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# Principles of Programming Languages

Lecture 06

*Parameters*

# Parameter Passing Modes

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- Definitional Modes (call time binding)
  - Call as constant CAC
  - Call by reference CBR
- Copying Modes (call time copying)
  - Call by value CBV
  - Call by copy CBC
    - ◆ Copy-in/copy-out
  - Call by value-result CBVR
- Delay Modes (reference time copying)
  - Call by text CBT
  - Call by name CBN
  - Call by need
    - ◆ R-value CBNeed-R
    - ◆ L-Value CBNeed-L

# Example Program

---

```
{ local i,j
  local a[1..12]
  proc P( X , Y )
  { local j
    j = 2
    i = i + 1
    print X
    X = X + 2
    print Y
    i--; print Y
  }
  a[1]=1; a[2]=2; ... ; a[12]=12;
  i = 1
  j = 3
  P( i , a[i*j] )
  print i
  print a[9]
```

# Program Execution Sequence

---

```
i = 1
```

```
j = 3
```

```
P( i , a[i*j] )
```

```
    X ,    Y
```

```
    j = 2
```

```
    // this j is local
```

```
    i = i + 1
```

```
    print X
```

```
    X = X + 2
```

```
    print Y
```

```
    i--; print Y
```

```
print i
```

```
print a[9]
```

# Call by text (macrosubstitution)

```
i = 1
```

```
j = 3
```

```
P( i , a[i*j] )
```

```
    X ,    Y
```

```
j = 2
```

```
i = i + 1
```

```
print X
```

```
X = X + 2
```

```
print Y
```

```
i--; print Y
```

```
print i
```

```
print a[9]
```

```
rewrite proc body
```

```
X -> i    Y -> a[i*j]
```

```
j = 2 // j==2
```

```
i=i+1 // i==2
```

```
print i 2
```

```
i = i+2 //i==4
```

```
print a[i*j] //a[4*2]8
```

```
i--; print a[i*j] 6
```

```
print i 3
```

```
print a[9] 9
```

# Call by name (copy rule)

```
i = 1
```

```
j = 3
```

```
P( i , a[i*j] )
```

```
    X ,    Y
```

```
j = 2
```

```
i = i + 1
```

```
print X
```

```
X = X + 2
```

```
print Y
```

```
i--; print Y
```

```
print i
```

```
print a[9]
```

*Rename locals j->j' & rewrite*

```
X -> i    Y -> a[i*j]
```

```
j = 2 //j'==2    j==3
```

```
i=i+1 //i == 2
```

```
print i           2
```

```
i = i+2 //i==4
```

```
print a[i*j]//a[4*3] 12
```

```
i--; print a[i*j]   9 !
```

```
print i           3
```

```
print a[9]       9
```

# Algol 60 “Copy Rule”

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- **4.7.3.2.** Name replacement (call by name)  
Any formal parameter not quoted in the **value** list is replaced, throughout the procedure body, by the corresponding actual parameter . . . Possible conflicts between identifiers inserted through this process and other identifiers already present within the procedure body will be avoided by suitable systematic changes of the formal or local identifiers involved . . . Finally the procedure body, modified as above, is inserted in place of the procedure statement [the call] and executed . . .
  - Report on the Algorithmic Language ALGOL 60,  
*CACM*, May 1960

# Algol 60 “Copy Rule” (cont.)

---

```
integer procedure f(x);
```

```
  integer x;
```

```
  begin integer y;
```

```
    y := 1;
```

```
    f := x + y;
```

```
  end;
```

```
begin integer y, w;
```

```
  y := 2; w := 10;
```

```
  w := f(y + w + 1);
```

```
end;
```

```
begin integer y, w;
```

```
  y := 2; w := 10;
```

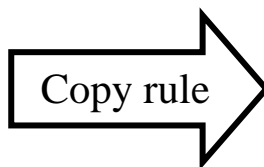
```
  begin integer z;
```

```
    z := 1;
```

```
    w := (y + w + 1) + z;
```

```
  end;
```

```
end;
```





