatorname{CLONE}(7, c, 9)
\end{aligned}
$$

## A slow algorithm. . .

- Build a clone table, a mapping from each pattern to the locations in $S$ where it occurs:


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- Build a clone table, a mapping from each pattern to the locations in $S$ where it occurs:
- Sort the table with largest patterns, most number of occurrences, fewest number of holes first!



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- Step 1:



## Step 2-3

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- After two more steps of specialization, we're done:

- They found this clone 10 times over some Java classes:

$$
\begin{gathered}
\text { for (int } \left.i=0 ; i<?_{1} ; i++\right) \\
\text { if }\left(?_{2}[i] \quad!=?_{3}[i]\right) \\
\text { return false; }
\end{gathered}
$$

- The strength of the algorithm is that it allows structural matching: holes can accept any subtree.


## Graph-based analysis <br> p. 635

## Programs are graphs!

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- Inheritance graphs!
- Can program similarity be computed over graph representations of programs?


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- Sub-graph isomorphism is NP-complete.
- Fortunately, graphs computed from programs are not general graphs.
- Control-flow graphs will not be arbitrarily large.
- Call-graphs tend to be very sparse.
- Heuristics can be very effective in approximating subgraph isomorphism.


# Algorithm ssKH 

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PDG-based clone detection


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- The nodes of a PDF are the statements of a function.
- There's an edge $m \rightarrow n$ if
(1) $n$ is data-dependent on $m$, or
(2) $n$ is control-dependent on $m$.
- Semantics-preserving reordering of the statements of a function won't affect the graph.


## Program Dependence Graph

$$
\begin{aligned}
& S_{0}: \text { int } \mathrm{k}=0 ; \\
& S_{1}: \text { int } \mathrm{s}=1 ; \\
& S_{2}: \text { while }(\mathrm{k}<\mathrm{w}) \text { \{ } \\
& S_{3}: \quad \text { if }(\mathrm{x}[\mathrm{k}]==1) \\
& S_{4}: \quad \mathrm{R}=(\mathrm{s} * \mathrm{y}) \% \mathrm{n} ; \\
& S_{5}: \quad \text { else } \\
& S_{6}: \\
& S_{7}: \quad \mathrm{s}=\mathrm{R}=\mathrm{s} ; \mathrm{R} \% \mathrm{n} ; \\
& S_{8}: \\
& \quad \mathrm{k}=\mathrm{k}+1 ;
\end{aligned}
$$

## Program Dependence Graph



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- Two nodes are matching if they have the same syntactic structure.
- Repeat until no more nodes can be added to the slice.


## A (contrived) example

$$
\begin{aligned}
& a_{1}: \mathrm{a}=\mathrm{g}(8) \text {; } \\
& b_{1}: \mathrm{b}=\mathrm{z} * 3 \text {; } \\
& a_{2} \text { : while (a<10) } \\
& a_{3}: a=f(a) ; \\
& b_{2} \text { : while (b<20) } \\
& b_{3}: b=f(b) ; \\
& a_{4} \text { : if ( } a==10 \text { ) \{ } \\
& a_{5}: ~ p r i n t f(" f \circ o \backslash n ") ; \\
& a_{6} \text { : } \mathrm{x}=\mathrm{x}+2 \text {; } \\
& \text { \} } \\
& b_{4} \text { : if }(b==20) \text { \{ } \\
& b_{5} \text { : printf("bar\n"); } \\
& b_{6} \text { : } y=y+2 \text {; } \\
& b_{7}: \operatorname{printf}(" b a z \backslash n ") \text {; } \\
& \text { \} }
\end{aligned}
$$

- Two similar pieces of code have been intertwined within the same function.


## A (contrived) example



## Algorithm: Step 1-3.

- $a_{4}$ and $b_{4}$ match. Add them to the slice.


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- $a_{3}$ and $b_{3}$ match, too. Add them to the slice.
- Add $a_{2}$ and $b_{2}$ to the slice since they match and are predecessors of $a_{3}$ and $b_{3}$.


## The PDF after Step 3



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- $a_{5} / b_{5}$ and $a_{6} / b_{6}$ really should belong to the clone!
- But, backwards slice won't include them.
- So, slice forward one step from any predicate in an if- and while-statement.