# Algol 60 “Copy Rule” (cont.): Thunks

- *thunk*: a 0-arg. Procedure encapsulating actual argument plus environment of caller, called at site of each formal.
- Used to implement CBN and delayed evaluation in general

```
integer procedure f(x);
  integer x;
  begin integer y;
    y := 1;
    f := x + y;
  end;
begin integer y, w;
  y := 2; w := 10;
  w := f(y + w + 1);
end;
```

```
int function f(int x);
  { int y;
    y = 1;
    f = *x() + y;
  }
{ int y,w;
int& function x()
{int t=y+w+1;return &t;}
  y = 2; w = 10;
  w = f(y+w+1);
}
```

# Call by name—implemented by thunk

```
i = 1
j = 3
P( i , a[i*j] )
```

```
    X ,    Y
j = 2
i = i + 1
print X
X = X + 2
print Y
i--; print Y
print i
print a[9]
```

- *thunk*: 0-ary function encapsulating argument text

```
int& X(){return &i}
int& Y(){return &a[i*j]}
j = 2 // j'==2  j==3
i=i+1 // i == 2
print *X()           2
X()=*X()+2 //i==4
print *Y()
//a[i*j]==a[4*3]    12
i--; print *Y()     9 !
print i             3
print a[9]         9
```

# Call by reference

```
i = 1
j = 3
P( i , a[i*j] )
```

```
    X ,    Y
j = 2
i = i + 1
print X
X = X + 2
print Y
i--; print Y
```

```
print i
print a[9]
```

*aliased*

```
lval(X) == lval(i)
```

```
lval(Y) == lval(a[1*3])
```

```
j = 2 // j'==2   j==3
```

```
i=i+1 // i== 2
```

```
print i 2
```

```
i = i+2 // i==4
```

```
print a[1*3] 3
```

```
i--; print a[1*3] 3
```

```
print i 3
```

```
print a[9] 9
```

# Call by value (copy-in)

```
i = 1
```

```
j = 3
```

```
P( i , a[i*j] )
```

```
    X ,    Y
```

```
j = 2
```

```
i = i + 1
```

```
print X
```

```
X = X + 2
```

```
print Y
```

```
i--; print Y
```

```
print i
```

```
print a[9]
```

```
X = i          //X==1
```

```
Y = a[i*j]) //Y== a[1*3]
```

```
j = 2 //j'==2   j==3
```

```
i=i+1 //i == 2
```

```
print X 1
```

```
X = X+2 //i==2  X==3
```

```
print Y 3
```

```
i--; print Y 3
```

```
print i 1
```

```
print a[9] 9
```

# Call by value–result (Algol W)

```
i = 1
j = 3
P( i , a[i*j] )
```

```
    X ,    Y
j = 2
i = i + 1
print X
X = X + 2
print Y
i--; print Y
```

```
print i
print a[9]
```

```
X = i
Y = a[i*j] // Y == a[1*3]
j = 2 // j' == 2   j == 3
i = i + 1 // i == 2
print X 1
X = X + 2 // i == 2   X == 3
print Y 3
i--; print Y 3
```

*Use names of actuals for copy-out*

```
i = X // i == 3
a[i*j] = Y // a[3*3] == 3
print i 3
print a[9] 3
```

# Call by copy (copy-in/copy-out)

```
i = 1
j = 3
P( i , a[i*j] )
```

```
    X ,    Y
j = 2
i = i + 1
print X
X = X + 2
print Y
i--; print Y
```

```
print i
print a[9]
```

```
px=lvalue(i)      X=*px
py=lvalue(a[1*3]) Y=*py
j = 2 // j'==2   j==3
```

```
i=i+1 // i == 2
print X                                1
X = X+2 //i==2 X==3
print Y                                3
i--; print Y                            3
```

*Use original lvals for copy-out*

```
*px = X //i==3
*py = Y //a[3]==3
print i                                3
print a[9]                              9
```

# Call by need, r-value (“normal”, lazy)

```
i = 1
j = 3
P( i , a[i*j] )
```

```
    X ,    Y
j = 2
i = i + 1
print X
X = X + 2
print Y
i--; print Y
```

```
print i
print a[9]
```

- Use *think once* on 1<sup>st</sup> ref to assign local; then use local

```
int& X(){return &i}
int& Y(){return &a[i*j]}
```

```
j = 2 // j'==2   j==3
i=i+1 // i == 2
print X = *X()           2
    //X==2
X = X+2 //i==2   X==4
print Y = *Y()
    //Y==a[i*j]==a[2*3]   6
i--; print Y             6
print i                 1
print a[9]              9
```

# Call by need, l-value

```
i = 1
j = 3
P( i , a[i*j] )
```

```
    X ,    Y
j = 2
i = i + 1
print X
X = X + 2
print Y
i--; print Y
```

```
print i
print a[9]
```

- At 1<sup>st</sup> ref, alias actual lval to formal

```
int& X(){return &i}
int& Y(){return &a[i*j]}
j = 2 // j'==2 j==3
i=i+1 // i == 2
lval(X) == X() // X aliases i
print X // X==2 2
X = X+2 // i==4 X==4
lval(Y) == Y() // Y aliases a[4*3]
print Y
// Y==a[12]} 12
i--; print Y 12
print i 3
print a[9] 9
```



# Call by Name vs. Call by Need

---

- Assume  $x$  is the formal and  $e$  the corresponding actual expression
- CBN
  - Delays evaluation of arguments past call until a reference to the formal
  - Re-evaluates argument  $e$  on each reference to  $x$  *in environment of caller*
  - No local variable  $x$  is allocated
  - Implemented by call to thunk
- CB Need
  - Delays evaluation of arguments past call until a reference to the formal
  - Evaluates  $e$  on 1<sup>st</sup> reference *in environment of caller* & loads local variable  $x$ ; no re-evaluation: subsequent references use local  $x$
  - Implemented by call to “memoized thunk”

# Call by constant

```
i = 1
```

```
j = 3
```

```
P( i , a[i*j] )
```

```
    X ,    Y
```

```
j = 2
```

```
i = i + 1
```

```
print X
```

```
X = X + 2
```

```
print Y
```

```
i--; print Y
```

```
print i
```

```
print a[9]
```

```
const X = i
```

```
const Y = a[1*3]
```

```
j = 2 // j'==2    j==3
```

```
i=i+1 // i == 2
```

```
print X 1
```

```
X = X+2 error
```

```
print Y (3)
```

```
i--; print Y (3)
```

```
print i (1)
```

```
print a[9] (9)
```