## The PDG after Step 4



## The extracted clone

$$
\begin{aligned}
& \text { \#define CLONE (x, c,d,s,p,y) \} } \\
{\text { while ( } x<c \text { ) } x=f(x) \text {; } \backslash} \\
{\text { if ( } x==d \text { ) \{ }} \\
{\text { printf(s); }} \\
{y=y+2 \text {; } \backslash} \\
{\mathrm{p}=1 ;\} \backslash} \\
{\text { else } p=0 \text {; }} \\
{\mathrm{a}=\mathrm{g}(8) \text {; }} \\
{\mathrm{b}=\mathrm{z} * 3 \text {; }} \\
{\operatorname{CLONE}(a, 10,10, " f o o \backslash n ", p, x)} \\
{\text { CLONE (b, 20, 20, "bar } \backslash \mathrm{n} ", \mathrm{p}, \mathrm{y} \text { ) }} \\
{\text { if (p) printf("baz\n"); }}
\end{aligned}
$$

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- This algorithm handles
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- clones where statements have been reordered,
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- Depressing performance numbers. A 11,540 line C program takes 1 hour and 34 minutes to process.


PDG-based plagiarism detection

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## ssLCHY: PDG-based plagiarism detection

- Uses PDGs, but for plagiarism detection.
- Uses a general-purpose subgraph isomorphism algorithm.
- Uses a preprocessing step to weed out unlikely plagiarism candidates.


## Plagiarised PDGs?

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## Plagiarised PDGs?

- What does it mean for one PDG to be considered a plagiarised version of another?
- We expect some manner of obfuscation of the code equality is too strong!
- The two PDGs should be $\gamma$-isomorphic.
- Set $\gamma=0.9$, ("overhauling (without errors) $10 \%$ of a PDG of reasonable size is almost equivalent to rewriting the code.")


## Common Subgraphs

## Definition

Common subgraphs Let $G, G_{1}$, and $G_{2}$ be graphs. $G$ is a common subgraph of $G_{1}$ and $G_{2}$ if there exists subgraph isomorphisms from $G$ to $G_{1}$ and from $G$ to $G_{2}$.
$G$ is the maximal common subgraph of two graphs $G_{1}$ and $G_{2}$ $\left(G=\operatorname{mcs}\left(G_{1}, G_{2}\right)\right)$ if $G$ is a common subgraph of $G_{1}$ and $G_{2}$ and there exists no other common subgraph $G^{\prime}$ of $G_{1}$ and $G_{2}$ that has more nodes than $G$.

## Common Subgraphs - Example

- The colored nodes induce a maximal common subgraph of $G_{1}$ and $G_{2}$ of four nodes:




## Graph similarity and containment

## Definition

Graph similarity and containment Let $|G|$ be the number of nodes in $G$. The similarity $\left(G_{1}, G_{2}\right)$ of $G_{1}$ and $G_{2}$ is defined as

$$
\operatorname{similarity}\left(G_{1}, G_{2}\right)=\frac{\left|\operatorname{mcs}\left(G_{1}, G_{2}\right)\right|}{\max \left(\left|G_{1}\right|,\left|G_{2}\right|\right)}
$$

The containment $\left(G_{1}, G_{2}\right)$ of $G_{1}$ within $G_{2}$ is defined as

$$
\operatorname{containment}\left(G_{1}, G_{2}\right)=\frac{\left|m c s\left(G_{1}, G_{2}\right)\right|}{\left|G_{1}\right|}
$$

We say that $G_{1}$ is $\gamma$-isomorphic to $G_{2}$ if

$$
\operatorname{containment}\left(G_{1}, G_{2}\right) \geq \gamma, \gamma \in(0,1] .
$$

## Graph similarity and containment - Example




- $\operatorname{similarity}\left(G_{1}, G_{2}\right)=\frac{4}{7}$ and


## Graph similarity and containment - Example




- $\operatorname{similarity}\left(G_{1}, G_{2}\right)=\frac{4}{7}$ and
- containment $\left(G_{1}, G_{2}\right)=\frac{4}{6}$.


## Filtering step

- Subgraph isomorphism testing is expensive - prune out $\frac{9}{10}$ of all program pairs from consideration:
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(3) remove $\left(g, g^{\prime}\right)$ if $\dot{\mathcal{L}}$ the frequency of their different node types are too different.
- For example, if $g$ consists solely of function call nodes and $g^{\prime}$ consists solely of nodes representing arithmetic operations, $\Rightarrow$ unlikely related.


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(1) statement reordering,
(2) variable renaming,
(3) replacing while-loops by for-loops,
(4) flipping the order of branches in if-statements.
- The PDG is affected by
(1) inlining and outlining
(2) add bogus dependencies to introduce spurious edges