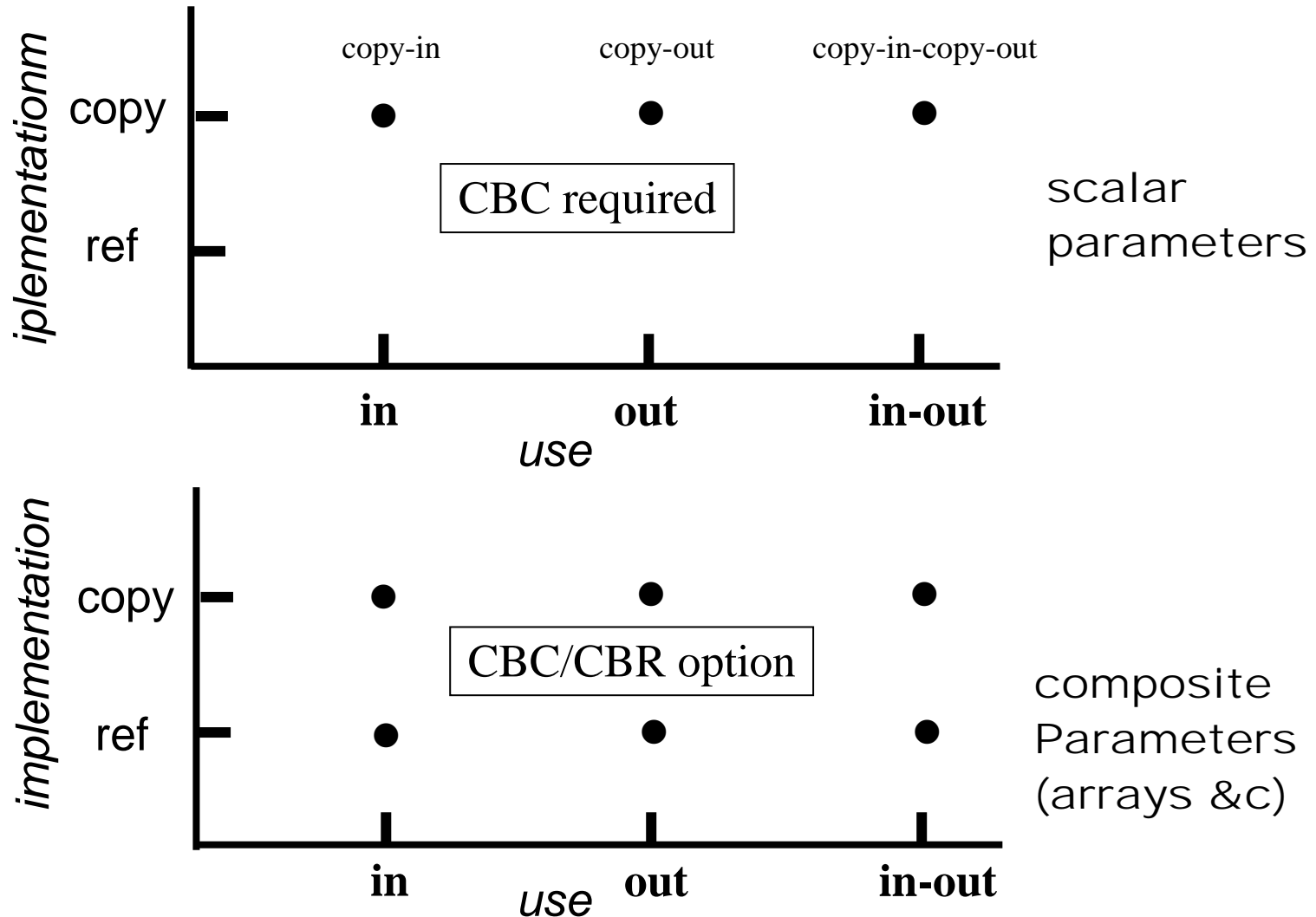
# Modes Differ

- **Definitional Modes (call time binding)**
  - Call as constant CAC example  
1 error
  - Call by reference CBR 2 3 3 3 9
- **Copying Modes (call time passing)**
  - Call by value CBV 1 3 3 1 9
  - Call by copy CBC 1 3 3 3 9
    - ◆ Copy-in/copy-out
  - Call by value-result CBVR 1 3 3 3 3
- **Delay Modes (reference time passing)**
  - Call by text CBT 2 8 6 3 9
  - Call by name CBN 2 12 9 3 9
  - Call by need
    - ◆ R-value CBNeed-R 2 6 6 1 9
    - ◆ L-Value CBNeed-L 2 12 12 3 9



# Ada Parameters

- Attempt at orthogonality of *use* vs *implementation*



# Arrays: by ref or by copy?



```
void function P(int x[])
```

```
{ ... x[i1] ... x[i2] . . . x[in] ... }
```

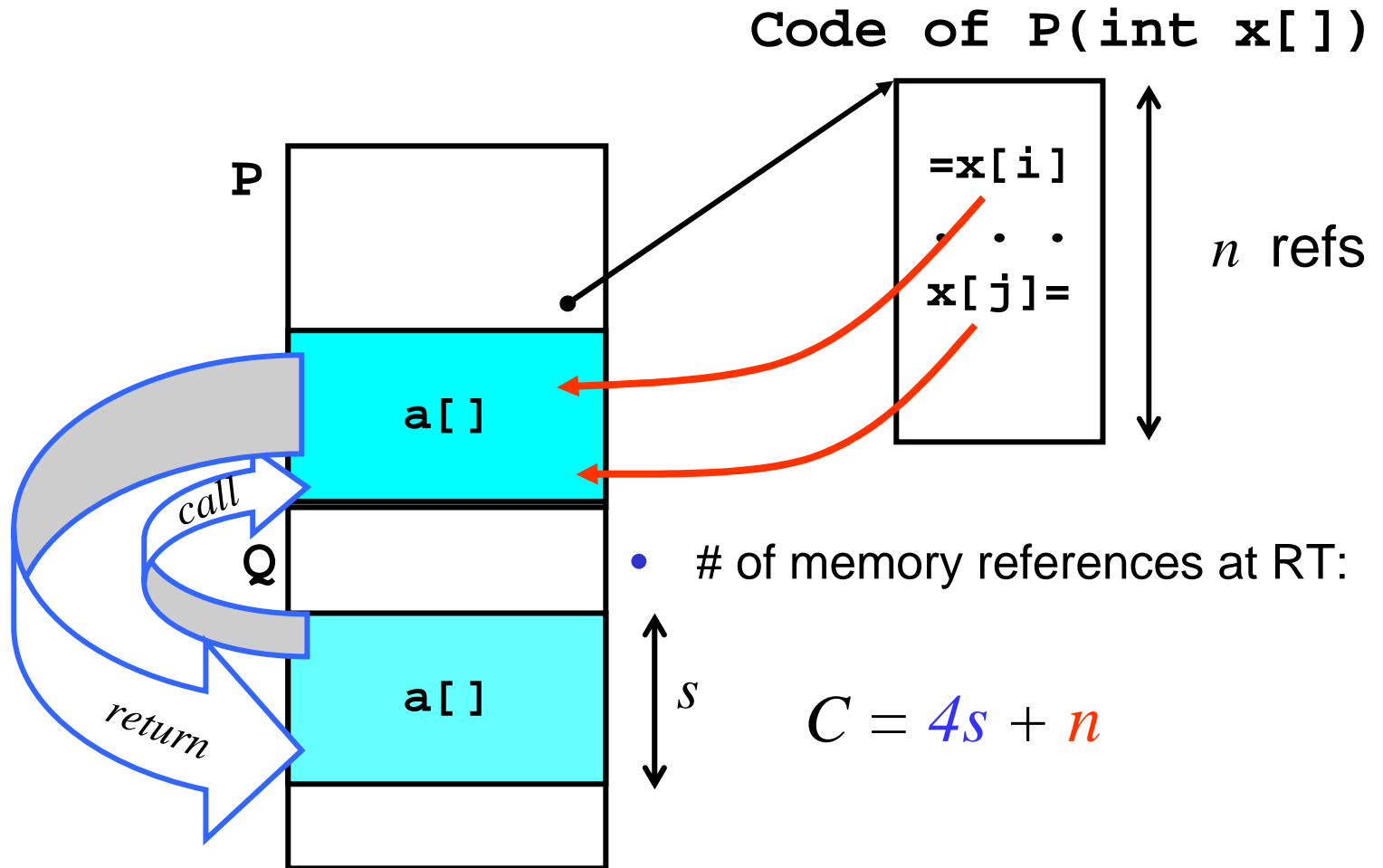


$n$  references to elements of formal `x[ ]` at RT ( $n$  known at RT)

- Call by reference: copy a pointer to `a[ ]` into AR for `P(a[ ])`
  - Each reference `x[i]` becomes indirect address through pointer to original argument `a[ ]` in caller; loads and stores reflected immediately in original array
- Call by copy: copy argument `a[ ]` into AR for `P(a[ ])` & overwrite original `a[ ]` from copy on return
  - Each reference `x[i]` directly addresses copy; stores and loads made to copy

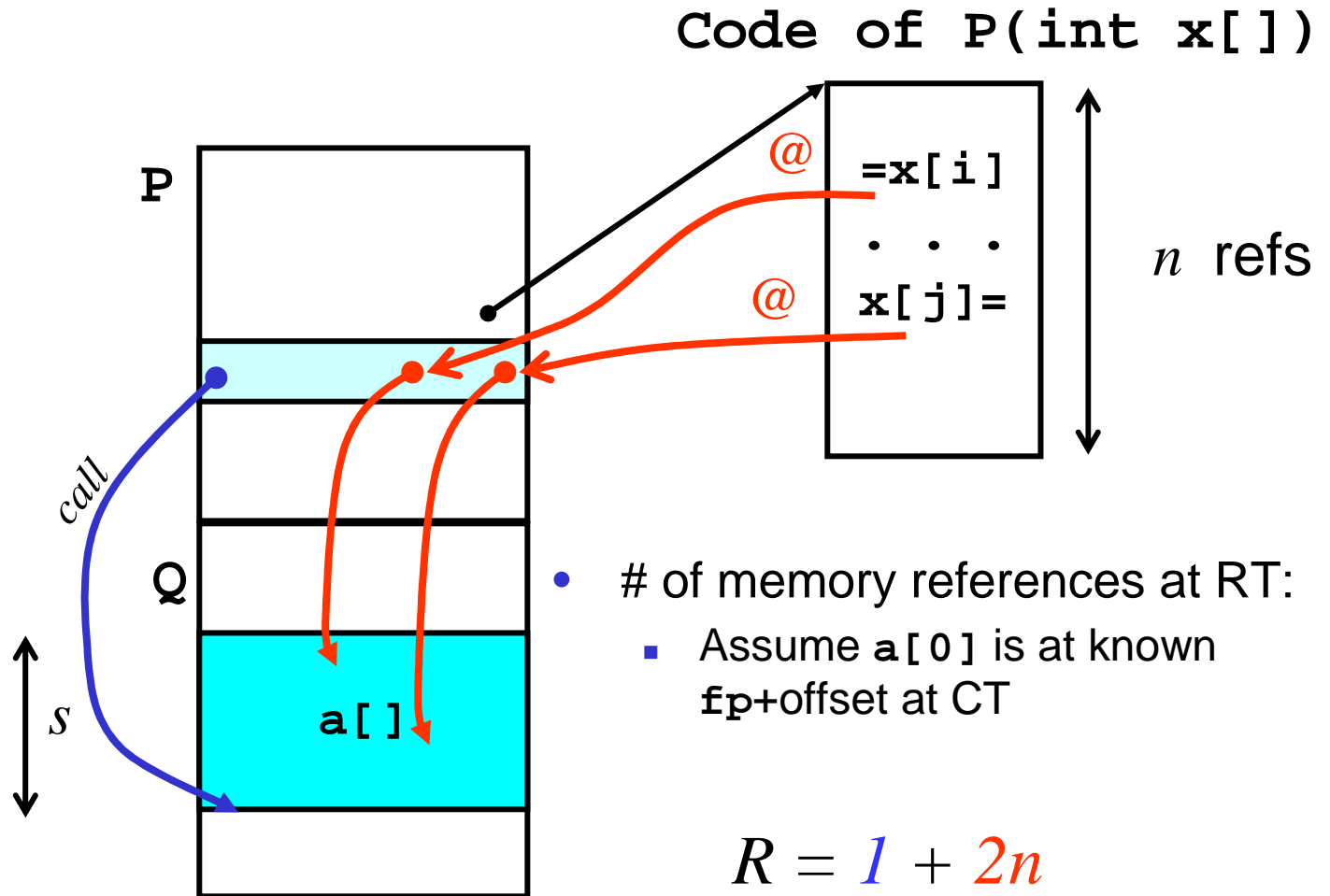
# by ref or copy? (cont.)

- Q calls  $P(a[])$  by copy:



# by ref or copy? (cont.)

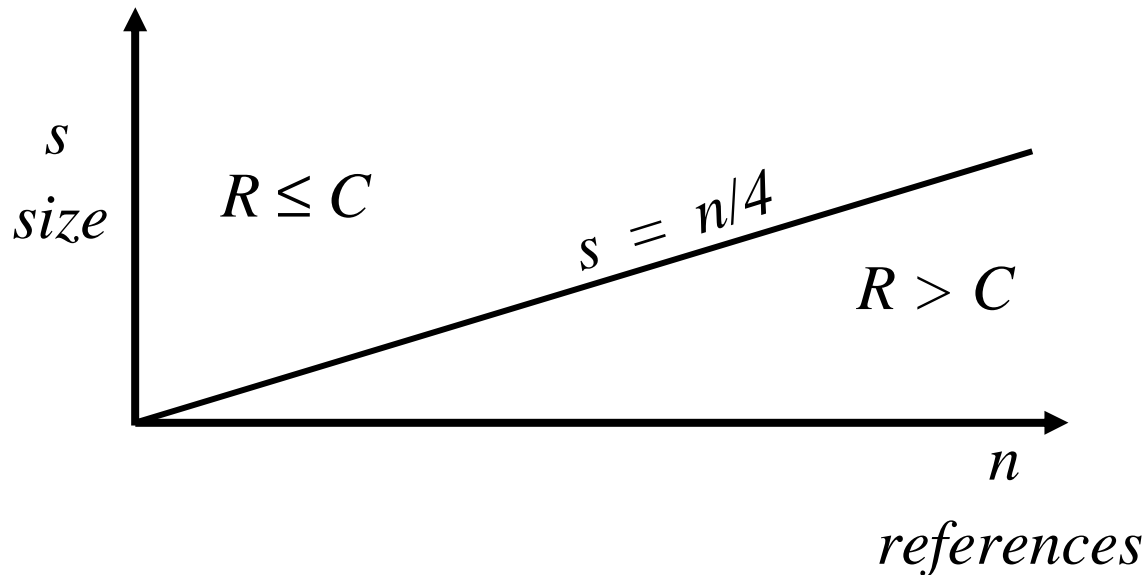
- Q calls  $P(a[])$  by reference:





# by ref or copy? (cont.)

- $R > C \Leftrightarrow 1 + 2n > 4s + n \Leftrightarrow n > 4s - 1 \Leftrightarrow n \geq 4s$



- Reference density:  $n / s = \text{ave. \# references per element}$
- Copying less expensive than reference:  
$$R > C \Leftrightarrow n / s \geq 4$$

# More on Call By Name

---

Most curious mode ever invented. Pros and Cons.

- CBN's main characteristics:
  - Defers evaluation of actual argument expressions
  - Re-evaluates the argument expression at each use of formal
    - So arg value can actually change from one ref to another

- Can simulate lazy evaluation

example: short circuit booleans

```
boolean procedure cand(p, q) ;
```

```
  boolean p, q ;
```

```
  if p then cand := q else cand := false ;
```

```
end
```

- Cannot be written as a procedure in an “eager” programming language (like Scheme)

# CBN (cont.)

---

- “Jensen’s Device” –weird sort of polymorphism

Example:

```
real procedure sigma(x, j, n);  
  value n; real x; integer j, n;  
begin real s;  
  s := 0;  
  for j := 1 step 1 until n do s := s + x;  
  sigma := s  
end
```

- $\text{sigma}(a(i), i, 3) \Rightarrow a(1) + a(2) + a(3)$
- $\text{sigma}(a(k)*b(k), k, 2) \Rightarrow a(1)*b(1) + a(2)*b(2)$

# CBN (cont.)

---

Example:

```
begin comment zero vector
procedure zero(elt, j, lo, hi);
  value lo, hi; integer elt, j, lo, hi;
  begin
    for j := lo step 1 until hi do
      elt := 0;
    end
integer i; integer array a[1:10], b[1:5, 1:5];
zero(a[i], i, 1, 10);
zero(b[i, i], i, 1, 5);
end
```

# CBN (cont.)

- Limitations of CBN: the obvious “swap” algorithm fails

**begin**

```
procedure swap(a, b);
```

```
integer a, b;
```

```
begin integer t;
```

```
  t := b; b := a;
```

```
  a := t;
```

```
end;
```

```
integer array a[1:10];
```

```
integer i;
```

```
i := 1; a[i] := 2;
```

```
// i=1 a[1]=2
```

```
swap(a[i], i);
```

```
//(a[1],i)=(2,1)
```

**end**

```
swap(a[i], i) //i==2 &  
              //a[1]==2
```

```
t := i // t==1
```

```
i := a[i] // i==2
```

```
a[i] := t // a[2]==1
```

```
//(a[1],i)=(2,2)
```

- Reordering code doesn't help;  
swap(i, a[i]) fails

# CBN (cont.)

---

- Proposed “solution”: assume in  $t := s$  that the target l-value is computed before the source r-value

```
procedure swap(a, b); integer a, b;
begin
  integer procedure testset(t,s); integer t,s;
  begin
    testset := t;      //ret. old r-val of target
    t := s;           //assign source r-val to target
  end;
  a := testset(b, a);
end
```

```
swap(a[i], i)  $\Longrightarrow$  a[i]:=testset(i,a[i])  $\Longrightarrow$ 
  ts:=i; i:=a[i]; a[i]:=ts
```

# CBN (cont.)

---

- Problem: proposed “solution” has a bug.
  - Difficulty is the re-evaluation of actual on each use of formal
  - Can arrange an actual that yields a distinct l-value on each use

```
begin integer array a[1:10]; integer j;  
  integer procedure i; comment return next integer;  
    begin j := j + 1; i := j end;  
  j := 0; swap(a[i], a[i])  
end
```

- `a[i] := testset(a[i], a[i])`  $\Rightarrow$   
 `ts := a[i]; a[i] := a[i]; a[i] := ts;`  $\Rightarrow$   
 `ts := a[1]; a[2] := a[3]; a[4] := ts;`